



A New Proposed Model for Covid-19

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Abstract

During the broadcast of COVID-19 (Coronavirus) across the world, many mathematicians made several mathematical models, to understand the forecast and behavior of this epidemic's spread accurately. Nevertheless, due to the lack of much information about it, the application of many models has become difficult and sometimes impossible, unlike the simple SIR model. In this study we proposed a new SIRD model for COVID-19. SIRD model is fitted to real data of COVID-19 patients in Egypt using R program, the sample consists of all patients in the susceptible state, infectious state, removed state, and the death state. The purpose of this study is to give a prediction of the epidemic peak and sizes in our country. The results of this study are an indicator for the widespread of COVID-19 in Egypt.

Key words: Mathematical model; COVID-19 pandemic; SIR model; SIR model; SIR model; SIRD model.

1. Introduction

The use of mathematical models in public health such as SIR models play an essential role in many aspects, for example: rapid visualization of epidemiological information, monitoring, prediction and estimating the spread of disease, and helping in decision-making on pandemic prevention and control (Layati et al, 2021).

As stated by the World Health Organization (WHO) report worldwide, as of March 7th, 2022 since the outbreak of COVID-19 was reported in December 2019, there have been 448 million confirmed positive states of COVID-19, including 6.01 million deaths and over 93.3 million who have recovered. In Africa, as of August 8th, 2021, 7,075,119 confirmed positive states have been reported with a total of over 3.27 million deaths (Mayabi et al, 2022).

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2. Mathematical Model & Materials

The topic was formalized by Kermack and McKendrick in 1927, who wrote down the first accurate mathematical models for disease transmission in a format that is still used today. The SIR model represents the spread of infectious diseases from which recovered individuals get immunity from re-infection (Black, 2010).

Mitra (2020) studied the epidemic patterns of Covid-19 in India during the period 30 Jan to 10 July 2020 from a mathematical modeling perspective using SIR model with an aim to forecast the precise description of the disease. Marques et.al (2022) proposed a discretized SIR compartmental model as a driving dynamics of disease dissemination through a spatially distributed multipopulational. Olu et.al (2023) used the compartmental model in this study to analyze COVID-19 cumulative and active cases in Nigeria during the year 2020. Sahran & Tee (2023) identified in this study the trend of the COVID-19 outbreak before and after the vaccination campaign by using the Susceptible-Exposed-Infectious-Recovered (SEIR) and Susceptible-Exposed-Infectious-Recovered-Vaccinated (SEIRV) models. Ahmed et.al (2023) analyzed the COVID-19 SIR model and characterized its positivity and boundness properties. Choi et.al (2023) The primary aim of this research is to estimate the number of COVID-19 cases through the analysis of SARS-CoV-2 derived from wastewater samples. Pathak et.al. (2024) proposed a model using a simple SIR model for analysis of the spread and control of COVID-19 pandemic in India after the subsequent lockdown by considering the approach of partial measures. Vanderpas et.al (2024) The trajectory of COVID-19 epidemic waves in the general population of Belgium was analyzed by defining quantitative criteria for epidemic waves from March 2020 to early 2023. The SIR compartmental model was applied to the first epidemic wave.

In this study we proposed a new SIRD model for COVID-19 to improve the SIR model for predicting the numbers of deaths of COVID-19 patients during the prevalence of pandemic in Egypt and to estimate the parameters of the proposed SIRD model. SIRD model is applied to a real data to investigate the dynamics of COVID-19 in Egypt.

The following figure shows the states of the proposed SIRD model and the possible transmissions between them.

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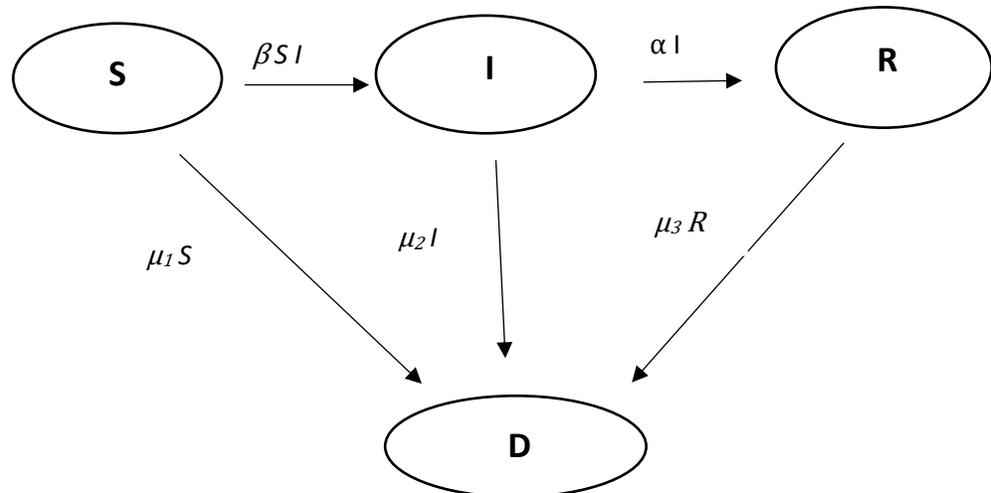


