STATIC BEHAVIOUR OF DIFFERENT TYPES OF R.C BEAM-COLUMN CONNECTIONS AS AFFECTED BY BOTH VALUE ACTING LATERAL HORIZONTAL FORCEAND GRADE OF USED CONCRETE (THEORETICAL STUDY) Part Two

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ABSTRACT

This paper describes a theoretical study of forty eight (48) Reinforced Concrete RC beam column joints, which generally classified as interior, exterior and corner joints. The most main parameters, which may influence the behavior of beam-column joint, transverse reinforcement, lateral shear reinforcement, longitudinal reinforcement, joint area, column axial load, concrete compressive strength, end boundary conditions ...etc. In this research FEA (finite element analysis) using ABAQUS\CAE commercial software will be developed to build a detailed model to predict the nonlinear behavior of beam-column joint under seismic loadings. The ABAQUS\CAE 6.7 solution is a practical way to implement the nonlinear dynamic earthquake analysis for the finite element model. Our study is focusing with joints where statically lateral load was applied and gradually increased maintaining constant axial load at the top of the column equal to 0.15 (A_cF_c). Several linear variable horizontal displacement transducers were mounted , the net story drift, bond stress, axial shear stresses and strains as well as energy absorption for using different grades of concrete C250, C400, C600 and C1200 are evaluated and discussed to illustrate the behaviour of the studied joints under the case study of loadings.

Keywords: RC Beam-Column Connections, Concrete Compressive Strength, Lateral Load, Shear and Bond Strength, Joint Deformation, Energy Absorption, Mode of Failure, and ABAQUS\CAE.

1. Introduction

There are several parameters, which may influence the behavior of beam-column joint. Among of these parameters are the followings:

- 1. <u>Type of joint</u>: which is mainly referred as interior joint, exterior joints or corner joints.
- 2. <u>Transverse Reinforcement</u>, an increase of joint transverse reinforcement causes an increase of joint shear stiffness. Because the capacity of both diagonal concrete strut and truss mechanisms is dependent on concrete compressive strength (Jaehong K. et al. 2008). Also(Ahmed H. 2003) summarized that the increase in transverse reinforcement above certain amount had a little effect on the ultimate strength of the joint and the transverse reinforcement in the joint is more effective in maintaining the strength than the stiffness.
- 3. <u>Lateral Shear Reinforcem</u>ent, The amount of joint lateral reinforcement has a significant effect on both strangled deformation capacity of the joints (**Kazuhiro K.** (1991).

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Civil Engineering Department, Faculty of Engineering, Assiut University

- 4. <u>Longitudinal Reinforcement</u>, **Hitoshi S.et al.**, (2002) studied the resultants in longitudinal bar do not exceeds the yield strength of the reinforcement, and the bars contributed only on the axial load carrying capacity .
- 5. Joint Area, S. R. Uma et al., (2006) study proved that the effective, joint area A_j is the area resisting the shear within the joint and is contributed by the framing members in the considered direction of loading.
- 6. <u>Column Axial Load</u> **Kumar et al., (2002)** found that the joint rotation and the axial load in the column increase the ductility and energy dissipation capacity and reduced the joint region damage.
- 7. <u>Concrete Compressive Strength</u>, Jaehong K. et al., (2008); summarized that concrete compressive strength is the most important parameter in determining RC joint shear, (Laura N. Lowes et al. 2004); indicated that concrete compressive strength is substantially less than that observed under monotonic loading and that concrete tensile strength deteriorates more rapidly as a function of tensile strain.
- 8. <u>Miscellaneous factors</u>: including lateral loads ratios of columns connected beams dimensions , boundary conditionsetc. , which are not available for the authors.
- 9. The following is a brief for the available main items and concept concerning and defining the characteristic of the behaviour of R.C joints:
- 10. Shear Strength, Codes Recommendations for Joint Shear Strength:

1. ACI 352R-95 and ACI 318-02

For modern RC beam-column connections, American Concrete Institute (maintaining proper confinement within a joint panel), has defined a nominal joint shear strength; that is: as Eq. (1).

$$V_{\rm n} = \gamma_{\rm ACI} \sqrt{f_{\rm c}} \mathbf{b}_{\rm j} \mathbf{h}_{\rm c} \tag{1}$$

747

Where: (γ_{ACI}) is the joint shear strength factor, f_c is the specified concrete compressive strength, (b_j) is the effective joint shear width, and (h_c) is the column depth.

2. <u>ECCS 203 (2001)</u>

Egyptian code for concrete structure sets the nominal shear strength of the joint (τ_J) as a function of concrete strength only, (A_j) is the effective joint area, (f_c) ; the cylinder compressive strength of concrete is given as Eq. (2);

$$\tau_{\rm j} = 0.96 A_{\rm j} \sqrt{f_{\rm c}} \tag{2}$$

3. <u>AIJ 1997</u>

Architectural Institute of Japan "Design guidelines for earthquake resistant reinforced concrete building based on ultimate strength concept and commentary" has recommended a nominal joint shear strength in the form of Eq. (3); that is:

$$\mathbf{V}_{\mathbf{j}} = \mathbf{k} \phi f_{\mathbf{j}} \mathbf{b}_{\mathbf{j}} \mathbf{D}_{\mathbf{j}} \tag{3}$$

where, k is the factor dependent on the shape of in-plane geometry (=1.0 for interior connections, =0.7 for both exterior connection, T-shape top story joints and =0.4 for corner knee connections); (ϕ) is the factor for the effect of out-of-plane geometry (1.0 for joints with transverse beams on both sides and 0.85 for other types of joints); (f_j) is the standard value of the joint shear strength (as a function of concrete compressive strength); (b_j) is the effective joint shear width; and (D_j) is the effective column depth.

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

The standard value of the joint shear strength (f_j) is suggested as given by equation (4); that is:

$$f_{\rm j} = 0.8 \times (f'_{\rm c})^{0.7} \tag{4}$$

4. <u>NZS 3101: 1995</u>

Standards New Zealand (Concrete Structures Standard) has suggested the design joint shear strength as Eq. (5) that is:

$$V_j = v_j b_j h_c \tag{5}$$

where (v_j) is the joint shear stress, (b_j) is the effective joint shear width, and (h_c) is the column depth. Joint shear stress is defined as Eq. (6) that is:

$$V_{j} = \frac{f_{c}}{6 \alpha} \frac{f_{jy} A_{jh}}{f_{by} A_{s}^{*}}$$
(6)

In Eq. (6) (α): is the parameter considering column axial load; (f_{jy}) is the yield stress of horizontal joint transverse reinforcement; (A_{jh}) is the total cross-sectional area of horizontal joint transverse reinforcement; (f_{by}) is the yield stress of longitudinal beam reinforcement; and (A_s^*) is the greater of the area of top or bottom beam reinforcement

passing through the joint (excluding bars in an effective tension flange).

