

**RHEOLOGICAL CONSTANTS OF THE FOUR
ELEMENTS BURGERS MODEL FOR POTATO
TUBERS AFFECTED BY VARIOUS FIXED LOADS
UNDER DIFFERENT STORAGE CONDITIONS**

Abd El-Maksoud, M. A. * Gamea, G. R. * Abd El-Gawad, A. M. **

ABSTRACT

The rheological constants of the four element Burgers model when potatoes (Diamont and Santana) were subjected to various fixed loads (stresses) on the main dimensions of the tubers were investigated .The rheological constants were K_1 (instantaneous elasticity ,N/mm)- K_2 (retarded elasticity ,N/mm)- C_1 (free viscous element ,N. min/mm and C_2 (retarded viscous element ,N. min/mm).The investigation was conducted for fresh and cured tubers as well as tubers under two different storage systems (trditional Nawalla at $16\pm 3^\circ\text{C}$; 84% RH and Cold store at 4°C ; 90% RH).

INTODUCTION

Potatoes are considering an agricultural biological material. Biological materials do not behave either as perfect elastic or perfect plastic materials. They exhibit both properties simultaneously. So, they are grouped under the definition of visco-elastic materials (Clevenger and Hamann, 1968-Mohsenin, 1970, Faborode and Callaphan ,1989.) In the same time, they show effects the dependent on time due to loading. The time dependent behavior of such viscoelastic materials may be described by constitutive equations whose variables are stress, deformation and time. These equations may be expressed by means of rheological models. Rheological models could describe and represent the behavior of biological materials. They help explain the stress, strain behavior of biological materials. The scope of the validity of such rheological models must be established by experiment. The most frequently applied quasistatic experimental methods, which can be utilized to determine viscoelastic properties of solid biological products like potatoes are creep and retardation and stress relaxation tests as well

* Assoc. Prof. of Ag. Eng. Dep. Fac. Of Ag. Menoufiya U.

** Eng. of Ag. Eng. Res. Center

as increasing the stress or deformation under constant rate. Models are mechanical analogues composed of element (springs and dashpots) where the ideal elastic behavior and the ideal viscous behavior are combined in different ways to model the actual behavior of the bio-materials. In stress relaxation test, the biological materials are deformed to a fixed strain and the strain is held constant. So the stress required to maintain this strain decreases with time. While in creep test, a constant load or stress is applied to the biological materials and the resulting (increasing) strain is measure with time. In fact this type of behavior is typical of fruits and vegetables. Besides it demonstrates the fact that the strain exhibited by the agricultural material under test is not independent of time (Mohsenin, 1978). Pitt and Chen 1983 stated that this time dependent can have a significant effect on the accuracy of predicted damage levels in fruits and vegetables during harvesting, handling transportation and storage . Datta and Morrow 1983 showed that the generalized kelven model (a series of kelven bodies) in series with Maxwell model must best represents the creep data obtained from apples, potatoes, and cheese. In this direction numerical attempts to fined a rheological model to represent the flesh of apples, potatoes, pear and other fruit as well as low, methoxyle pectingel preparations under condition of static creep have yielded the Burgers model (Reiner , 1960; Mohsenin , 1978). It can be seen in figure (1). The creep curves of apples (Skinner 1983), tomatoes (Abdel Maksoud , 1992) and grain dust (Chang and Martin ,1983) showed behavior identical to that of the four element Burgers model. In addition , Mohsenin 1986 sited that the frequently used rheological model which may represents the creep behavior is the four element Burger model as shown in figure (1) and added that the rheological equation biased on the model in creep and recovery test is given as follows:-

$$\varepsilon(t) = \sigma_0 \left[\frac{1}{E_0} + \frac{1}{E_r} (1 - e^{-t/T_{ret}}) + \frac{t}{\eta_v} \right]$$

Where:

ε = Strain t = time, min. σ_0 = stress, MPa

E_0 = instantaneous modulus or modulus at zero time

η = viscosity coefficient of the liquid in the dashpot, Mpa.min;

$\eta v =$ Viscosity, Mpa.min and $T_{ret} = \eta / E_r$ The time of relaxation.

This equation is based on the model consists of a Kelvin model connected in series to a spring and a dashpot element. The model may thus be divided into three parts A, B and C as shown in figure (1)

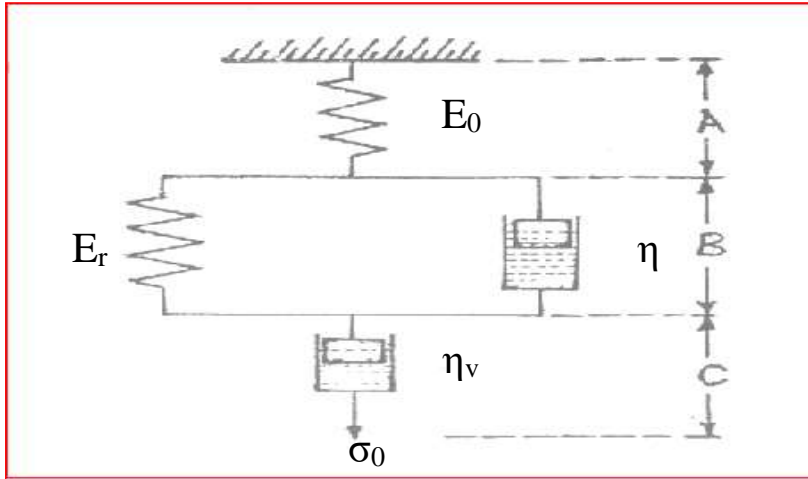


Figure (1): 4-element model (Burgers model)

In the same time figure (2) shows the behavior of the four elements Burgers model.

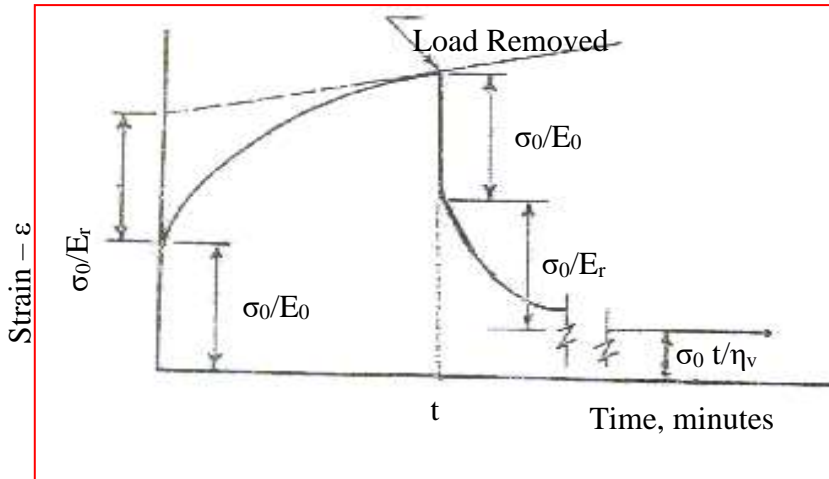


Figure (2): Typical creep and recovery curve in a viscoelastic material exhibiting instantaneous elasticity, retarded elasticity and viscous flow.

When the stress σ_0 is removed at time $t = t_1$, the elastic component of deformation ceases instantly, while the creep deformation decreases with time and tends asymptotically to the value σ_0 / E_0 and the recovery of strain during period $t > t_1$ will be

$$\varepsilon(t) = \left(\frac{\sigma_0}{E_r} \right) \left(e^{\frac{t_1}{T_r}} - 1 \right) e^{-\frac{t}{T_r}}$$

As shown in figure (2) the elements of the model may be determined from the loading – unloading curve, using the values of the intercepts of the

vertical axis, the deformation at $t=0$, $\varepsilon(0) = \left(\frac{\sigma_0}{E_0} \right)$ and the

deformation rate at $t = \infty$, $\varepsilon(\infty) = \frac{\sigma_0}{\eta_v}$.

Mohsenin 1986 illustrated a typical curve for creep and recovery test of Mackintosh apple as a relationship between deformation in inches and time in minutes as shown in figure (3).

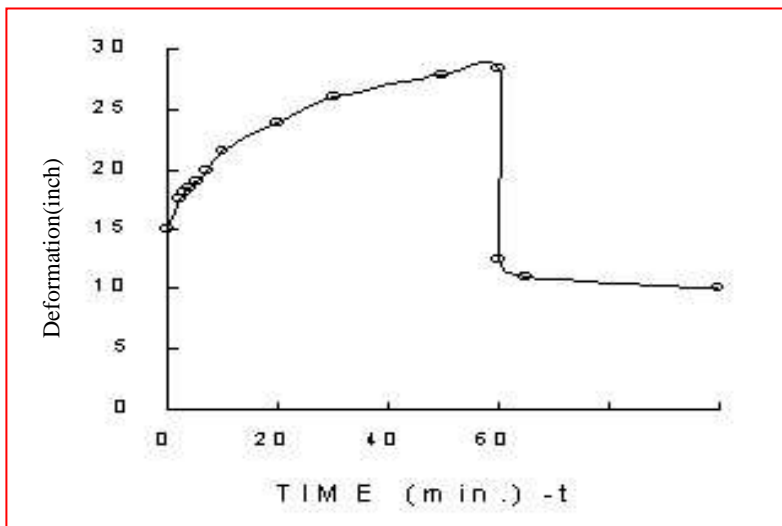


Figure (3): Distortion of McIntosh apple under dead load of 21 lbs determined by axial creep and recovery test with ¼ inch rigid plunger.