Figure (1): The proposed *SIRD* model

The Proposed SIRD Model

The proposed SIRD model is a system of ordinary differential equations which is defined as follows:

$$\frac{dS}{dt} = -\beta SI$$

$$\frac{dI}{dt} = \beta SI - \alpha I$$

$$\frac{dR}{dt} = \alpha I$$

$$\frac{dD}{dt} = \mu_1 S + \mu_2 I + \mu_3 R$$

with initial conditions $S(0) = S_0 > 0$, $I(0) = I_0 > 0$, $R(0) = R_0$, $D(0) = 0$, and the total population $N = S + R + I + D$. The transmission rate is β , the recovery rate is α and the death rate is μ .

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If the values of parameters are not known, some simple observations about the solutions to the proposed SIRD system can be made that hold for each or a big set of possible parameter values.

- a) Suppose $N(t) = S(t) + I(t) + R(t) + D(t)$ denotes the total population. Thus, by adding the equations of SIRD model it turns out that,

$$\frac{dN}{dt} = 0,$$

Thus, the total population $N(t) = N_0 = S_0 + I_0 + R_0$ remains constant.

- b) From the equation $\frac{dS}{dt} = -\beta SI$ shows that $\frac{dS}{dt} \leq 0$.

So that, $S(t)$ is always decreasing. Especially $S(t) \leq S_0$.

- c) Rewrite the equation $\frac{dI}{dt} = \beta SI - \alpha I$ as follow:

$$\frac{dI}{dt} = (\beta S - \alpha) I.$$

Then, the following two cases occur:

1. If $S_0 < \frac{\alpha}{\beta}$, then $\frac{dI}{dt} |_{t=0} < 0$. Since $S(t) \leq S_0 \leq \frac{\alpha}{\beta}$, and $I'(t) < 0$ for all $t \geq 0$, and thus $I(t)$ strictly decreases. As a conclusion, no epidemics can occur in this case.
2. If $S_0 > \frac{\alpha}{\beta}$, then $S(t) > \frac{\alpha}{\beta}$ for $t \in [0, \bar{t})$ for some $\bar{t} > 0 > 0$. This implies $I'(t) > 0$ and thus $I(t)$ strictly increases for $t \in [0, \bar{t})$. As a conclusion, an epidemic happens.

The main assumptions of the proposed SIRD model are:

- The population remains constant over time, who make up the population move from susceptible to infected.

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- The population leaves the infected state recovering from the disease, and those who manage to do so acquire immunity and so can no longer be infected again.
- The death state is added in the proposed SIRD model.
- The population is closed, so, no one from the outside enters the population, and no one leaves the population except the death states. The influx of new susceptible is zero, and so are the removal rates from all states.
- Individuals become infected regardless of age, sex, social status.
- Constant rates (for example: transmission, removal rates)
- The latent period for the disease is ignored.
- Well-mixed population (Allen,2010; Allen,2017; Hethcote, 2000; Brauer et al, 2008; Martcheva, 2015; Li, 2018).

The Proposed SIRD as a Markov Chain

Ching & Ng (2006) defined the transitions probabilities as follows:

The probability P_{ij} represents transition probabilities from an illness state i at to another illness state j .

$$P_{ij} = P(X_n = j | X_{n-1} = i) \quad i, j = 0, 1, 2, \dots \quad n \geq 0.$$

The transitions probability matrix is defined as follows:

$$P = \begin{bmatrix} p_{11} & p_{12} & p_{13} & p_{14} \\ p_{21} & p_{22} & p_{23} & p_{24} \\ p_{31} & p_{32} & p_{33} & p_{34} \\ p_{41} & p_{42} & p_{43} & p_{44} \end{bmatrix}$$

P is (4×4) square transition probability matrix. The elements of these matrix p_{ij} represent that the patient will be in state j (the future), given it is in state i (the present).