5. <u>EN 1998–1:2003</u>

Euro code has limited the nominal shear stress, (v_{jh}) within interior beam column joint to be less than the stress value given by the Eq. (7).

$$V_{\rm jh} \le \eta f_{\rm cd} \sqrt{1 - \frac{V_{\rm d}}{\eta}} \tag{7}$$

where $\eta = 0.6 \left(1 - \frac{f_c}{250} \right)$ enotes the reduction factor on concrete compressive strength due to tensile strains in transverse direction.

6. <u>AIJ Guidelines</u> derived from Japanese database of the tests of beam-column joint without transverse beams. They are given by the equations,

$$\tau_{ju} = 1.56 \times \sigma_B^{0.712}$$
 for interior beam-column joint (8)

$$\tau_{iu} = 1.1 \Im \sigma_B^{0.718}$$
 for exterior beam-column joint (9)

where, (τ_{ju}) is joint shear strength and (σ_B) is concrete compressive strength.

7. <u>Bond Strength</u>:

A maximum bond stress Bu of beam reinforcement over the column width was estimated by assuming simultaneous yielding of the beam reinforcement in tension and compression at the two faces of the joint. Bond-strength values, required to complete calibration of the model, are defined on the basis of experimental data provided by a number of different researchers. The results of previous research indicate that bond strength is a function of the material state of the anchored bar as well as of the concrete and transverse reinforcing steel in the vicinity of the reinforcing bar (Lowes, L. 2002). Bond strength is relatively high if reinforcement is anchored in a reinforced concrete zone that carries compression perpendicular to the bar axis, and relatively low if the reinforced concrete carries tension (Eligehausen, et al., 1993). Further, bond strength

is reduced for reinforcement carrying stress in excess of the tensile yield strength and increased for reinforcement carrying compressive stress less than the compressive yield strength (Shima et al., 1997). The bond strength was assumed proportional to the square root of the concrete compressive. Laura, N. (1992).

749

- 8. <u>Flexure Strength</u>, Deformation as shear deformation of the beam-column connection increases, while the remaining shear-resisting capacity of the connection is reserved (**Hitoshi Sh. 2004**).
- 9. <u>Energy Absorption</u> and Effect of End Boundary Conditions the sub assemblages were tested by (**John S. et al., 2001**) within a reaction frame with loading and boundary conditions Pin connections were attached to the sub assemblages at approximate locations of points of contra flexure under lateral loading.
- 10. <u>Failure Modes</u>, There are Three Failure Modes for Beam-Column Joints: A) The new behavior model for shear failure of an interior beam-column joint is illustrated by (Hitoshi Sh. 2004) B) The analytical deformed shape and cracking pattern of specimen JL are compared with the experimental results by (Teeraphot Su. et al., 2008). The FEM demonstrates an extensive deformation at the ends of beam framing into the joints, indicating a flexural failure, C) Beam bending failure with a ductile load-deflection behavior model well illustrated by (Josef H., et al., 2003) The ultimate bending moment capacity of the beam is reached and the beam reinforcement is yielding, and joint failure in which the ultimate bending moment capacity of the beam crack is observed inside the joint. D) Extensive cracking within the joint core region can be found in the early stages, and the cracks open widely is the horizontal displacement increases (Bing Li, et al., 2003).

To investigate and compare the behaviors of the joints of the following detailed dimensions and end conditions e (48)joint, the normal-strength and high-strength joints are both representative of an interior, exterior and corner joint are chosen. Different lateral loads were applied maintaining constant axial load at the top of the column equal to $0.15(A_cF_c)$, to measure and evaluated the net story drift, shear deformations, axial, shear stresses, bond stress , and total absorbed energy for such joints having different grades of concrete C250,C400,C600 and C1200.

2. Details of R.C joints

Table1 and Fig.1 include the connection between the main beam, column, slab. (48) Joints , which taken into account.

Beam sizes for all joints of $(b_b \times d_b)$ mm (250 mm wide by 300 mm deep) mm as well as column sizes of $(b_c \times d_c)$ mm (300×300 mm), were kept constant.

The total height of the columns was the same for both specimens at H=2.0 m, which gave L/2=1.5 m above and below the beam. The floor slabs for both specimens were of equal sizes, with a thickness of 120 mm. The boundary conditions, beam ends were supported by horizontal rollers, while the bottom of the column was supported by a constant mechanical hinge too.

750 L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

All the specimens were cast in concrete of specified characteristic cube strength (f_c), of 250–400–600 and 1200 kg/cm², with yield stress for reinforcing bar (f_y) 2400–2800–3600 and 4000 kg/cm² respectively.

The reinforcement details of all the specimens were identical in Figures 1.a for interior joint, 1.b for exterior joint and 1.c for corner joint, apart from the joints. The beam was equally reinforced at the top and bottom by four high-yield deformed bars of 16 mm diameter (A_{bs}) (i.e. $4\Phi 16$, $4\Phi 16$).

Stirrups bent(ρ_w) from 6-mm-diameter mild steel round bars with specified characteristic yield strength of 2400 kg/cm² were provided at 80 mm centers (i.e. $\Phi 6@80$ stirrups). The column contained (A_{cs}) 12 Φ 16 longitudinal reinforcing bars evenly distributed around the perimeter. The transverse reinforcement in the column comprised $\Phi 6$ square hoops and R6 cross ties in two perpendicular directions at 80 mm centers, as shown in Table 1.

3. Mesh arrangement

The mesh module allows generate meshes Figures 2.a. you to at 2.b, 2.c, on assemblies created with ABAQUS\CAE various levels of automation and control are available so that you can create a mesh that meets the needs of your analysis. Mesh refinement is required. When severely nonlinear material Models are used, however, increasing the number of element can increasing constrains within the model. These reduce shear deformation that can lead to an overlay stiff load deflection response

(Abaqus. 2000).

4. Boundary conditions and applied loading

The loading set up is shown in Figures 3.a, 3.b, 3.c for interior and exterior and knee joint. The specimens were supported in vertical position. The top of the column was loaded by two actuators in vertical and horizontal directions. The beam ends were supported by horizontal rollers, while the bottom of the column was supported by a mechanical hinge. The distance between two loading points for beams and columns were 3,000mm and 2,000 mm respectively. With different lateral load was applied maintaining constant axial load at the top of the column equal to 0.15 AcFc. The lateral load applied was gradually increased. Several linear variable displacement transducers were mounted on the test specimens to measure the net story drift, bond stress, shear deformations, axial, shear stresses strains, and energy absorption.