Similarly, Abd el Maksoud , 1992 and Sabbah et al.1994 used the four element Burgers model and the following equation as illustrated in figure (4) to determine the rheological constants of the model (K_1 , K_2 , C_1 , C_2) and their relations with fruit (tomatoes) parameters . They also reported results for predicting the fruit behavior under the effect of a static loading for a certain time in creep tests.

$$d(t) = F_0 \left[\frac{1}{K_1} + \frac{1}{K_2} (1 - e^{-t/T_{ret}}) + \frac{t}{C_1} \right]$$

Where :

- d = deformation, mm; t = time, min;
 F_0 = force, N; K_1 = instantaneous elasticity, N/mm;
 K_2 = retarded elasticity, N/mm;
 C_1 = free viscous element, N.min/mm;
 C_2 = retarded viscous element, N.min/mm; and $T_{ret} = C_2/ K_2$ The time of retardation.

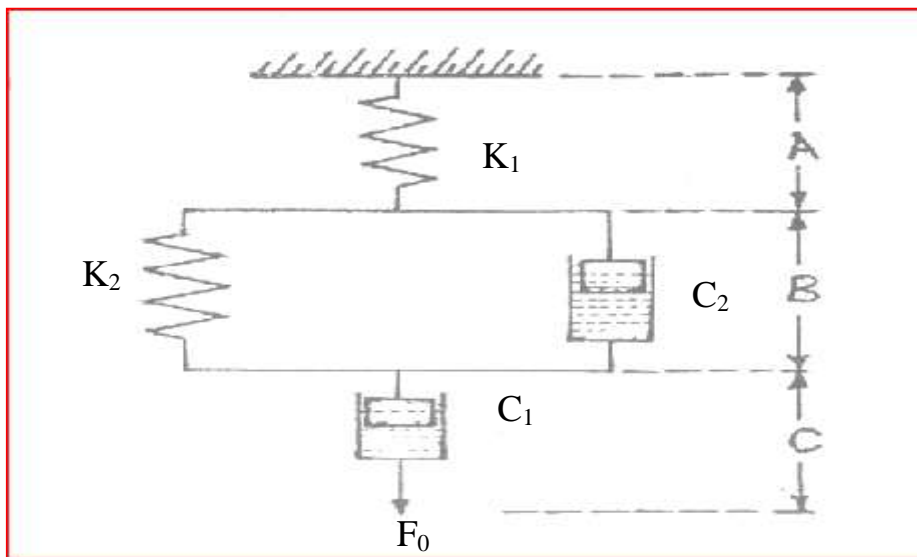


Figure.(4): 4-element model (Burgers model) where deformations are additive while the force is the same in all the three units A, B, and C.

Sabbah et al., 1994 reported that the deformation increases with increasing of loading level and stage of maturity .Generally, it was inversely proportional with fruit size under the same loading .Meanwhile ,they observed considerable variations throughout creep tests on individual fruits due to the non homogenous nature of tomatoes and the stress concentration set up by its irregular shape surface.

Knowledge of the rheological model constants by creep test experiments helps in describing the behavior of the biological material under the static load applied. These are essential for the designer of harvesting and handling equipment to estimate and even predict the amount of material damaged an applied load or deformation.

The specific objectives addressed by this investigation are:

- 1- Using the creep and recovery test to determine the viscoelastic properties of potato tubers through the constants of the rheological Burgers model.
- 2- Studying the effect of the storage time under two different storage systems and temperatures, potato tubers weight, the constant static load applied to tubers (constant stress) and the position of the effected load on the rheological constants of the model.

MATERIAL AND METHODS

180 for creep and recovery test experiments including, three load levels (10, 14 and 18N) two storage systems (Nawalla at $16\pm 3^{\circ}\text{C}$; 84% RH and Cold store at 4°C ; 90% RH), three loading positions (L – longitudinal , D – radial and T – minimum axis) and two potato varieties (Diamont and Santana) where each treatment was replicated three times for fresh, cured and stored 25,50 and 75 days were conducted to study the rheological properties of potatoes during the mentioned stages. The procedure to conduct the creep test was run by using the creep test device. It was constructed specifically according to the creep test device used by (Abdel – Maksoud, 1992 and Sabah et al, 1994) as shown in figure (5). Experiments were run by placing the potato tuber between two parallel plates. The tuber was placed on the base of the apparatus in the considered position while, the crosshead was just touching its surface at zero loading condition. The tuber was then loaded by the concerned fixed load. The instantaneous deformation with time was indicated by the dial micrometer and then recorded as illustrated in table (1). The total time of

every test was one hour. It divided into 30 minutes loading period and 30 minutes unloading period (retardation).

The creep apparatus (Figure (5)) was calibrated before starting creep tests and the calibration curve is as shown in figure (6).

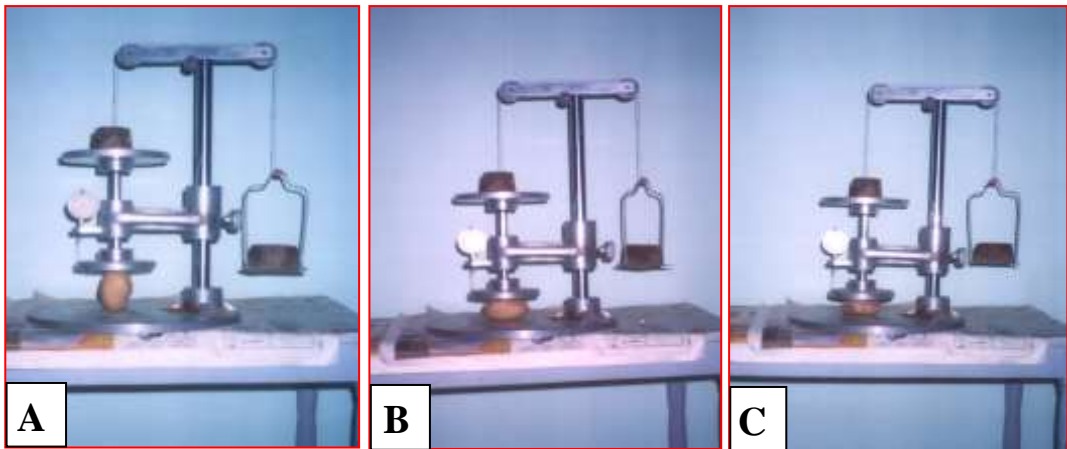


Figure (5): Creep test apparatus photos: A) *L = Longitudinal position.*
 B) *D = Radial position.* C) *T = Minimum axis position.*

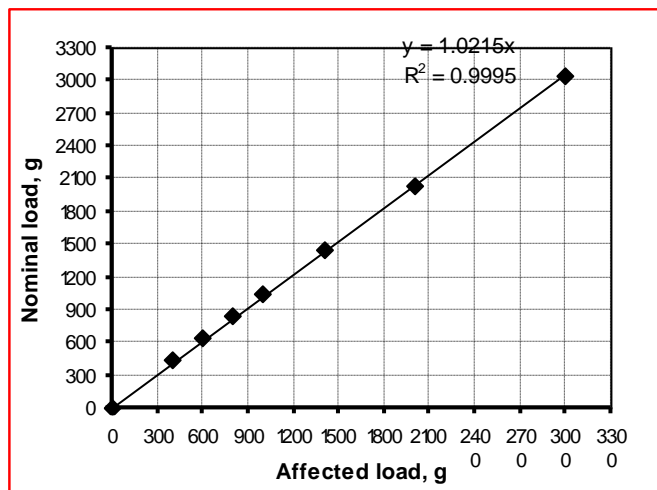


Figure (6): Calibration curve of creep test apparatuses.

The obtained data from tests of this investigation were used for plotting creep curves for calculating the constants of the rheological Burgers model (K_1 , K_2 , C_1 , C_2) as shown in figure (7) for potato tubers

.Constants of the model were calculated by using the plotted curves and the following equation of the model,

$$d(t) = F_0 \left[\frac{1}{K_1} + \frac{1}{K_2} (1 - e^{-t/T_{ret}}) + \frac{t}{C_1} \right]$$

Where:

$d(t)$ = Deformation at any time t ; mm;

F_0 = Constant force, N ;

K_1 = Instantaneous elasticity, N/mm;

K_2 = Retarded elasticity, N/mm;

C_1 = Free viscous element, N.min/mm;

C_2 = Retarded viscous element, N.min/mm; and

$T_{ret} = C_2 / K_2$ The time of retardation

The method of estimating the rheological constants of Burgers model and its behavior is as shown in the following creep and recovery curve (fig. 7)

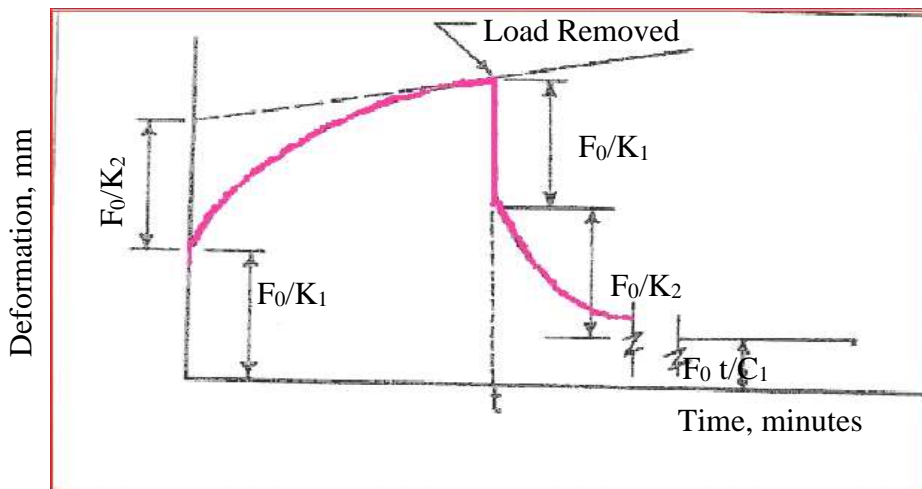


Fig. (7): Typical creep and recovery curve in a viscoelastic material exhibiting instantaneous elasticity, retarded elasticity and viscous flow.