For all i, j in the transition probability matrix there are two conditions:

1. $P_{i,j} \geq 0$,

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$$2. \sum_{j \in N} P_{i,j} = 1.$$

Every row in the probability matrix P shows a vector of transition probabilities where the sum of elements in every row is one. The value of off-diagonal elements of the probability matrix shows the probability of movement between classes and the value of the diagonal matrix shows the probability of a class remaining in year $(t + 1)$ in the same class as in year t (Shabani & Shahnazi, 2020).

According to the data, the state space for the Markov chain consists of four elements defined as follows:

$$C = \{S, I, R, D\}$$

As regards the SIR model, the model supposes the time is discrete, the variable t takes values in $\{0, 1, 2, \dots\}$, so the random variables which define the various states of the Markov chain are discrete. In the SIR model, the elements of the population are classified into three states: Susceptible (S), Infected (I), and Recovered (R).

The transitions probability matrix of the proposed SIRD is defined as follows:

$$P = \begin{bmatrix} -\beta SI - \mu_1 S & \beta SI & 0 & \mu_1 S \\ 0 & \beta SI - \alpha I - \mu_2 I & -\alpha I & \mu_2 I \\ 0 & 0 & \alpha I - \mu_3 R & \mu_3 R \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0.2 & 0.6 & 0 & 0.2 \\ 0 & 0.2 & 0.3 & 0.5 \\ 0 & 0 & 0.6 & 0.4 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

From the transitions probability matrix it is noticed that $p_{11} = -\beta SI - \mu_1 S$ which means that the probability of being in the susceptible state = 0.2, $p_{12} = \beta SI$ the probability of transmission from susceptible state to infected state = 0.6, $p_{14} = \mu_1 S$ the probability of transmission from susceptible state to death state = 0.2, $p_{22} = \beta SI - \alpha I - \mu_2 I$ the probability of being in the infected state = 0.2, $p_{23} = -\alpha I$ the probability of transmission from infected state to removable state = 0.3, $p_{24} = \mu_2 I$ the probability of transmission from infected state to death state = 0.5, $p_{33} = \alpha I - \mu_3 R$ the probability of being in the removable state = 0.6, $p_{34} = \mu_3 R$ the probability of transmission from removable state to death state = 0.4 and finally $p_{44} = 1$ the probability of being in the death state the absorbing state.

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3. Data Description

The total sample of patients consists of 500 COVID-19 patients in the period of the prevalence of the COVID-19 pandemic especially in the first year of its prevalence in 2020 in Egypt. They represent a random sample, and the data of COVID-19 patients is regarded as states of SIRD model. SIRD patients transmit from state to another state in a stochastic manner. Using the R program, the data are supplied to R as a series of states, grouped by patients.

4. Results

The sample size was divided into five groups as follows: 100, 200, 300, 400 and 500.

The first group:

The first group consists of 100 COVID-19 patients and their results are as follows:

Table(1): Results of the first group n = 100

| time | S | I | R | D |
|------|----------|----------|----------|----------|
| 0 | 99 | 1 | 0 | 0 |
| 1 | 98.54037 | 1.343295 | 0.11634 | 10.58723 |
| 2 | 97.92695 | 1.800597 | 0.272451 | 21.38685 |
| 3 | 97.11185 | 2.406738 | 0.481412 | 32.46884 |
| 4 | 96.03497 | 3.204846 | 0.760188 | 43.92414 |
| 5 | 94.62297 | 4.24654 | 1.130492 | 55.86932 |
| 6 | 92.78984 | 5.590592 | 1.61957 | 68.4511 |
| 7 | 90.44028 | 7.298968 | 2.260757 | 81.84963 |
| 8 | 87.47759 | 9.428977 | 3.093434 | 96.27894 |
| 9 | 83.81744 | 12.02059 | 4.161974 | 111.9823 |
| 10 | 79.4075 | 15.07933 | 5.513178 | 129.2195 |
| 11 | 74.25044 | 18.55766 | 7.191897 | 148.2454 |
| 12 | 68.42381 | 22.34123 | 9.234961 | 169.2789 |
| 13 | 62.08761 | 26.24808 | 11.66431 | 192.4674 |
| 14 | 55.47201 | 30.04698 | 14.481 | 217.8549 |

The results of the first group show the risk of the COVID-19 pandemic where there are increases in the number of deaths by the time from 0 on the first day until reaching 218 cases at the end of 15 days.