The modifications were based on nonlinearity analytically model carried out by (**Sam Lee 2008**) The degradation factors for compression (dc) and tension (dt) are dependent on the plastic strain (ABAQUS, v6.5).

The nonlinearity of the structure includes geometry nonlinearity, material nonlinearity and a combination of both.

5. Geometry nonlinearity

Geometry nonlinearity can be modeled accurately by using of the Green strain formula. The P- \Box effects and large deflection effects are automatically taken into account. Most general finite element analysis packages have this built-in function available

Table 1.

Properties of Joints.

Type of beam-column joints			
	Interior joint	Exterior joint	Corner joints
(a) Beam ($b_b \times d_b$) mm	(250×300)	(250×300)	(250×300)
Top bars	4Φ16	4 Φ 16	4 Φ 16
a _t mm ²	804	804	804
pt %	1.18	1.18	1.18
Bot. bars	4Φ16	4 Φ 16	4 Φ 16
a _t mm ²	804	804	804
$p_t \%$	1.18	1.18	1.18
Stirrups	2- Φ6	2 - Φ6	2- Φ 6
@ (mm)	80	80	80
$P_w \%$	0.64	0.64	0.64
(b) column $(b_c \times d_c)$ mm	(300×300)	(300×300)	(300×300)
Total Bars	12- Φ16	12- Φ16	12- Φ 16
a _g mm ²	2412	2412	2412
pg%	2.62	2.62	2.62
Hoops	24 D6	2 ΦD6	2 ΦD6
@ (mm)	80	80	80
$P_w \%$	0.27	0.27	0.27
(c) connection H×L mm	(2000×3000)	(2000×1500)	(1000×1500)
Hoops	3-Фб	3- Фб	3- Фб
Sets	3 @ 60	3@60	3@60
$a_w mm^2$	192	192	192
$p_w\%$	0.38	0.38	0.38
Shape	Closed	Closed	Closed
(d) Slabs thick. t _s cm	12	12	12
Longitudinal Dir	24 D 8	24 D 8	24 D 8
@ (mm)	100	100	100
Stirrups ratio %	0.38	0.38	0.38
Transverse Dir.	24 D 8	24 D 8	24 D 8
@ (mm)	200	200	200
Stirrups ratio %	0.27	0.27	0.27

Note: a_t : total area of tensile reinforcement, p_t : tensile reinforcement ratio, a_g : total area of longitudinal reinforcement, p_g : gross reinforcement ratio, aw : total area of web reinforcement placed between top and bottom beam bars, ρ_w : web reinforcement ratio, Ec = 14000 $\sqrt{f'c}$ kg/cm², Es = 2.2×10⁶ kg/cm², f_y : yield strength, f'_c : concrete compressive strength, f'_t : concrete tensile strength.

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



a) Reinforcement details of interior beam-column joint



b) Reinforcement details of exterior beam-column joint



c) Reinforcement details of roof corner beam-column joint

Fig. 3. The loading set up and Boundary condition of joints

6. Materials nonlinearity

Steel and concrete are the basic materials used in the structural elements. To model the cyclic characteristics of the earthquake load, a nonlinear material model with specific cyclic features should be used for each.

<u>Steel</u>: In this article, an isotropic kinematics hardening model is used for steel material. As shown in Figure 4, the blushing effect has been taken into account, and there is no stiffness degradation during the cycling. It is acceptable for the skyscraper structure as the maximum steel strain should be less than 2.5%.

Concrete: The plastic-damage model (**J. Lee, 1998**) is used to model the concrete material. The model is a continuum, plasticity-based, model for concrete. It assumes that the main two failure mechanisms are tensile cracking and compressive crushing of the concrete material. It captures the three major characteristics of the concrete in the buildings: (1) the strength of compression is larger than that of tension; (2) the stiffness degrades when it goes into plastic range; (3) the stiffness recovers when it reverses from tension to compression.



Fig.4. Steel constitute law (Sam Lee 2008)



Fig. 5. Concrete in tension (Sam Lee 2008)

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



Figures 5 and 6 show the concrete material's stress-strain curves, the stiffness of the concrete degrades when it unloads from the plastic range. The degradation factors for compression (dc) and tension (dt) are dependent on the plastic strain (ABAQUS,V 6.5). Figure 7 shows the hysteric curve of the concrete, it can be seen that the stiffness recovers when the material stress status reverses from tension to compression.



Fig.7. Concrete hysteric curve (Sam Lee 2008)

In the fixed crack model, the crack direction is determined and fixed at the time of crack initiation. In the rotating crack model, the crack direction is identical with a principal strain direction and rotates if the strain direction changes. The main difference in these crack models is

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

the absence of shear stresses on the crack plane in the rotating crack model due coincidence of principal strain directions with the crack orientation, which makes the rotating crack model more simple. In the fixed crack model the shear resistance of the cracks is modeled by means of the variable shear retention factor, which reflects the aggregate interlock effect of cracked concrete) Concrete in plane stress condition can be well described by a damage model such as the one used in the ABAQUS, see Figure 8. It is based on the "equivalent uniaxial law", which covers the complete range of the plane stress behaviour in tension and compression. The effect of biaxial stress state on the concrete strength is captured by the failure function due to (**Kupfer et al., 2011**). For the tensile response (cracking) the crack band method described above is applied. Similar method is applied for the compressive softening. Thus complete softening behaviour is based on an objective and mesh independe1nt approach.



Fig. 8. a Equivalent uniaxial law (left)



Fig. 8. b Bi-axial failure function by Kupfer2011

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7. Data given and obtained results

Figure 9 shows the 3-D meshed modeling connections with loading , boundary condition and deflection Shapes studying by ABAQUS\CAE 6.7 software for interior, exterior and corner joints.

The obtained theoretically evaluated values of various stresses and displacements for both interior and exterior joints for the case study are tabulated and given in Tables (2),(3) and (4).



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg





Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



c) On knee joint



L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

The effect of the studied parameters on the behavior of beam-column joint are evaluated according to table 2,3and 4 with the following relationships:



1. Relation of story shear force (Vc) ton - story drift ($\theta\%$)

a) Relation of story shear force-story drift at interior joint



b) Relation of story shear force-story drift at exterior joint

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

762



c) Relation of story shear force-story drift at corner joint

Fig. 10. Relation of story shear force(Vc)- Story Drift ($\theta\%$) for Beam-Column Joint

Fig.10 illustrate that in general as the story shear forces (V_c) increase, the corresponding story drift angle (θ %) increase.