As shown in the figure an instantaneous deformation will happen in the spring (1) due to the instantaneous fixed load F_0 and has the value F_0/K_1 .

Knowing F_0 the value of K_1 can be calculated as $K_1 = F_0/d_1$. After the initial deformation, creep continues at a higher rate but gradually slows down due to the viscous effect attained by the dashpot C_1 . The value of C_1 can be calculated by substituting the creep duration and the constant load in the flow

The retarded elasticity K_2 can be evaluated from F_0/K_2 taken from $\frac{F_0 \cdot t}{C_{11}}$ parameter

the loading portion of the curve.

The time of retardation can be estimated from the equation of Burgers model as follows

$$\text{Let } M = F_0/K_2 \frac{F_0}{K_2} \left(1 - e^{-\frac{t}{T_{ret}}} \right), \quad \text{and } N = F_0/K_2.$$

$$\text{Then } M = N \left(1 - e^{-\frac{t}{T_{ret}}} \right) / N$$

$$M/N = \left(1 - e^{-\frac{t}{T_{ret}}} \right) \quad \text{Then } (1 - M/N) = \left(e^{-\frac{t}{T_{ret}}} \right)$$

$$\text{Ln } (1 - M/N) = \frac{-t}{T_{ret}}$$

Then for various values of M at various times values of (t) , the resulted slope of the obtained linear regression will equal $1/(T_{ret}) = -K_2 / C_1$.

Knowing K_2 then C_1 can be calculated.

RESULTS AND DISCUSSIONS

180 Potato creep experiments with three replicates for each test were conducted in this investigation. Experiments included two potato varieties (Daimont and Santana), three separated static loads (10, 14 and 18 N), three loading position on potato tuber (L - longitudinal, D – radial and T – minimum axis) and two different storage system (Nawalla $16 \pm 3^\circ\text{C} - 84\%$ RH and cold store $4^\circ\text{C} - 90\%$ RH) .All experiments were achieved for fresh, cured and stored at 25, 50 and 75 days potato tubers. Figure (8) illustrates typical creep and retardation test curves for fresh Santana

potato tubers variety due to the effect of a static load (fixed stress) of 10N. The static load continued affecting the whole tuber for 30 minutes and then recovered where, the test continued for 30 minutes without loading. The curves shown in the figure demonstrate the deformation behavior of the samples due to the static load and after the load was removed with time for every tuber sample position. It is cleared from the typical creep and recovery test curve that the deformation decreases as a function of time. The mean creep data obtained from tests were analyzed by the rheological Burgers model to determine model constants (K_1 – instantaneous elasticity, N/mm); (K_2 – retarded elasticity, N/mm); (C_1 – free viscous element, N.min/mm) and (C_2 – retarded viscous element, N.min/mm).as following :

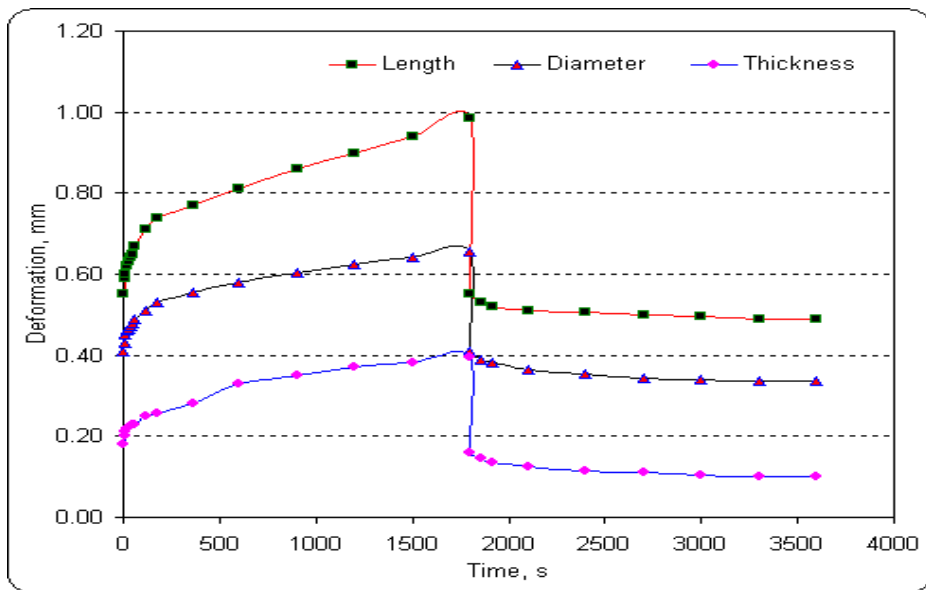


Fig. (8); typical curve of creep retardation test for fresh potato Santana variety at 10 N under room temperature.

1- Instantaneous elasticity (K_1 – N/mm)

The instantaneous elasticity (K_1) versus time expressed by its beginning for fresh tubers curing time "after 15 days" and storage time is demonstrated in figures 9, 10, 11 and 12. It is cleared from the figures that the instantaneous elasticity K_1 decreased with time especially, during curing and at the first 25 days of the storage period where the rate of

decrement decreased until the end of storage period. This can be explained by the instantaneous deformation of the tuber when subjected to a certain constant load on the specific orientation increased with time especially storage time under the two storage systems. This led to a significant reduction in K_1 . The exerted reduction was slightly higher under Nawalla storage system ($16 \pm 3^\circ\text{C}$, 84% RH) than in Cold storage system (4°C , 90% RH). As shown in the figures, differences were found in the values of K_1 when the orientations of load on the sample were considered where the narrow dimension of tuber has the bigger mean values of K_1 . Also, the fresh potatoes exhibited a straight line relationship, whereas the stored ones showed a curvilinear relationship. Another observation was that K_1 increased slightly in its magnitude with increasing the static load. Multiple regression equations were determined to describe the relationship between the instantaneous elasticity (K_1), N/mm and (ST), days; loading (F_0), N; loading position index (P_i) where $L=1$, $D=2$ and $T=3$ and potato weight (W),g. The regression analyses were conducted for the two varieties in two storage system (Cold store- 4°C and 90% RH and Nawalla store - $16 \pm 3^\circ\text{C}$ and 84% RH.).

The regression equations were as follows:

a- Cold storage system:

$$\text{Diamont } K_1 = 7.15 P_i - 0.15 ST + 0.17 F_0 + 0.2 W + 42.93 \quad R^2 = 0.82$$

$$\text{Santana } K_1 = 8.27 P_i - 0.15 ST + 0.15 F_0 + 0.03 W + 7.68 \quad R^2 = 0.86$$

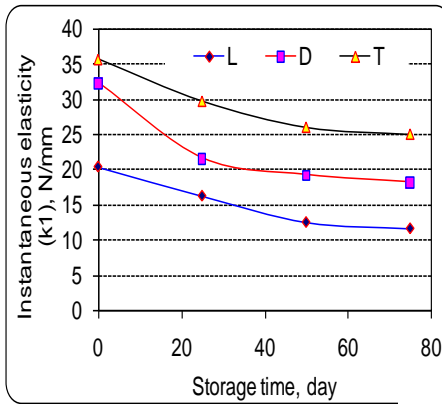
b- Nawalla storage system:

$$\text{Diamont } K_1 = 5.97 P_i - 0.23 ST + 0.43 F_0 + 0.14 W + 30.3 \quad R^2 = 0.78$$

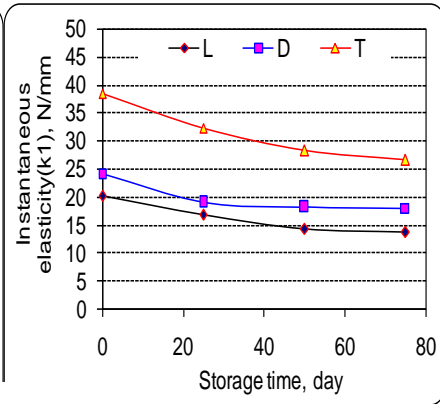
$$\text{Santana } K_1 = 8.39 P_i - 0.2 ST + 0.55 F_0 + 0.1 W - 9.86 \quad R^2 = 0.88$$

It is observed from the linear regression equations that a negative relationship was occurred between K_1 and storage time where the other factors affected positively with a satisfying values of (R^2). An example from the resulted mean values of K_1 were cleared that the decreasing rate of K_1 for Santana variety tubers under the constant load of 10N on L position was 24.59% from harvesting to the end of 15 days curing period.