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The following table shows the summary of the SIRD model of the first group:

Table (2): Summary of the SIRD model of n = 100

| | S | I | R | D |
|---------|----------|----------|----------|----------|
| Min. | 1.964897 | 0.043174 | 0 | 0 |
| 1st Qu. | 1.998341 | 0.431673 | 55.76113 | 572.6826 |
| Median | 2.363016 | 2.96055 | 93.37945 | 1212.301 |
| Mean | 17.47412 | 9.707089 | 72.8188 | 1144.967 |
| 3rd Qu. | 10.64055 | 15.07933 | 97.56999 | 1723.782 |
| Max. | 99 | 40.54584 | 97.99193 | 2220.531 |
| N | 100 | 100 | 100 | 100 |
| sd | 30.05438 | 12.72971 | 34.76767 | 679.8512 |

It is noticed from the table of n= 100 that the data does not belong to the normal distribution and the standard deviation is increased especially for removed states and death states which refer to Extremely dangerous of COVID- 19.

The following table shows the Maximum likelihood estimations for the first group:

Table(3): Maximum likelihood estimations for n = 100

| Parameter | Estimate | SE |
|-----------|----------|---------|
| Beta | -13.7892 | 7.01289 |
| Gamma | -9.5689 | 6.02598 |
| Sigma 1 | 6.7823 | 4.28941 |
| Sigma 2 | 5.68921 | 3.02698 |
| Sigma 3 | 7.2587 | 4.69861 |

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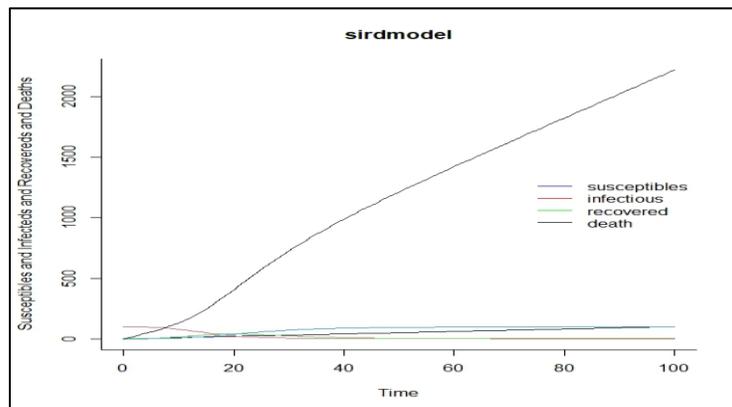


Figure (2): SIRD model at n=100

Figure (2) shows SIRD model when the sample size is equal to 100 of the COVID-19 patients and it is obvious that the number of deaths increases through time from 0 until reaching to 2221 at the end of 100 day which shows the severity of COVID-19.

The second group:

The second group consists of 200 COVID-19 patients and their results are as follows:

Table (4): Results of the second group n = 200

| time | S | I | R | D |
|------|----------|----------|----------|----------|
| 1 | 199 | 1.00+00 | 0 | 0 |
| 2 | 197.854 | 2.00+00 | 0.144391 | 20.72834 |
| 3 | 195.5872 | 3.98+00 | 0.432459 | 42.19589 |
| 4 | 191.1849 | 7.81+00 | 1.001594 | 65.1101 |
| 5 | 182.9296 | 1.50e+01 | 2.105087 | 90.77696 |
| 6 | 168.4177 | 2.74e+01 | 4.171442 | 121.4122 |
| 7 | 145.5733 | 4.66e+01 | 7.815629 | 160.2165 |
| 8 | 115.1443 | 7.12e+01 | 13.67797 | 210.5823 |
| 9 | 82.3886 | 9.56e+01 | 22.04649 | 274.1907 |
| 10 | 54.09202 | 1.13e+02 | 32.56551 | 349.5016 |
| 11 | 33.68946 | 1.22e+02 | 44.40299 | 432.5303 |
| 12 | 20.6112 | 1.23e+02 | 56.68673 | 519.0028 |
| 13 | 12.70738 | 1.19e+02 | 68.77805 | 605.7362 |
| 14 | 8.014126 | 1.12e+02 | 80.30251 | 690.8182 |
| 15 | 5.208055 | 1.04e+02 | 91.07752 | 773.2689 |

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The results of the second group show the risk of the COVID-19 pandemic where there are increases in the number of deaths by the time from 0 on the first day until reaching 773 cases at the end of 15 days.