2. Relation of joint shear stress (τ_i) kg/cm² -story drift $(\theta\%)$.



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.



b) Relation of story shear stress - story drift at exterior joint



c) Relation of story shear stress-story drift at corner joint

Fig. 11. Relation of Story Shear (τ_i) - Story Drift $(\theta\%)$ for Beam-Column Joint

It is observed at Fig.11 that the relation between joint shear stress (τ_j) and story drift angle $(\theta\%)$ is leaner for story drift (1-2)%.

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

764

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814

Table 2.

Obtained Theoretical Results for Studied Interior Beam-column Joints.

Joint No.	Compressive concrete (f _c) kg/cm ²	Yield strength (fy) kg/cm ²	Axial load ton (N _c)	N _c / f _{c'} A _c	Lateral load ton (V _c)	Draft angle (θ%)	Top lateral Displace- ment mm(δh)	Max principle stress Kg/cm ² (σ ₁)	Joint shear stress kg/cm ² (t _J)	Joint bond stress kg/cm ² (µ _b)	Max principle strain cm/cm (ε ₁ ×10 ⁻⁴)	Joint shear distortion radian (y %)	Energy Absorption (E.A) ton×mm
J (1)	250	2400	0	0	0	0	0	0	0	0	0	0	0
J (2)	250	2400	25	0.15	5	0.345	6	44.11	16.32	8.36	0.129	0.48	480
J (3)	250	2400	40	0.15	11	0.8	12	102	37.75	16.60	0.256	1.11	1200
J (4)	250	2400	60	0.15	45	2.80	56	170.74	66.30	29.11	0.373	1.60	2278.5
J (5)	400	2800	0	0	0	0	0	0	0	0	0	0	0
J (6)	400	2800	25	0.15	7.5	0.45	6.40	70.32	35.32	14.60	0.23	0.6	440
J (7)	400	2800	40	0.15	10	0.71	8.5	104.9	45.33	20.20	0.31	0.77	1580
J (8)	400	2800	80	0.15	51	3.10	62	227.50	82.50	43.02	0.66	1.75	2959
J (9)	600	3600	0	0	0	0	0	0	0	0	0	0	0
J (10)	600	3600	40	0.15	13	0.84	5.2	135.8	53.31	35.39	0.34	0.88	450
J (11)	600	3600	80	0.15	20	1.25	8	210.3	78.77	57.5	0.51	1.29	1600
J (12)	600	3600	120	0.15	61.20	3.80	76	359.1	94.95	67.87	1.42	3.60	3020
J (13)	1200	4000	0	0	0	0	0	0	0	0	0	0	0
J (14)	1200	4000	60	0.15	13	0.68	8.30	142.7	65.62	69.20	0.39	0.92	610
J (15)	1200	4000	120	0.15	22	1.12	14	317.9	106.8	82.64	0.65	1.50	2170
J (16)	1200	4000	240	0.15	75	4.01	86	521.4	155.8	113.20	1.07	2.48	4083

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

Table 3.

Obtained Theoretical Results for Studied Exterior Beam-column Joints.

Joint No.	Compressive concrete (f _c) kg/cm ²	Yield strength (fy) kg/cm ²	Axial load ton N _c	N _c / f _c A _c	Lateral load ton (V _c)	Draft angle (0 %)	Top lateral Displace- ment mm(δh)	Max. principle stress kg/cm ² (σ ₁)	Joint shear stress kg/cm ² (t _J)	Joint bond stress Kg/cm ² (µ _b)	Max. principle strain cm/cm (ε ₁ ×10 ⁻⁴)	Joint shear distortion radian (γ%)	Energy Absorption (E.A) ton×mm
J (17)	250	2400	0	0	0	0	0	0	0	0	0	0	0
J (18)	250	2400	15	0.15	10	0.5	8.16	40	20	10.71	0.15	0.12	190
J (19)	250	2400	30	0.15	13	0.79	12.72	57.5	23.70	24.09	0.603	0.48	390
J (20)	250	2400	50	0.15	15	2.913	18.26	65	32.50	25.20	1.08	1.70	690
J (21)	400	2800	0	0	0	0	0	0	0	0	0	0	0
J (22)	400	2800	25	0.15	15	0.66	9.79	48.75	26.40	15.72	0.22	0.17	305
J (23)	400	2800	40	0.15	23	1.01	18.58	75	40	35.32	1.03	0.80	620
J (24)	400	2800	80	0.15	25	3.40	21.58	80.62	46.63	35.66	1.19	2.20	1098
J (25)	600	3600	0	0.	0	0	0	0	0	0	0	0	0
J (26)	600	3600	40	0.15	20	0.81	10.68	64.50	49.45	39.85	0.93	0.67	430
J (27)	600	3600	60	0.15	32	1.29	18.92	81.57	62.65	43.72	3.75	2.70	860
J (28)	600	3600	120	0.15	35	4.45	28.67	214.6	64	44.25	3.89	2.80	1520
J (29)	1200	4000	0	0	0	0	0	0	0	0	0	0	0
J (30)	1200	4000	80	0.15	25	0.89	13.75	97.62	82.36	53.87	1.05	0.93	850
J (31)	1200	4000	120	0.15	40	1.43	22.44	122.38	107.2	54.62	1.25	1.10	1750
J (32)	1200	4000	240	0.15	45	4.85	32.62	318	116	55.54	4.20	3.70	2082

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814

Table 4.

Obtained Theoretical Results for Studied Corner (Knee) Beam-column Joints.

Joint No.	Compressive concrete (f _c) kg/cm ²	Yield strength (fy) kg/cm ²	Lateral load (V _c) ton	Draft angle (θ%)	Top lateral Displacement (δh) mm	$\begin{array}{c} Max\\ principle\\ stress\\ (\sigma_1)\\ Kg/cm^2 \end{array}$	Joint shear stress (\u03ct_J) Kg/cm ²	Joint bond stress (µ _b) kg\cm ²	Max principle strain ε ₁ ×10 ⁻⁴ cm/cm	Joint shear distortion (γ%) radian	Energy Absorption (E.A) Ton×mm
J (33)	250	2400	0	0	0	5	0	0	0	0	0
J (34)	250	2400	15	1.0	10	87.70	24.20	16.54	0.62	0.73	105
J (35)	250	2400	18	1.2	12.7	102.3	28.10	18.32	0.74	0.86	223
J (36)	250	2400	20	2.6	22.29	122.95	29.77	19.69	1.56	1.82	395
J (37)	400	2800	0	0	0	10	0	0	0	0	0
J (38)	400	2800	15	1.23	12.3	75.53	26.20	25.30	0.71	0.67	150
J (39)	400	2800	28	2.3	23.0	125.1	43.20	28.67	1.15	1.10	300
J (40)	400	2800	30	3.5	35.67	145.50	44.30	30.59	2.73	2.60	540
J (41)	600	3600	0	0	0	0	0	0	0	.0	0
J (42)	600	3600	20	0.8	8.0	82.92	22.48	35.20	0.63	0.562	200
J (43)	600	3600	36	2.35	22.5	233.67	62.26	46.76	2.03	1.67	400
J (44)	600	3600	40	4.9	49.05	245.9	65.47	48.33	4.06	3.42	715
J (45)	1200	4000	0	0	0	0	0	0	0	0	0
J (46)	1200	4000	30	1.10	11.0	146.20	43.50	52.63	1.05	0.934	420
J (47)	1200	4000	46	2.41	22.0	296.12	87.65	53.42	2.15	1.89	850
J (48)	1200	4000	50	5.30	53.51	323.9	96.40	65.90	5.35	4.67	1552