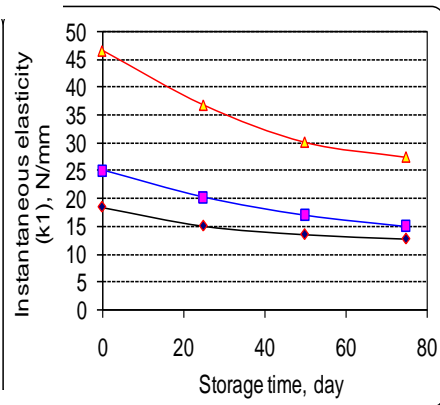
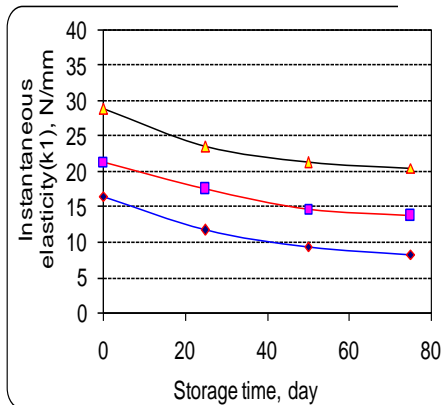
Diamont



Santana



At 10 N



At 14 N

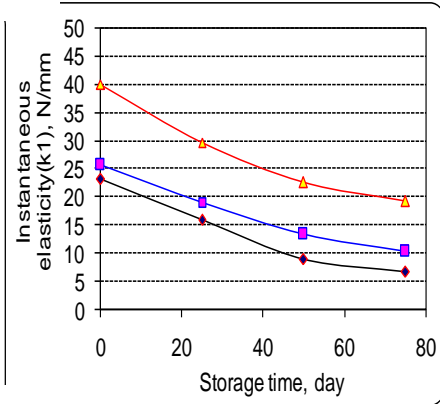
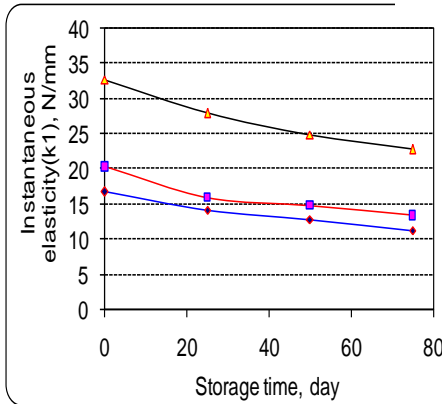


Fig. (9)

At 18 N

Fig. (10)

Fig.(9&10): Relationship between instantaneous elasticity (k_1), N/mm, for Diamont and Santana varieties during storage in Cold storage system at three loading positions (Longitudinal (L), Radial axis (D), and Minimum axis (T) for 10, 14, and 18 N of static loads

Diamont

Santana

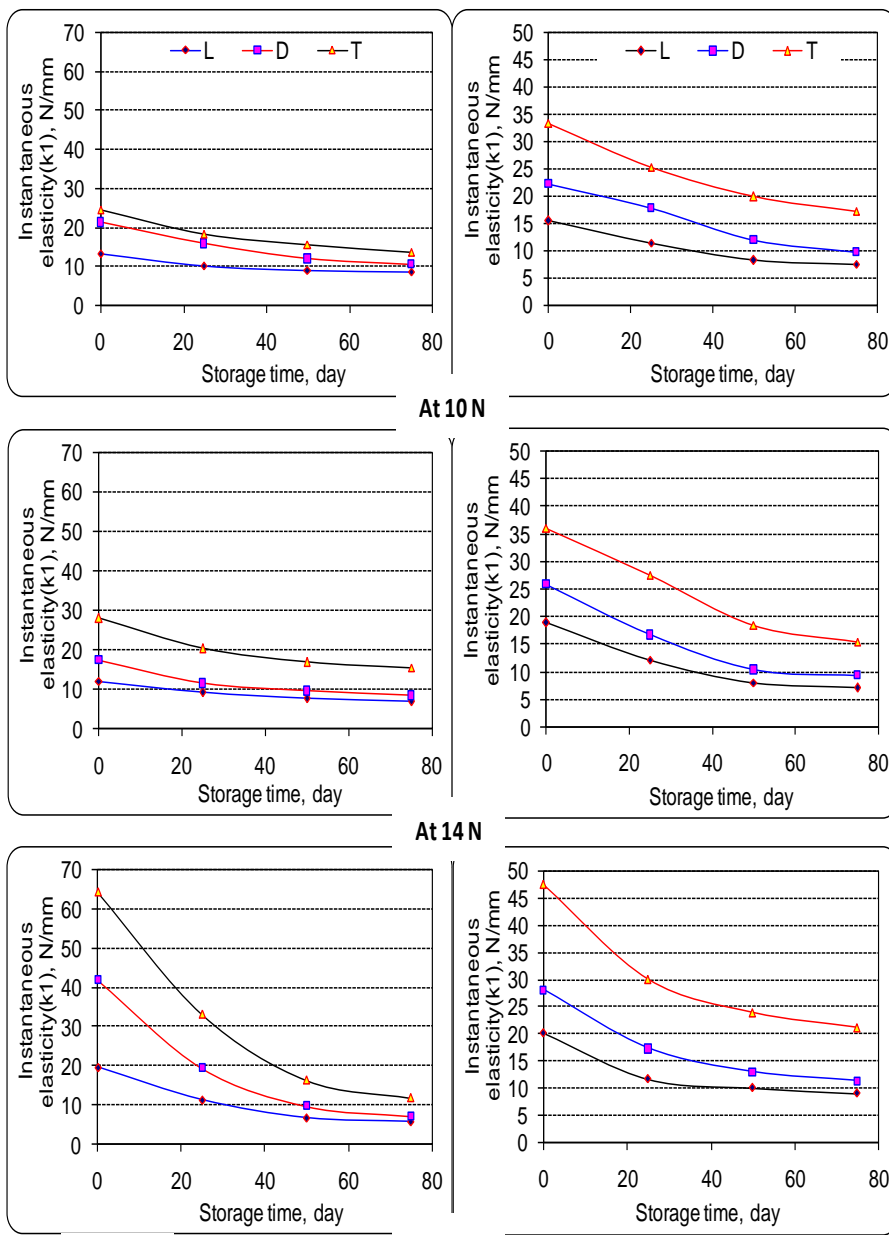


Fig. (11)

Fig. (12)

Fig.(11&12): Relationship between instantaneous elasticity (k_1), N/mm, for Diamont and Santana varieties during storage in Nawalla storage system at three loading positions (Longitudinal (L), Radial axis (D), and Minimum axis (T) for 10, 14, and 18 N of static loads

In the same time, the total decreasing rate reached the magnitude of 41.9 % and 68.35% when tubers stored in Cold and Nawalla system respectively. The collected data and represented the mean values of K1 in the same conditions showed that the decreasing rate of K1 for Diamont variety tubers was 23.48% from harvesting till the tubers cured .Mean while, the total decreasing rate reached the values of 47.15 and 60.47 when tubers stored in Cold and Nawalla storage systems respectively. The demonstrated example shows progressively decreasing trends for the rheological parameter K1 with storage time for all varieties and at the two storage systems.

2-Retarded elasticity (K₂), N/mm

The results of the mean values of the retarded elasticity (K₂) are presented in the figure 13 to 16. The results show that its magnitude decreases with increasing storage time in Nawalla and Cold storage systems for the two varieties. It is observed also that a significant reduction was happened in Nawalla storage system than in the Cold system where the storage temperature was higher. Another observation was noticed that the higher the values of the static load used the greater the values of the retarded elasticity even on the load positions of the tuber. Multiple linear regression equations were delivered to describe this significance between the storage time (ST), days – static load (F_o), N – loading position index (Pi), L=1, D=2 and T=3 – and potato weight (W). g and the retarded elasticity (K₂), N. mm for the two varieties of tubers in the two different storage systems as follows:

a- Cold storage system:

$$\begin{array}{l} \text{Diamont} \\ \text{variety} \end{array} \quad K_2 = \quad 13.3 P_i - 0.34 ST + 0.31 F_o + 0.08 W + 8.9 \quad R^2 = 0.84$$

$$\begin{array}{l} \text{Santana} \\ \text{variety} \end{array} \quad K_2 = \quad 13.7 P_i - 0.33 ST + 2.9 F_o + 0.25 W - 48.9 \quad R^2 = 0.90$$

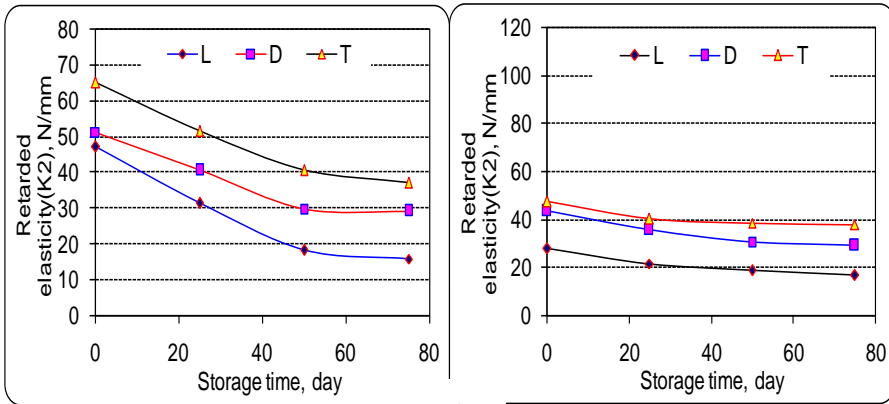
b- Nawalla storage system:

$$\begin{array}{l} \text{Diamont} \\ \text{variety} \end{array} \quad K_2 = \quad 14 P_i - 0.48 ST + 0.86 F_o + 0.2 W + 47.5 \quad R^2 = 0.92$$