The following table shows the summary of the SIRD model of the second group:

Table (5): Summary of the SIRD model of n = 200

| | S | I | R | D |
|---------|----------|----------|----------|----------|
| Min. | 0.066936 | 1.07e-06 | 0 | 0 |
| 1st Qu. | 0.066936 | 1.53e-04 | 196.7965 | 2624.328 |
| Median | 0.066994 | 2.19e-02 | 199.9111 | 4626.445 |
| Mean | 8.191285 | 1.00e+01 | 181.8099 | 4557.791 |
| 3rd Qu. | 0.075884 | 2.56e+00 | 199.9329 | 6616.199 |
| Max. | 199 | 1.23e+02 | 199.9331 | 8605.866 |
| N | 200 | 200 | 200 | 200 |
| sd | 35.29945 | 2.56E+01 | 47.2945 | 2423.292 |

It is noticed from the table that the data does not belong to the normal distribution and the standard deviation is increased especially for removed states and death states which refer to Extremely dangerous of COVID- 19.

The following table shows the Maximum likelihood estimations for the second group:

Table (6): Maximum likelihood estimations of n = 200

| Parameter | Estimate | SE |
|-----------|----------|---------|
| Beta | -11.7892 | 6.58320 |
| Gamma | -8.96321 | 5.58961 |
| Sigma 1 | 6.02631 | 3.45221 |
| Sigma 2 | 5.00045 | 2.00554 |
| Sigma 3 | 7.00111 | 3.96621 |

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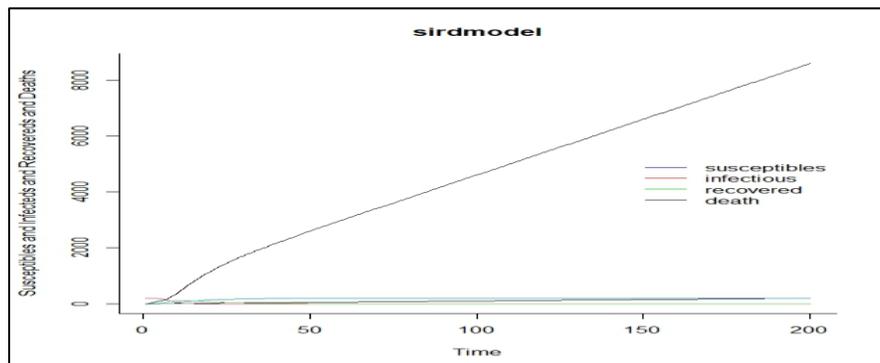


Figure (3): SIRD model at n=200

Figure (3) shows the SIRD model when the sample size equals 200 of the COVID-19 patients and it is obvious that the number of deaths increase through time from 0 until reach to 8606 at the end of 200 days which shows the severity of COVID-19.

The third group:

The third group consists of 300 COVID-19 patients and their results are as follows:

Table (7): Results of the third group n = 300

| time | S | I | R | D |
|------|----------|----------|----------|----------|
| 1 | 2.99e+02 | 1.00e+00 | 0 | 0 |
| 2 | 2.97e+02 | 2.98e+00 | 0.181516 | 30.91503 |
| 3 | 2.91e+02 | 8.75e+00 | 0.718516 | 63.64031 |
| 4 | 2.73e+02 | 2.46e+01 | 2.260371 | 101.4855 |
| 5 | 2.32e+02 | 6.17e+01 | 6.350485 | 152.3358 |
| 6 | 1.61e+02 | 1.23e+02 | 15.47148 | 228.9799 |
| 7 | 8.67e+01 | 1.82e+02 | 30.95546 | 338.6717 |
| 8 | 3.91e+01 | 2.10e+02 | 50.85548 | 472.2393 |
| 9 | 1.67e+01 | 2.11e+02 | 72.07315 | 614.4734 |
| 10 | 7.34e+00 | 2.00e+02 | 92.69005 | 755.8055 |
| 11 | 3.40e+00 | 1.85e+02 | 111.9368 | 892.2836 |
| 12 | 1.68e+00 | 1.69e+02 | 129.6042 | 1022.711 |
| 13 | 8.80e-01 | 1.53e+02 | 145.7031 | 1146.983 |
| 14 | 4.90e-01 | 1.39e+02 | 160.3236 | 1265.399 |
| 15 | 2.89e-01 | 1.26e+02 | 173.5797 | 1378.385 |

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The results of the third group show the risk of the COVID-19 pandemic where there are increases in the number of deaths by the time from 0 on the first day until reaching 1378 cases at the end of 15 days.