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.





a) Relation of story shear force - lateral top displacement at interior joint



b) Relation of story shear force - lateral top displacement at exterior joint

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg





Fig. 12. Relation of Story Shear Force (V_c) - Lateral Top Displacement $(\delta_h) for$ Beam-Column Joints

Fig.12 illustrates that in general as the story shear forces (V_c) increase, the corresponding lateral top displacement (δ_h) increase.



a) Shear stress at C250 Joint No. (2) for interior joint



b) Shear stress at C600 Joint No. (28) for exterior joint



c) Shear stress at C1200 Joint No. (48) for knee joint





4. Relation of Joint Shear Stress (τ_j) kg/cm²-Joint Shear strain($\gamma\%$).

a) Relation of joint shear stress-joint shear strain joint (distortion) interior joint



b) Relation of joint shear stress - (distortion) exterior joint

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.



c) Relation of joint shear stress-joint (distortion) interior joint (distortion) corner joint

Fig. 14. Relation of Joint Shear Stress (τ_j) –Joint Shear Strain $(\gamma\%)$ for Beam-Column Joints.

Fig. 14 illustrates that in general as the joint shear stress (τ_j) increases, the corresponding joint shear strain (γ) increases.



5. Relation of Principal Tensile Strain (ϵ_1)–Joint Shear Strain (Distortion) ($\gamma\%$) radian.

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg





b) Relation of principal tensile strain-joint shear strain (distortion) exterior joint



c) Relation of principal tensile strain-joint shear strain (distortion) corner joint

Fig. 15. Relation of Principal Tensile Strain(ε_1) – Joint Shear Strain ($\gamma\%$) for Beam-Column Joints

In terms of principal tensile strains, a nearly linear relationship with respect to the joint shear distortion was obtained for various levels as shown in Fig.15.

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.



774



a)Relation of principal strain-joint bond stress for interior joint.



b) Relation of principal strain-joint bond stress for exterior joint

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



c) Relation of principal strain-joint bond stress for corner joint

Fig. 16. Relation of Principal Strain (ϵ_1) – Joint Bond Stress (μ_B) for Joints

It can be seen in Fig. 16 that generally as the principal strains (ϵ_1) increases, the corresponding joint bond stress (μ_B) increases,

7. Relation of Joint Shear Stress (τ_J) kg/cm² –Principle Axial Stress (σ_1) kg/cm².



a) Relation of shear strength (τ_J) -axial stress (σ_1) for interior

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



b) Relation of shear strength (τ_J) - axial stress (σ_l) for exterior joint



c) Relation of shear strength (τ_J) - axial stress (σ_1) for corner joint



Fig.17 illustrates that in general as the axial stress (σ_1) increases the corresponding shear stress (τ_J) increases too up to the maximum stresses.



8. Relation of Principle Axial Stress (σ_1)-Principle Axial Strain(ϵ_1).

a) Relation of max. principle stress - max. principle strain for interior joint



b)Relation of max. principle stress - max. principle strain for exterior joint

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg





Fig.18. Relation of Maximum Principle Stress (σ_1) – Maximum Principle Strain (ϵ_1) for Beam-Column Joints

Generally, as the axial stress (σ_1) increases corresponding axial strain (ϵ_1) increases too up to the maximum stress as shown in Fig. 18

9. Relation of Energy Absorption (EA)–Lateral Displacement(δh)



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



b) Relation of Energy Absorption - Lateral load for exterior joint



c) Relation of Energy Absorption (E.A.) (ton×mm) –Lateral Load (vc)ton for corner (Knee joint)

Fig.19. The Relation of Energy Absorption (E.A.) - Lateral Load(Vc) for Joints

a nearly linear relationship with respect to the lateral load was obtained for various levels energy absorption as shown in Fig.19.

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

8. Analysis and discussion of the obtained results

- 8.1. W.R.T Strength and Stresses Points of View:
- 8.1.1. Effect of Concrete Compressive Strength (f'c) on Joint Shear Stresses (τJ):

The obtained results on interior, exterior and knee connections indicated that the governing factor influencing the joint shear strength is the concrete compressive strength



Fig.20. Relation of Concrete Compressive Strength (fc) - Joint Shear Stress (τ j)



Fig. 21. Relation of Concrete Compressive Strength (\dot{f}_c) - Joint Mode Strength (Joint Shear-Resistance)

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814

Based on Table 5 and Figures 20 and 21, it is obvious that; as the compressive strength of concrete increases the corresponding joint shear stress increases for all types of joints. Also it obvious that the interior joints posses higher joint shear stress in comparison with both that for exterior or corner joint. Also Figure 20 indicates that use of high strength concrete has a beneficial effect on increasing the connection shear strength compared to that of normal–strength. An increase of about 2.5% for interior joint, 4.8% for exterior joint and 3.5% for knee joint were observed. The results were compared with that obtained by (**Felica th. 2007**) studies, where an increase of about 5% case of no moment was stated. The (J) mode strength, defined by $(\tau j/f_c)$, for the various joints was calculated and plotted against the corresponding compressive strength (f_c) as shown in Figure 21. Figure 21 declared that the $(\tau j/f_c)$ mode strength decrease by increase the grade of concrete. Higher values were corresponding to interior joints rather than that for exterior joints and finally smaller value were for corner joints.

Table 6 gives the available codes recommendations for joint shear strength values for the studied types of R.C joints. Table 7 also indicates a comparison between the calculated values of joint shear strength as reported in the commentary of different Codes and the obtained theoretical results of beam-column joints in our study.

The obtained values of joint shear stress (τ_j) as calculated by the available Codes as well as the our obtained results are plotted against the used corresponding concrete strength $(\dot{f_c})$ in Figures 22, 23 and 24 for the studied joints.



Fig. 22. Concrete Compressive Strength (\dot{f}_c) – Joint Shear Stress (τ_i) Interior Joint

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

Table 5.