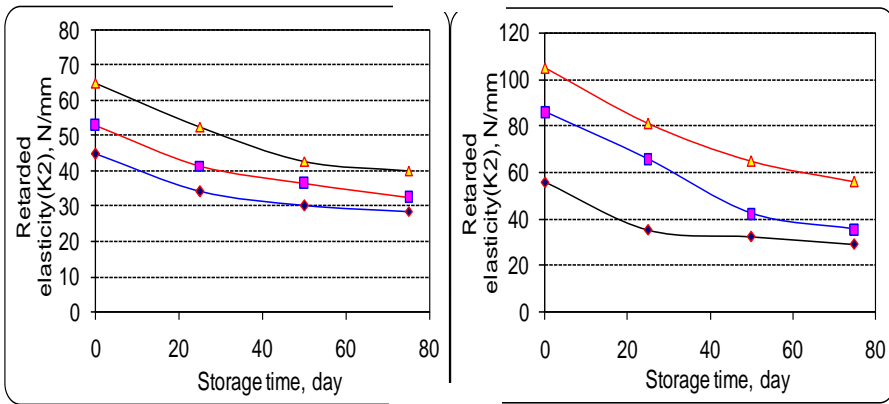
$$\begin{array}{l} \text{Santana} \\ \text{variety} \end{array} \quad K_2 = \quad 13 P_i - 0.46 ST + 0.95 F_o + 0.26 W + 51.2 \quad R^2 = 0.81$$

Diamont

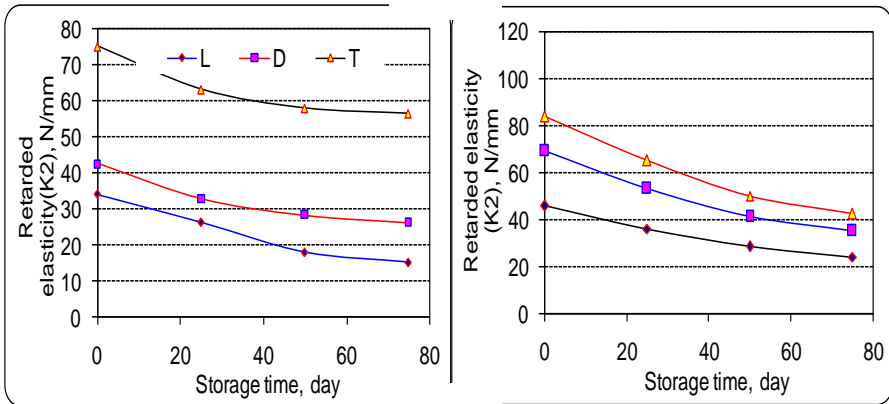
Santana



At 10 N



At 14 N



At 18 N

Fig. (13)

Fig. (14)

Figures: (13&14) : Relationship between retarded elasticity (K_2), N/mm, for Diamon and Santana t varieties during storage in cold storage system at three loading positions (Longitudinal (L), Radial axis (D), and Minimum axis (T) for 10, 14, and 18 N of static loads

Diamont

Santana

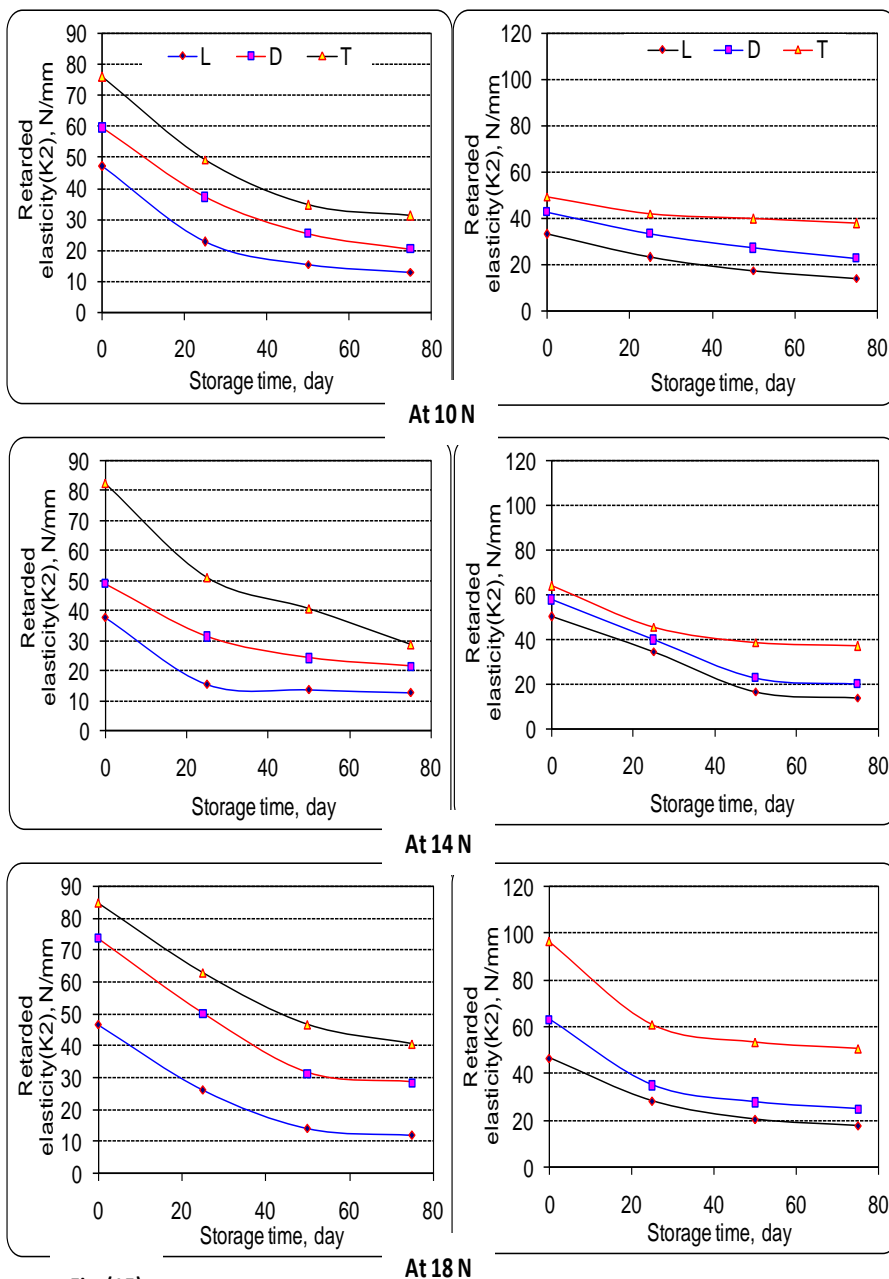


Fig. (15)

Fig. (16)

Figures: (15&16) : Relationship between Retarded elasticity (K2), N/mm, for Diamon and Santana varieties during storage in Nawalla storage system at three loading positions (Longitudinal (L), Radial axis (D), and Minimum axis (T) for 10, 14, and 18 N of static loads

The equations clarified that the storage time was inversely proportional with storage time, while the other parameters had nearly a positive effect on the retarded elasticity (K_2).

The behavior of the rheological constant (K_2) when tubers were subjected to a constant load 10N on L position appeared a reduction in its magnitude. The values of (K_2) decreased with respect to Santana and Diamont varieties by 13.72; % from harvesting to the end of the 15 days curing period. While, it decreased by (52; 599%) and (;%) as a total decrement till the end of storage time under the two storage conditions (Cold and Nawalla storage systems).

It is apparent from the analyzed experimental data that the magnitude of K_2 decreased during storage significantly as well as with the temperature of the storage condition. This can be noticed from the higher values of change percentage under storage tubers in Nawalla than Cold storage.

3-Free viscous element (C_1) N.min/mm.