The following table shows the summary of the *SIRD* model of the third group:

Table (8): Summary of the SIRD model of n =300

| | S | I | R | D |
|---------|----------|----------|----------|----------|
| Min. | 1.84e-03 | 7.02e-11 | 0 | 0 |
| 1st Qu. | 1.84e-03 | 9.34e-08 | 299.7068 | 5527.81 |
| Median | 1.84e-03 | 1.65e-04 | 299.998 | 10013.96 |
| Mean | 5.70e+00 | 1.00e+01 | 284.2981 | 9952.941 |
| 3rd Qu. | 1.86e-03 | 2.91e-01 | 299.9982 | 14498.95 |
| Max. | 2.99e+02 | 2.11e+02 | 299.9982 | 18983.93 |
| N | 300 | 300 | 300 | 300 |
| sd | 3.73e+01 | 3.40+01 | 54.14817 | 5305.774 |

It is noticed from the table of n = 300 that the data does not belong to the normal distribution and the standard deviation is increased especially for removed states and death states which refer to extremely dangerous of COVID-19.

The following table shows the Maximum likelihood estimations for the third group:

Table(9): Maximum likelihood estimations of n = 300

| Parameter | Estimate | SE |
|-----------|-----------|---------|
| Beta | -10.00111 | 4.00125 |
| Gamma | -6.32587 | 2.98651 |
| Sigma 1 | 5.65891 | 2.56234 |
| Sigma 2 | 3.45789 | 1.98521 |
| Sigma 3 | 5.75321 | 2.98433 |

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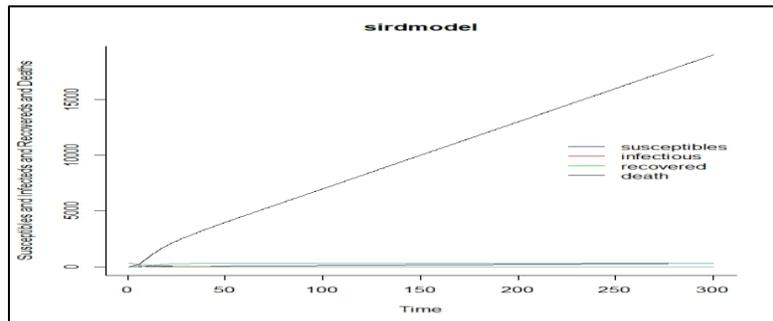


Figure (4): SIRD model at n=300

Figure (4) shows the SIRD model when the sample size equals 300 COVID-19 patients, and it is obvious that the number of deaths increases through time from 0 until reach to 18984 deaths at the end of 300 days which shows the severity of COVID-19.

The Fourth group:

The fourth group consists of 400 COVID-19 patients and their results are as follows:

Table (10): Results of the fourth group n = 400

| time | S | I | R | D |
|------|----------|----------|----------|----------|
| 1 | 3.99e+02 | 1.00e+00 | 0 | 0 |
| 2 | 3.95e+02 | 4.44e+00 | 0.231009 | 41.16383 |
| 3 | 3.80e+02 | 1.91e+01 | 1.239479 | 86.26788 |
| 4 | 3.23e+02 | 7.18e+01 | 5.291525 | 146.8113 |
| 5 | 1.95e+02 | 1.87e+02 | 17.84486 | 250.6376 |
| 6 | 7.44e+01 | 2.84e+02 | 41.98669 | 414.2567 |
| 7 | 2.25e+01 | 3.06e+02 | 71.94035 | 609.7038 |
| 8 | 6.76e+00 | 2.91e+02 | 101.9329 | 808.3727 |
| 9 | 2.21e+00 | 2.68e+02 | 129.9169 | 999.9048 |
| 10 | 7.94e-01 | 2.44e+02 | 155.4893 | 1182.057 |
| 11 | 3.14e-01 | 2.21e+02 | 178.7091 | 1354.885 |
| 12 | 1.35e-01 | 2.00e+02 | 199.7478 | 1519.019 |
| 13 | 6.31e-02 | 1.81e+02 | 218.7954 | 1675.2 |
| 14 | 3.17e-02 | 1.64e+02 | 236.035 | 1824.154 |
| 15 | 1.70e-02 | 1.48e+02 | 251.6361 | 1966.556 |

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The results of the fourth group show the risk of the COVID-19 pandemic where there are increases in the number of deaths by the time from 0 on the first day until reaching 1967 cases at the end of 15 days.