Effect of Concrete Compressive Strength on Shear Stresses on Beam- Column Joint.

	Joint No.	Yield strength (f _y)kg/cm ²	$N_c / (f_c)A_c$	Lateral load ton (V _c)	Joint shear stress kg/cm ² (τ _J)	Max principal stress kg/cm ² (σ ₁)	l Joint bond stress kg/cm ² (µ _b)	(J) mode strength (τ _J)/(f _c [*])	Energy Absorption (E.A) Ton×mm	Max. principal stress / compressive stress (σ_1) / (fc')
nt	J (4)C250	2400	0.15	45	66.30	170.74	24.11	0.265	2278	0.68
joj	J (8)C400	2800	0.15	51	82.50	227.50	43.02	0.521	2959	0.57
srior.	J (12)C600	3600	0.15	61	94.95	359.1	67.87	0.158	3020	0.59
Inte	J(16)C1200	4000	0.15	75	155.8	521.4	113.20	0.095	4083	0.45
nt	J (20)C250	2400	0.15	15	32.50	65	25.20	0.202	690	0.26
ioi	J (24)C400	2800	0.15	25	46.43	80.62	35.60	0.107	1098	0.20
srior.	J (28)C600	3600	0.15	35	64	214.6	44.25	0.265	1520	0.35
Exte	J (32C1200	4000	0.15	45	116	318	55.54	0.097	2082	0.26
Ę	J (36)C250	2400	0.15	20	29.77	122.95	19.69	0.12	395	0.49
oin	J (40)C400	2800	0.15	30	44.30	145.50	30.59	0.11	540	0.36
ner j	J (44)C600	3600	0.15	40	65.47	245.9	48.33	0.109	715	0.41
Cor	J(48)C1200	4000	0.15	50	96.40	323.90	65.90	0.08	1552	0.27

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814

Table 6.

Different Codes	Nominal Joint Shear Strength (Interior Joint)	Nominal Joint Shear Strength (Exterior Joint)	Nominal Joint Shear Strength (Knee Joint)
ACI 352R-02 and ACI 318-02	$V_{\rm n} = \gamma_{\rm ACI} \sqrt{f_{\rm c}} b_{\rm j} h_{\rm c}$	Vn ex. = 0.75 Vn int.	$f_{\rm j} = 0.19 (\dot{f}_{\rm c})$
ECCS 203 (2001)	$\tau_{\rm j} = 0.96 A_{\rm j} \sqrt{f_{\rm c}}$		
AIJ 1997	$V_{j} = k\phi f_{j}b_{j}D_{j}, \text{ or,}$ $v_{j} = 0.8 \times (f_{c})^{0.7}$	$f_{\rm j} {\rm ex.} = 0.9 f_{\rm j}$ int.	$f_{j} = 0.48 f_{j} ACI$
NZS 3101: 1995	$f_{\rm j} = 0.2 \times (f_{\rm c}) \rm Aj$	$f_j \text{ ex.} = 0.9 \ 8 \ f_j$ int.	
EN 1998-1: 2003	$V_{\rm jh} \leq \eta f_{\rm cd} \sqrt{1 - rac{V_{\rm d}}{\eta}}$	V_{jh} Ex. = 0.80Vjh Int.	
	$\eta = 0.6 \left(1 - \frac{f_c}{250} \right),$		

Codes Recommendations for Shear Strength of Different Types of Joints.

Remarks and Symbols:

 V_n : nominal shear strength of beam-column joints according to the general procedures of ACI 318; A_j : is the effective horizontal joint area defined as the product of the column dimension in the direction of loading; γ_{ACI} : is the joint shear strength factor = 0.67; f'_c : is the specified concrete compressive strength; \mathbf{b}_j : is the effective joint shear width; \mathbf{h}_c : is the column depth; τ_J : the nominal shear strength of the joint as a function of only concrete strength; \mathbf{v}_{jh} : nominal shear stress; \mathbf{v}_d : normalized axial force ratio on column; η : denotes the reduction factor on concrete compressive strength due to tensile strains in transverse direction; f_{cd} : concrete cylinder compressive strength; \mathbf{k} : is the factor dependent on the shape of in-plane geometry (1.0 for interior connections, 0.7 for exterior connections and T-shape top story joints. and 0.4 for corner knee connections); $\boldsymbol{\phi}$: is the factor for the effect of out-of-plane geometry (1.0 for joints with transverse beams on both sides and 0.85 for other types of joints); f_j : is the standard value of the joint shear strength (as a function of concrete compressive strength); and D_j : is the effective column depth. ;Int.: internal joint,

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

Table 7.

The Calculated Values of the Available Codes Recommendations as well as Obtained Results for Joint Shear Strength (τ_J) for the Studied Joints.

	Joint No [.]	Yield strength (f_y) (kg/cm^2)	Experimental results (\u03ct_J)(kg/cm ²)	$\begin{array}{c} ACI \ 352R-02 \ and \\ ACI \ 318-02 \ (\tau_J) \\ (kg/cm^2) \end{array}$	NZS 3101: 1995 (τ _J)(kg/cm ²)	EN 1998-1:2003 $(\tau_J)(kg/cm^2)$	AIJ 1997 (τ _J)(kg/cm ²)	ECCS 203 (2001) (τ _J)(kg/cm ²)
int	J (4)C250	2400	66.30	95.34	45	67.45	34.34	128
.jo	J (8)C400	2800	82.50	120.60	72	85.20	53.03	144
rior	J (12)C600	3600	94.95	147.70	108	104.37	77.52	198
Inte	J(16)C1200	4000	155.8	208	216	147.37	114.42	280.59
nt	J (20)C250	2400	32.5	71.50	44	27.47	30.90	
joi	J (24)C400	2800	46.63	90.45	71	42.42	47.70	
rior	J (28)C600	3600	64	110.7	105	62.01	69.76	
Exte	J (32C1200	4000	116	157	211	117.6	102.6	
ıt	J (36)C250	2400	29.77	47.50			23	
joi	J (40)C400	2800	44.30	76			35	
ner	J (44)C600	3600	65.47	114			55	
Cor	J(48)C1200	4000	96.40	228			110	

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814



Fig. 23. Relation of Concrete Compressive Strength (f_c) – Joint Shear Stress (τ_j) Exterior Joint



Fig. 24. Relation of Concrete Compressive Strength (f'c) – Joint Shear Stress (τj) Knee Joint

<u>AIJ 1997</u> Architectural Institute of Japan (Design guidelines for earthquake resistant reinforced concrete building based on ultimate strength concept and commentary) has a standard value of the joint shear strength (τ_i) is suggested as given by Eq. (10);

$$\tau_{\rm i} = 0.8 \times (f_{\rm c})^{0.7} \tag{10}$$

Based on same trend of reference it is illustrated that the following equations 11, 12 and 13 can evaluated for our studied joints.