Figures 17 – 20 illustrate the graphs of the mean values of C_1 v.s. storage time for Diamont and Santana varieties under the conditions of storage in both Nawalla and Cold storage systems. Each figure shows both the effect of the static fixed load and the position of its effect on the tuber .The graphs show that the free viscous element (C_1) decreases by increasing storage time for the two varieties of potato tubers stored in Nawalla and Cold store. Similarly, it decreases with all static levels of load and on the three positions of the tuber. Increasing the static load from 10 to 18N had a slight effect in the magnitude of C_1 as a positive relationship. In this regard multiple linear regression analyses were achieved to yield functional equations. These equations expressed the relationship between the free viscous element (C_1),N.min/mm versus storage time (ST),days; static load (F_0) N; position of load effect (index P_i) where $L=1$, $D = 2$ and $T= 3$ and potato weight (W) g. The effect of the above mentioned parameters, involved in the equations, on C_1 under the experimental conditions was analyzed for the potato varieties when stored in Nawalla ($16 \pm 3^\circ\text{C}$,.84% RH) and Cold store (4°C , 90% RH). The equations which provided the best fitting of data are:

a- Cold storage system:

$$\begin{array}{l} \text{Diamont} \\ \text{variety} \end{array} \quad C_1 = 335.2 P_i - 10.2 ST - 21.5 F_o - 3.4 W + 1439 \quad R^2 = 0.86$$

$$\begin{array}{l} \text{Santana} \\ \text{variety} \end{array} \quad C_1 = 398.3 P_i - 8.9 ST - 4.9 F_o - 3.96 W - 121.7 \quad R^2 = 0.83$$

b- Nawalla storage system:

$$\begin{array}{l} \text{Diamont} \\ \text{variety} \end{array} \quad C_1 = 345.7 P_i - 12.2 ST - 2.2 F_o - 4.9 W + 1343 \quad R^2 = 0.85$$

$$\begin{array}{l} \text{Santana} \\ \text{variety} \end{array} \quad C_1 = 422.1 P_i - 12 ST - 35 F_o - 15.2 W + 2942 \quad R^2 = 0.89$$

It can be concluded from the graphs and equations that (C_1) is inversely proportional with storage time while it has a positive relationship with tuber weight. As for the dimensions it is appear that the greater the physical dimension, the lower magnitude of (C_1) N.min/mm even during storage time. It is clear also that a slight increasing in C_1 was found due to increasing the static load (fixed load). It is apparent from the curves that the mean values of the retarded viscous element (C_1) decreased sharply during the first 25 days while, small decreasing rate was noticed after till the end of storage time in the two storage systems. According to exposure of L dimension of the tuber by 10N static load for the two varieties Santana and Diamont in the two storage systems Cold and Nawalla respectively the mean value of C_1 for fresh tubers was 949.06 and 1066.1N.min/mm It decreased by (29.27%; 19.12%) from harvesting to the end of 15 days curing period. The total percentage of decrement was 60.67%; 62.48% and 72.51; 74.07%.

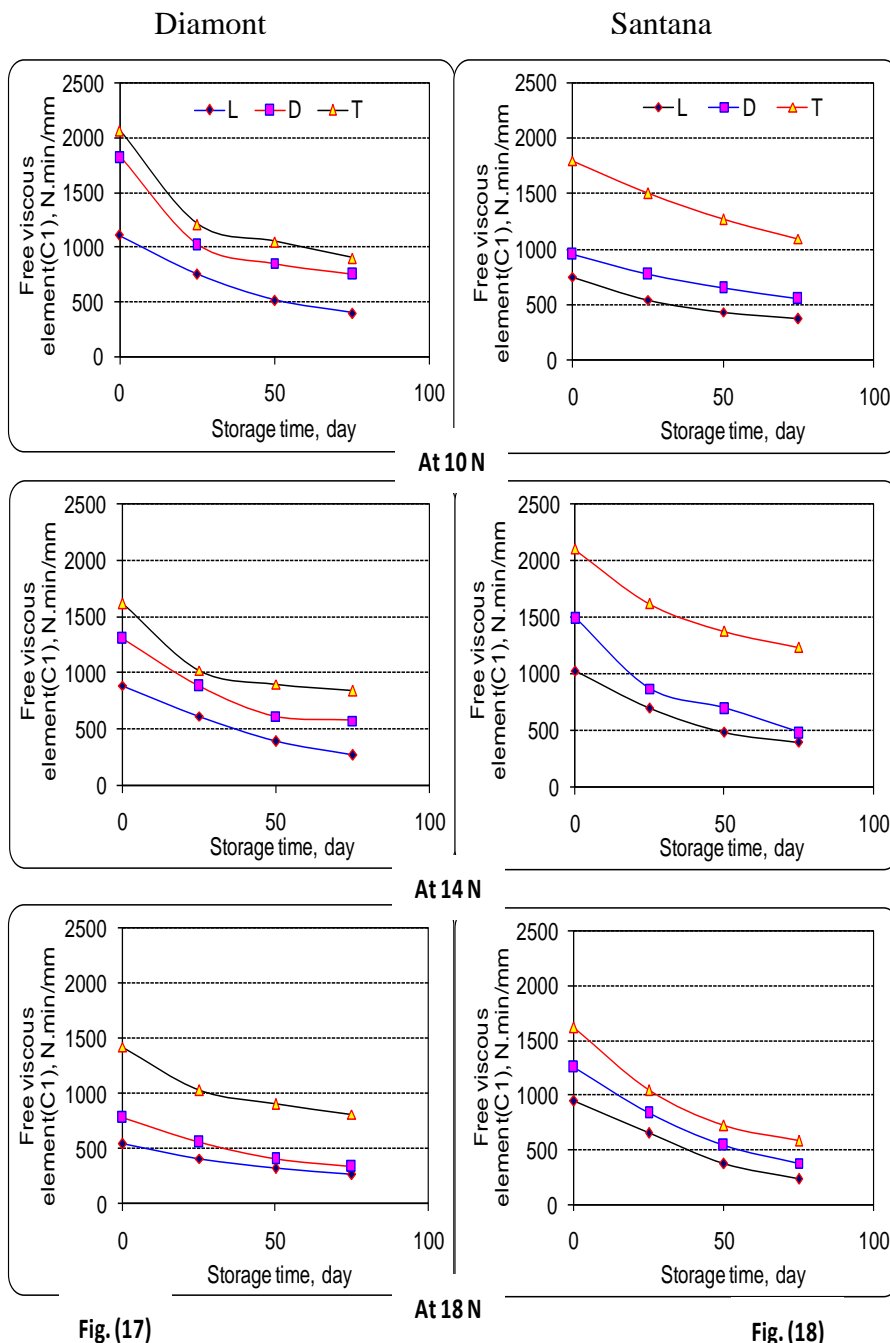


Fig. (17)

Fig. (18)

Figures(17&18) Relationship between free viscous element(C1), N.min/mm, for Diamon and Santana varieties during storage in Cold storage system at three loading positions (Longitudinal (L), Radial axis (D), and Minimum axis (T) for 10, 14, and 18 N of static loads

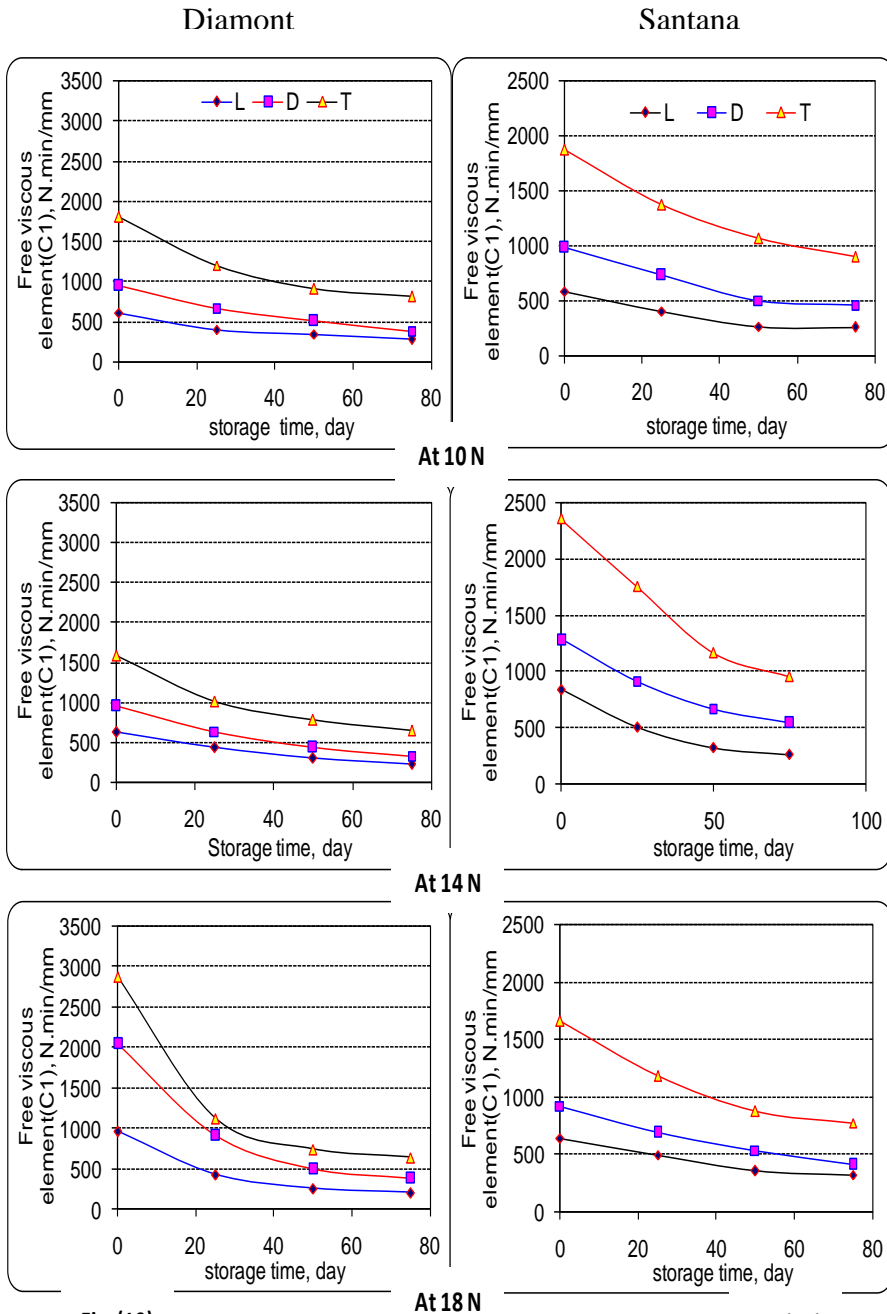


Fig. (19)

Fig. (20)

Figures: (19&20): Relationship between free viscous element(C1), N.min/mm, for Diamon and Santana varieties during storage in Nawalla storae system at three loading positions (Longitudinal (L), Radial axis (D), and Minimum axis (T) for 10, 14, and 18 N of static loads

4-Retarded viscous element (C₂) N.min/mm.