The following table shows the summary of the SIRD model of the fourth group:

Table (11): Summary of the SIRD model of n = 400

| | S | I | R | D |
|---------|----------|----------|----------|----------|
| Min. | 4.49e-05 | 5.92e-15 | 0 | 0 |
| 1st Qu. | 4.49e-05 | 7.97e-11 | 399.9719 | 9419.895 |
| Median | 4.49e-05 | 1.30e-06 | 400 | 17400.01 |
| Mean | 4.50e+00 | 1.00e+01 | 385.5001 | 17343.1 |
| 3rd Qu. | 4.50e-05 | 2.80e-02 | 400 | 25380.01 |
| Max. | 3.99E+02 | 3.06e+02 | 400 | 33360.01 |
| N | 400 | 400 | 400 | 400 |
| sd | 3.88e+01 | 4.07e+01 | 59.74384 | 9344.863 |

It is noticed from the table of n = 400 that the data does not belong to the normal distribution and the standard deviation is increased especially for removed states and death states which refer to Extremely dangerous of COVID- 19.

The following table shows the Maximum likelihood estimations for the fourth group:

Table (12): Maximum likelihood estimations of n = 400

| Parameter | Estimate | SE |
|-----------|----------|---------|
| Beta | -7.36925 | 2.11447 |
| Gamma | -3.98752 | 1.99884 |
| Sigma 1 | 3.55882 | 1.56478 |
| Sigma 2 | 1.96325 | 0.99876 |
| Sigma 3 | 2.98754 | 1.97452 |

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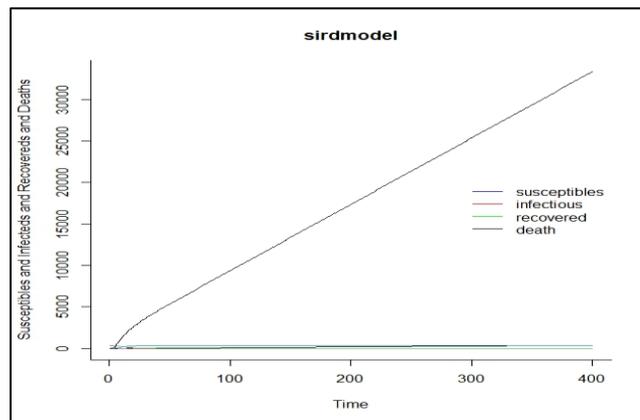


Figure (5): SIRD model at n = 400

Figure (5) shows the SIRD model when the sample size is equal to 400 of the COVID-19 patients and it is obvious that the number of deaths increases through time from 0 until reach to 33360 at the end of 400 days which shows the severity of COVID-19.

The fifth group:

The fifth group consists of 500 COVID-19 patients and their results are as follows:

Table (13): Results of the fifth group n = 500

| time | S | I | R | D |
|------|----------|----------|----------|----------|
| 1 | 4.99e+02 | 1.00e+00 | 0 | 0 |
| 2 | 4.93e+02 | 6.60e+00 | 0.297429 | 51.4976 |
| 3 | 4.57e+02 | 4.08e+01 | 2.195985 | 111.0878 |
| 4 | 3.08e+02 | 1.80e+02 | 12.03113 | 210.859 |
| 5 | 1.02e+02 | 3.59e+02 | 39.79993 | 402.1415 |
| 6 | 2.14e+01 | 4.00e+02 | 78.68748 | 652.4711 |
| 7 | 4.49e+00 | 3.78e+02 | 117.7692 | 907.7217 |
| 8 | 1.06e+00 | 3.45e+02 | 153.9224 | 1152.1 |
| 9 | 2.84e-01 | 3.13e+02 | 186.8012 | 1383.557 |
| 10 | 8.62e-02 | 2.83e+02 | 216.5905 | 1602.698 |
| 11 | 2.93e-02 | 2.56e+02 | 243.5556 | 1810.552 |
| 12 | 1.10e-02 | 2.32e+02 | 267.9578 | 2008.159 |
| 13 | 4.57e-03 | 2.10e+02 | 290.0388 | 2196.483 |
| 14 | 2.05e-03 | 1.90e+02 | 310.019 | 2376.403 |
| 15 | 9.97e-04 | 1.72e+02 | 328.0979 | 2548.719 |

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The results of the fifth group show the risk of the COVID-19 pandemic where there are increases in the number of deaths by the time from 0 on the first day until reaching 2548 cases at the end of 15 days.