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

$\tau_{ju} = 1.56 \times f_c^{0.673}$	Interior beam-column joint	(11)
$\tau_{ju} = 1.13 \times f_c^{0.573}$	Exterior beam-column joint	(12)
$\tau_{ju} = 1.09 \times f_c^{0.573}$	Knee beam-column joint	(13)

On the light of Table 7 and Figures 22, 23 and 24 for comparing codes recommendations with our results, it is obtained that:

- 1. <u>For Interior Joint</u> the maximum shear stress capacity for the studied connections is 69% lower as per ACI 318M-02 and is lower as 52% per ECCS 203 (2001) and higher than that provided by NZS 3101:1995 per 67% and higher than that provided by AIJ 1997 per 52% and also the same per EN 1998-1:2003.
- For Exterior Joint the maximum shear stress capacity for the studied connections is 45% lower as per ACI 318M-02 and is lower as 74% per NZS 3101:1995 and higher than that provided by per 85% per EN 1998-1:2003 and higher than that provided by AIJ 1997 per 95%.
- 3. For Knee Joint the maximum shear stress capacity for studied connections is 63% lower as per ACI 318M-02 and higher than that provided by AIJ 1997 per 77%.

8.1.2. Effect of Concrete Compressive Strength (f'c) on Bond Strength (μb).

A maximum bond stress (u_b) of beam reinforcement over the column width was estimated by assuming simultaneous yielding of the beam reinforcement in tension and compression at the two faces of the joint. The bond strength was assumed proportional to the square root of the concrete compressive strength Table 8. The beam bar bond index (BI) was defined by dividing the average bond stress by the square root of the concrete strength.



Fig. 25. Relation of Concrete Compressive Strength (\dot{f}_c)-Joint Bond Stress kg/cm² (μ_b)

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

786



Fig. 26. Relation of A beam bar bond index (BI) - Range of Mode Strength(J) (Effect of Bond Capacity)

Table 8.

Effect of Bond Capacity of Interior, Exterior and Corner (Knee) Joint at Concrete Compressive Strength.

č	Joints No.	Yield strength of reinforcement (f _y) kg/cm ²	(J) Range of mode strength $(\tau_j \setminus f_c) = j$	Average bond strength (µ _b) kg/cm ²	(BI) Average bond strength / k=1.8 square root of (f _c ') (μ _b / k√f _c ')	Average bond strength\ concrete compressive stress (µ _b \f _c ')
л	J (4)C250	2400	0.28	29.11	0.84	0.116
eric	J (8)C400	2800	0.22	43.02	1.20	0.107
jc	J (12)C600	3600	0.18	67.87	1.52	0.113
	J(16)C1200	4000	0.15	113.20	1.80	0.094
	J (20)C250	2400	0.162	25.20	0.88	0.11
ior It	J (24)C400	2800	0.138	35.66	1.01	0.089
ioir	J (28)C600	3600	0.11	44.25	1.28	0.074
щ	J (32C1200	4000	0.097	55.54	1.58	0.046
	J (36)C250	2400	0.13	19.69	0.79	0.078
ner nt	J (40)C400	2800	0.10	30.59	0.93	0.076
joi	J (44)C600	3600	0.085	48.33	1.09	0.080
	J(48)C1200	4000	0.073	65.93	1.43	0.055

Figure 25 shows the relation between compressive strength of concrete (f_c) and the joint bond stress (μ_b) for studied joints for the studied case of loading. The increase of concrete

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

compressive strength with yielding of the beam reinforcement effective to increase the bond strength.

This result is important, it was observed that the interior joint has maximum bond strength at high concrete compressive strength, it can be denoted that interior joint is stronger than exterior joint.

Figure 26 shows the calculated value of J-mode strength defined by the parameter of (K) .Larger value of k generally gives larger joint shear strength. The Fig. 26 also compare the calculation and the average strength reported in the commentary of **AIJ Guidelines (AIJ 1999)** derived from Japanese database of test of beam-column joint beam bar bond index (BI) was introduced to indicate the severity of bond stress relative to the bond strength.

Based on the work of (Kazuhiro K.1991)

Bond index=(BI) =
$$\frac{\mathbf{u}_b}{\sqrt{\mathbf{f}_c'}} = \frac{fy}{2\sqrt{fc} \setminus \frac{db}{hc}}$$
 (14)

Based on our results (Table 8, Fig. 25and 26) the bond index can be represented by the equations from 15 to 20 for the studied joints as follows:

1. **For interior joint:** The beam bar bond index (BI) was defined by dividing the average bond stress (μ_b) by the square root of the concrete and given by :

(BI) =
$$\frac{\mathbf{u}_b}{\sqrt{\mathbf{f}_c'}} = \frac{\mathbf{f}_y}{3.5\sqrt{\mathbf{f}_c'}} \frac{\mathbf{d}_b}{\mathbf{h}_c}$$
 for 2400 $\leq f_y < 3600$ (kg/ cm²) (15)

(BI) =
$$\frac{\mathbf{u}_{b}}{\sqrt{\mathbf{f}_{c}'}} = \frac{\mathbf{f}_{y}}{2\sqrt{\mathbf{f}_{c}'}} \frac{\mathbf{d}_{b}}{\mathbf{h}_{c}}$$
 for 3600 < $f_{y} \le 4000$ (kg/ cm²) (16)

where f_y : yield strength of beam bars in kgf/cm², d_b : diameter of beam bars, h_c : column width and f_c : concrete compressive strength in kgf/cm².

2. For Exterior Joint the bond index (BI) is given by Eqs. (17) and (18):

$$(BI) = \frac{u_{\rm b}}{\sqrt{f_{\rm c}}} = \frac{f_{\rm y}}{4.50\sqrt{f_{\rm c}}} \frac{d_{\rm b}}{h_{\rm c}} \quad \text{for } 2400 \le f_{\rm y} < 3600 \quad (\text{kg/ cm}^2)$$
(17)

$$(BI) = \frac{u_{b}}{\sqrt{f_{c}'}} = \frac{f_{y}}{3.20\sqrt{f_{c}'}} \frac{d_{b}}{h_{c}} \quad \text{for } 3600 < f_{y} \le 4000 \quad (\text{kg/ cm}^{2})$$
(18)

3. For Knee Joint the bond index (BI) is given by Eqs. (19) and (20):

(BI)=
$$\frac{u_{\rm b}}{\sqrt{f_{\rm c}}} = \frac{J_y}{6.20\sqrt{f_{\rm c}}} \frac{d_b}{h_c}$$
 for $2400 \le f_y < 3600 \ (\text{kg/ cm}^2)$ (19)

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814

(BI)=
$$\frac{u_{\rm b}}{\sqrt{f_{\rm c}}} = \frac{f_y}{3.20\sqrt{f_{\rm c}}} \frac{d_b}{h_c}$$
 for 3600 < $f_y \le 4000$ (kg/ cm²) (20)

By comparing our results by AIJ Guidelines.

$$\mathbf{u}_{\mathrm{b}} = \mathbf{k} \sqrt{\mathbf{f}_{c}} \sum \phi \mathbf{D}_{\mathrm{b}}$$
(21)

Where : $\Sigma \varphi$ is the total perimeter length of longitudinal bar in the first layer of beam side in the column in mm, and D_b : beam depth in mm, The value of (k) of 1.8 for modeling of bond capacity of non yielding tensile bar passing beam-column joint by (Lowes, L. 2002).