Figures 21 to 24 show (C₂) – storage time relation at various fixed loads on the three positions of the tuber for Diamont and Santana varieties stored in Cold and Nawalla storage systems. Firstly, it is cleared that retarded viscous element (C₂) decreased with increasing storage time through the storage period in Cold and Nawalla storage conditions. The Cold system was at 4°C and 90% RH, where the storage conditions in Nawalla were at 16 ± 3°C and 84% RH. This reduction in C₂ and even K₂ was most probably due to the degradation of pectin substances, which make up 52% of potato cell wall, and are responsible for the bending of cells (Alvarez et al., 2000; and Scanlon et al., 1996). A positive relation was found from the figures between C₂ and static load. Also the mean values of C₂ for Santana variety which characterized by the big weight and volume were found higher than in Diamont variety.

Statistical equations based on multiple linear regression analysis were determined using the obtained data for the calculated values of C₂ affected by storage time (ST), (days), tuber weight, (g), static load, F (N) and loading position index, Pi (L=1, D=2, and T=3) for the two potato varieties (Diamont and Santana) stored at two different storage conditions. The equations delivered were as follows:

a-Cold storage system:

$$\text{Diamont } C_2 = 399.4 P_i - 10.1 ST + 9.2 F_o + 2.4 W + 267.4 \quad R^2 = 0.84$$

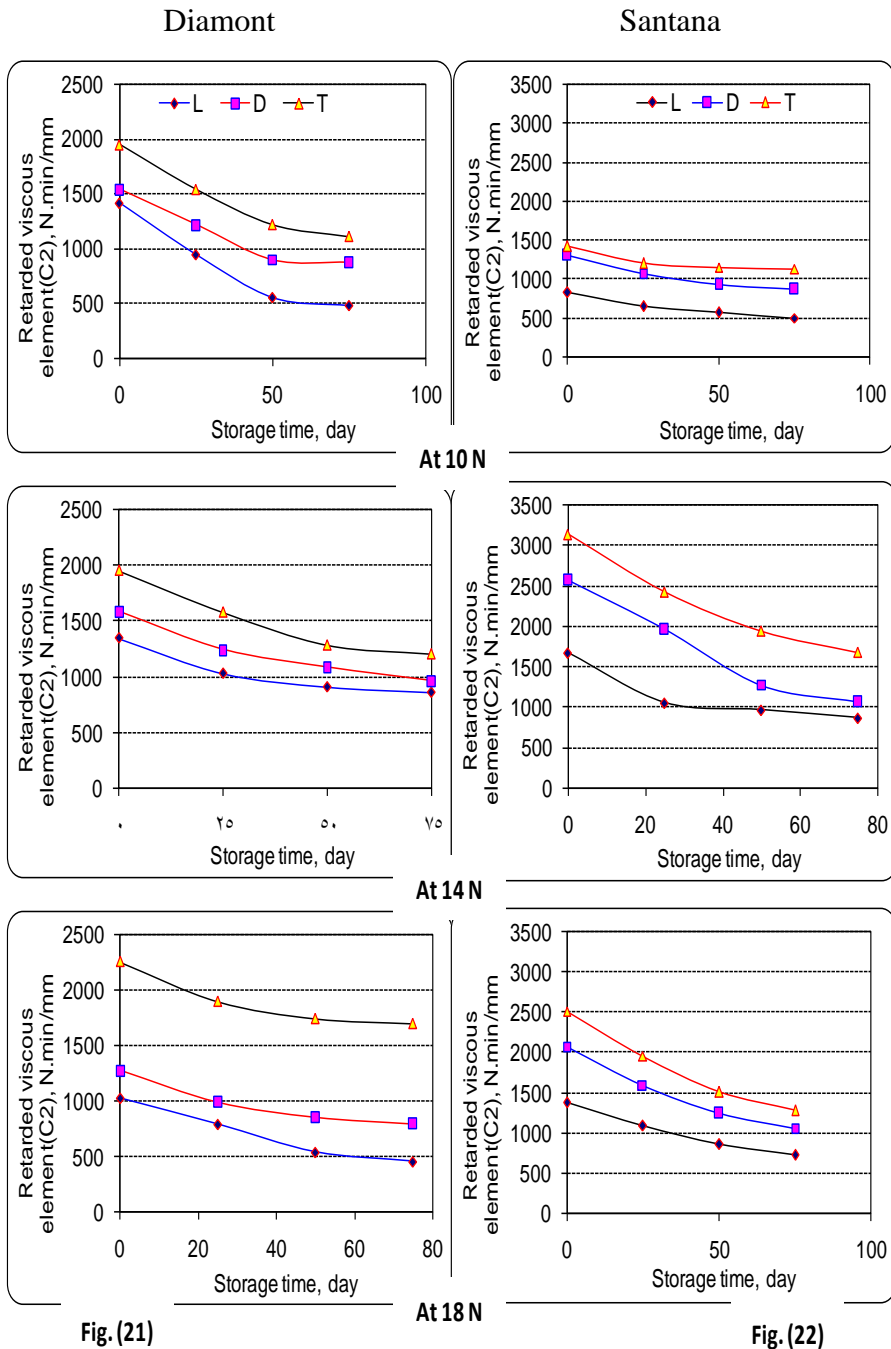
$$\text{Santana } C_2 = 409.8 P_i - 9.8 ST + 85.7 F_o + 7.5 W - 14663 \quad R^2 = 0.90$$

b- Nawall storage system:

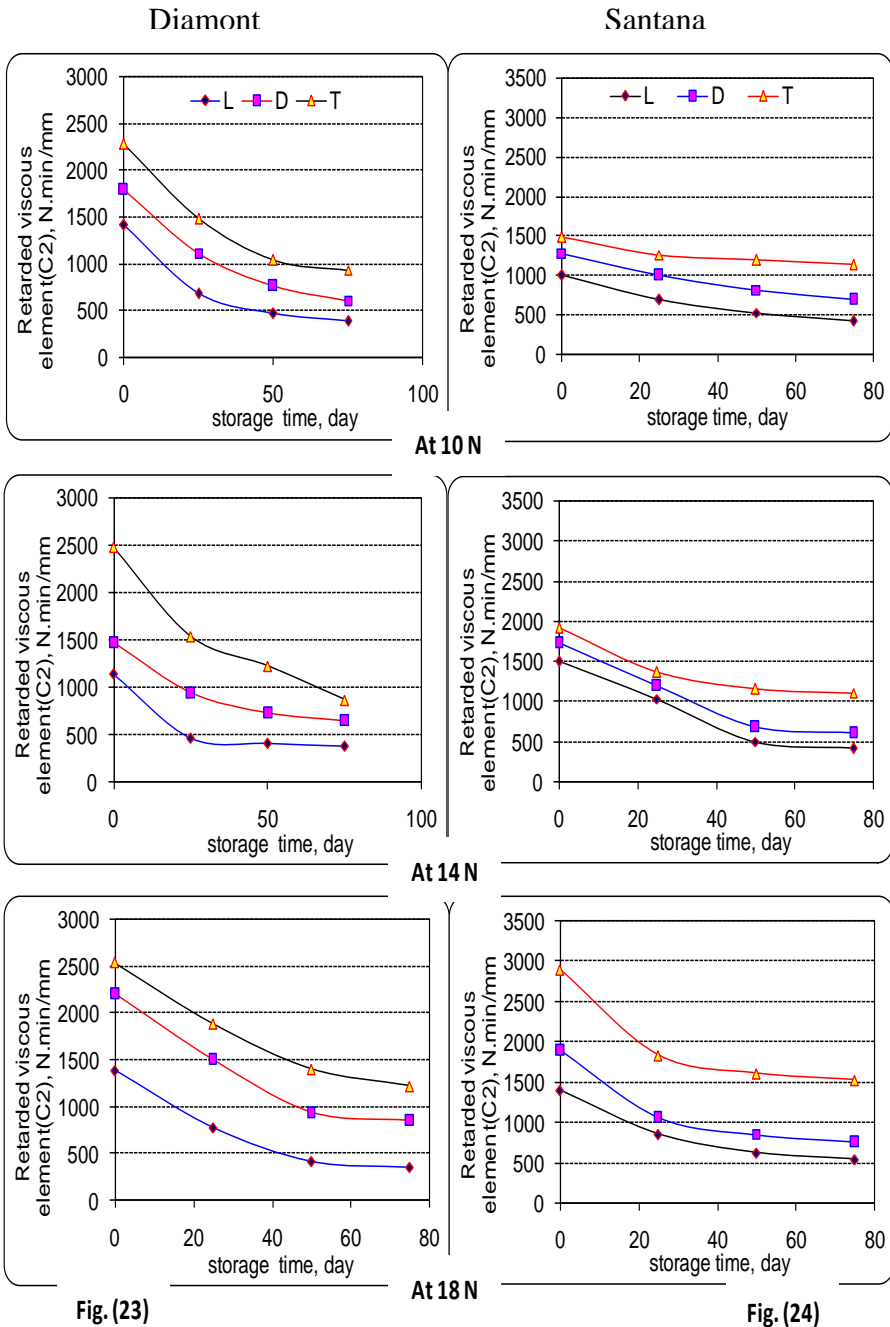
$$\text{Diamont } C_2 = 421 P_i - 14.3 ST + 25.7 F_o + 5.8 W + 1426 \quad R^2 = 0.92$$

$$\text{Santana } C_2 = 391 P_i - 13.9 ST + 28.5 F_o + 7.9 W + 1536 \quad R^2 = 0.81$$