The following table shows the summary of the SIRD model of the fifth group:

Table (14): Summary of the SIRD model of n = 500

| | S | I | R | D |
|---------|----------|----------|----------|----------|
| Min. | 1.03e-06 | 4.94e-19 | 0 | 0 |
| 1st Qu. | 1.03e-06 | 7.21e-14 | 499.9973 | 14311.32 |
| Median | 1.03e-06 | 1.05e-08 | 500 | 26786.33 |
| Mean | 3.77e+00 | 1.00e+01 | 486.2265 | 26731.99 |
| 3rd Qu. | 1.03e-06 | 2.67e-03 | 500 | 39261.33 |
| Max. | 4.99e+02 | 4.00e+02 | 500 | 51736.33 |
| N | 500 | 500 | 500 | 500 |
| sd | 4.00e+01 | 4.64e+01 | 64.67348 | 14540.29 |

It is noticed from the table of n = 500 that the data does not belong to the normal distribution and the standard deviation is increased especially for removed states and death states which refer to Extremely dangerous of COVID- 19.

The following table shows the Maximum likelihood estimations for the fifth group:

Table (15): Maximum likelihood estimations of n = 500

| Parameter | Estimate | SE |
|-----------|----------|---------|
| Beta | -5.56324 | 1.33661 |
| Gamma | -1.65832 | 0.95412 |
| Sigma 1 | 1.96210 | 0.99665 |
| Sigma 2 | 0.66523 | 0.00987 |
| Sigma 3 | 1.55221 | 0.69988 |

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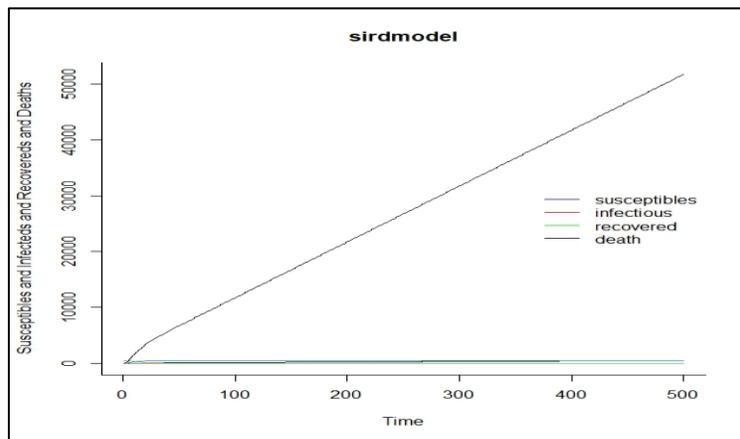


Figure (6): SIRD model at n = 500

Figure (6) shows the SIRD model when the sample size equals 500 of the COVID-19 patients and it is obvious that the number of deaths increases through time from 0 until reach to 51736 at the end of 500 days which shows the severity of COVID-19.

5. Conclusions:

In the present study, observed data of COVID-19 in Egypt in the first year of 2020 is analyzed using SIRD model with an aim to predict the precise description of the disease, such as, the spread of the disease, the probable peak date, the total number of infected, the total number of removed, the total number of deaths, the duration of an epidemic. SIRD model provides a method to investigate the risk of the epidemic disease COVID-19 and contributes to decision making in the face of future epidemics or pandemics. The SIRD mode helps government officials to take precautionary measures to prevent or decrease the risk of any epidemic or pandemic in the future.

From the analysis of COVID-19 data in the study sample:

- Most COVID-19 patients 66% of them has centered in the grade 3 which included: doctors, nursing staff, university teaching staff, engineers, managers, teachers, officers, computer engineers, businessmen, Lawyers and accountants.
- COVID-19 is more widespread in women than men and most of COVID-19 patients 62% are females, their age range from 20 to 40.
- The study showed that infection with COVID -19 is not affected by medical history which included patient history and smoking.

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