A decreasing relation was clarified by the equations for C₂ as affected by storage time. The tubers weight was directly proportional with C₂. In the same time, a positive relationship characterized the effect of static load on respect to loading tubers with a static load of 10 N on L position appeared



Figures: (21&22): Relationship between free viscous element(C_2), N.min/mm, for Diamon and Santana varieties during storage in cold storage system at three loading positions (Longitudinal (L), Radial axis (D), and Minimum axis (T) for 10, 14, and 18 N of static loads



Figures: (23&24): Relationship between free viscous element(C_2), N.min/mm, for Diamon and Santana varieties during storage in Nawalla storage system at three loading positions (Longitudinal (L), Radial axis (D), and Minimum axis (T) for 10, 14, and 18 N of static loads

C_2 .In the same direction, the mean values of data obtained for C_2 with that C_2 for fresh tubers was 1057.53 and 1532.44 N.min/mm for Santana and Daiamont varieties. After curing its value reached 912.45 and 1414.56 N.min/mm .It reduced by 52.58, 59.97 and 68.95, 74.58 % when tubers of the two varieties were stored 75 days in both Cold and Nawalla storage systems.

CONCLUSION

The rheological model constants determined in this study cleared the following observations:

The constants decreased significantly with storage time.

The constants appeared a positive relation with potato tuber weight.

The constants had a slight positive effect with increasing the static fixed load.

Concerning temperature, the mean values of the rheological model constants were higher in magnitude when storing tubers in Nawalla storage system, 16 $^{\circ}$ C; 85 %RH, where the higher storage temperature than in Cold storage system, 4 $^{\circ}$ C; 90 % RH, where the lower storage temperature. It was observed from the creep and retardation test for potato tubers that, the instantaneous deformation of the tested potato tubers when subjected to the constant load increased with time and also with storage time under all storage conditions in the investigation. When the tuber unloaded, the deflection happened due to the effect of the static load divided to two portions .One is not recoverable due to the fluid which has moved out of the cells .The other is recoverable which is probably due to the elasticity of the cell walls of the tuber .This observation was also noticed and described by Finny and Hall, 1967.

REFERENCES

- Abdelmaksoud,M.A.,1992.Rheological properties of tomatoes and their dependence on maturity.M.Sc.thesis Ag.Eng.Dept;Fac.of Ag.,Alexandria Univ.
- Alvarez, M.D., Saunders, D.E., and Vineent, J.F. (2000). Effect of turgor on the cutting energy of rtored potatoes. European Food Research Technology, 210,331-339.

- Chang,C.S.and C.R Martin,1983. Rheological properties of grain dust ,Trans. Of the ASAE.1249:1256.
- Clevenger, J.J. and D.D. Haman, 1968. The behavior of apple skin under tensile loading. Trans of The ASAE 11(1):34 – 37.
- Faborode,M.O.and J.R..O Calla ghan (1989). A rheological model for the compaction of fibrous agricultural material J.agric.Engn.Res.42: 165 – 178.
- Finney,F.E. and CW. Hall, 1967. Elastic properties of potatoes. TRANSACTIONS of ASAE : 10(1):4-8.
- Mohsenin, N.N.1970. Physical properties of plant and animal materials .Vol. 1.Gorden And Breach Science Publishers. New York.
- Mohsenin, N.N.1978.
- Pitt,R,E. and Chen,H.L.(1983). Time – dependent aspects of strength and rheological of vegetative tissue Trans. Of the ASAE 26(5):1275 – 1280.
- Sabbah,M.A.; Soliman S.N. and M.A.Abdelmaksoud,1994.Creep properties of tomatoes and their dependence on maturity.Mist,J.Ag.Eng,11(1).
- Scanlon, M.G., Pang, C.H., and Billaderis, C.G.(1996). The effect of osmotic adjustment on the mechanical, properties of potato parenchyma. Food Research International 29,481-488.

الملخص العربي

الثوابت الريولوجية لنموزج بيرجرز ذو الأربعة عناصر لدنرات البطاطس

المتأثرة بأحمال ثابتة ومختلفة تحت ظروف تخزين مختلفة

* د. محمد عبد الفتاح عبد المقصود * د. جمال رشاد جامع ** م. عبد الجواد محمد عبد الجواد

تم في هذا البحث دراسة النموزج الريولوجي لدنرات البطاطس صنفى دايمنت و سلتنا وذلك باستخدام اختبار الزحف و الاسترجاع و قد استخدم نموزج بيرجرز ذو الأربعة عناصر لتطيل نتائج الدراسة و إيجاد ثوابت النموزج خلال مراحل التدول للدنرات (طازجة- معالجة- مخزنة على ثلاث قترات كل ٢٥ يوم داخل نظلمى التبريد) وذلك عند ثلاثة مستويات تحميل مختلفة وثابتة على الثلاث أبعاد الأساسية للدنرة لزوم اختبار الزحف و الاسترجاع و الذي يعبر عن سلوك حصص المرونة و اللزوجة للدنرات تحت تأثير الاجهاد الثابت ..
بذلك اشتملت الدراسة على الأتى :

- ١- ثلاث مستويات للحمل الثابت (١٠ - ١٨١٤ نيوتن).
- ٢- ثلاث اوضاع اساسية لتأثير الحمل الثابت على الدنرة (الطول- العرض- السمك).
- ٣- صنفن من الدنرات وهى دايمنت و سلتنا.
- ٤- نظلمين لتخزين دنرات البطاطس : التخزين في التلاجة (٤ درجات مئوية ٩٠ % رطوبة نسبية) ، التخزين في النواله (١٦±٣ درجات مئوية ٨٤ % رطوبة نسبية).
- ٥- اجريت التحارب على ٥ مراحل للدنرة (طازجة- معالجة لفترة ١٥ يوما- بعد ٢٥ يوم تخزين- بعد ٥٠ يوما تخزين- بعد ٧٥ يوما تخزين).
- ٦- ٣ مكررات

اجريت جميع اختبارات الزحف و عددها ٥٤٠ تجربة خلال ٦٠ دقيقة قسمت الي ٣٠ دقيقة تحميل و ٣٠ دقيقة اخرى استرجاع للتجربة الواحدة حيث قد تم تصنيع وحدة لقياس اختبارات الزحف و معيبرتها لتقدير الفقد في القوة باإحتكاك وقد تم إيجاد جميع القيم المتوسطة للثوابت الريولوجية للنموزج في جميع مراحل الدنرة الخمسة وكذلك قد تم رسم العلاقات بين زمن التخزين وتأثيره على القيم المتوسطة لهذة الثوابت .
وقد تم ايضا إيجاد علاقات الإبحار الخطى المتعدد بين القيم المتوسطة لهذة الثوابت الريولوجية و كل من زمن التخزين با لأيام - قيمة الأحمال الثابتة المختلفة بالنيوتن - الأوضاع المختلفة لتأثير الحمل على الدنرة وكذلك وزن الدنرة بالجرام .
وقد تم التوصل الي النتائج و الملاحظات التالية:

- ١- إزداد التمدد اللحظى للدنرات المختبرة عند تعرضها للأحمال الثابتة لمختلفة مع زمن التخزين تحت ظروف التخزين في كل من التلاجة و النواله .
- ٢- عند إزالة الحمل الثابت انقسم الإبتعاج الحلت في الدنرة الى جزئين رئيسيين الأول تم ازالته وقد يرجع ذلك الي مرونة جدار الخلية للدنرة و الثاني لم يزال نتيجة لخروج السائل من الخلايا للدنرة. وقد ايد ذلك العلمن Hall و Finney سنة ١٩٦٧ .
- ٣- قلت الثوابت الريولوجية مع زمن التخزين وخاصة في الأيام الأولى من التخزين و بعد فترة المعالجة .
- ٤- أظهرت الثوابت الريولوجية علاقة موجبة مع وزن الدنرات .
- ٥- إزدادت الثوابت الريولوجية زلزلة طفيفة مع زيادة الحمل الثابت على أوضاع الدنرة الثلاث .
- ٦- إزدادت القيم المتوسطة للثوابت الريولوجية في النواله عنها في التلاجة .

* أستاذ مساعد الهندسة الزراعية قسم الهندسة الزراعية- كلية الزراعة- جامعة المنوفية.

** مهندس بمعهد بحوث الهندسة الزراعية- القاهرة