Finally the value of (*k*) was suggested for chosen modeling of bond capacity using the following equation for different types of joints;

$$u_{b} = k \sqrt{f_{c}}$$

where (k) is a constant depends on used grade of concrete as given in the following Table.

Table 9.

Suggested Values of (k) for Calculating Average Bond Capacity of R.C. Joints.

	(k) values of (f'_c)	
Type of Joint	C250 and C400	C600 and C1200
Interior joint	1.80	3.20
Exterior joint	1.58	1.70
Knee joint	1.20	1.92

From the above results and values, it is obvious that for any used grade of concrete interior beam-column joint has larger safety margin than exterior beam-column joint. The same result was found in reference (**Hitoshi Sh. 2004**).

Figure 27 illustrates the relation between the concrete compressive stress (f_c) and the corresponding induced ratio of compressive stress /bond stress $((\mu_b \ \dot{y_c}))$. Figure 27 indicates that the increase of concrete grade is usually accompanied by decreased in the induced $(\mu_b \ \dot{y_c})$. Also its obvious that the interior joints posses the higher value of $((\mu_b \ \dot{y_c}))$ than that for exterior and corner joint corresponding to the increase of concrete grade (f_c) .

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.



Fig. 27. Relation of Concrete Compressive Strength ($\dot{f_c}$)- Bond Stress Compressive Strength ($\mu_b \backslash \dot{f_c}$) for Studied Joints

8.1.3. Effect of Concrete Compressive Strength (f_c) on Maximum Principle Stresses (σ_l):

Figure 28 and Table 5 show maximum principle stresses values of the joint concrete at the maximum strength for peak loading for interior, exterior and knee joint. The increase of concrete compressive strength is effective to increase the principle stresses.

For C250 and C400, the principle stresses for exterior and knee joint is 62% that for interior beam column joint, however for C600 the principle stress for exterior and knee joint equals 57% that for interior beam column joint. Finally for C1200 the principle stress for exterior and knee joint is about 43% of that for interior beam column joint.

(Hitoshi Sh. 2005) stated that the strength of the exterior beam-column joints is 53% of the strength of the interior beam-column joint.

790

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814



Fig.28. Relation Concrete Compressive Strength(f_c) - Maximum Principle Stress(σ_1)

Figure 29 illustrates that as the ratio of $(\sigma_1 \backslash f'_c)$ decreases with the corresponding concrete compressive strength (f'_c) increases for (C250-C400) for interior ,exterior and corner joint , however the ratio of $(\sigma_1 \backslash f'_c)$ increases with the corresponding concrete compressive strength (f'_c) increases from(C400-C600). Also it is obvious that the interior joints posses higher joint ratio of $(\sigma_1 \backslash f'_c)$ in comparison with that for both corner and exterior joint respectively.



Fig.29. Relation of Concrete Compressive Strength (f_c) - Maximum Principle Stress \ Concrete Compressive Strength $(\sigma_1 \setminus f_c)$ for Studied Joints

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

8.2. W.R.T Deformations and Strains Points of View:

8.1. Effect of Concrete Compressive Strength (f_c) on Joint Deformation (horizontal displacement (δ h), Drift angle (θ %) Ratio and Shear Strain (γ %) {Distortion}:

- 1. It can be seen according to the Table 10 and Figure 30, that: as the compressive strength increases the horizontal displacement decreases for studied joints. Concrete compressive strength has a moderate effect to decrease horizontal displacement.
- 2. Based on Figure 31 it is obvious that the increase of concrete grade (f_c) is usually accompanied with a decrease of the induced drift angle ($\theta\%$) for studied type of R.C joints. Also the induced drift angle ($\theta\%$), for a given grade of concrete (f_c), mainly depends on the type of joint. The interior joint possesses the smallest value of drift angle ($\theta\%$) in comparison with that for exterior or corner joint. The corner joint possess the higher value of drift angle ($\theta\%$).
- 3. It is obvious that on light of Figure 32 the increase of concrete grade (f_c) is usually accompanied with a slight decrease of joint shear distortion ($\gamma\%$). At the same time the corner joint possess higher value compared with that for both exterior and interior joints. The minimum value of joint shear distortion ($\gamma\%$) is corresponding to the interior joints







Fig. 31. Relation of Concrete Compressive Strength (f'_c)–Drift angle (θ %)



Fig. 32. Relation of Concrete Compressive Strength (f'_c) –Joint Shear Distortion radian ($\gamma\%$)

8.2. Effect of Concrete Compressive Strength (fc`) on the Maximum Principal Strains ($\varepsilon 1$):

Figure 33 and Table 10 indicates that the increase of concrete grade is usually accompanied by an increase in the induced principle strains disregarding the type of joint. Also it is interesting to note that Interior joint usually possess higher values of maximum induced principle strain for any grade of concrete. The smallest values of maximum

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

principle strains are corresponding to corner joints. Also Figure 33indicates that the rate of increase of maximum principle strain with respect to the increase of concrete grade is more or less equal for all kinds of studied joints.

Figure 34 indicates that the increase of concrete grade is usually accompanied by an increase in the induced principle stress / principle strain ratio (σ_1/ϵ_1), However, concrete compressive strength (f'_c) has a slight effect to increase (σ_1/ϵ_1) for corner joints. Also it is obvious that an interior joints and exterior joint posses the same ratio of increasing the (σ_1/ϵ_1) corresponding to the increasing of concrete grade (f_c).



Fig. 33. Relation of Concrete Compressive Strength (f'_c) - Max. Principal Strain (ε_1) cm/cm



Fig. 34. Relation of Concrete Compressive Stress (f_c) – Ratio of Maximum Principle Stress / Maximum Principle Strain (σ_1 / ϵ_1) for Studied Joints

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814

Table 10.

Effect of Concrete Compressive Strength on Deformations and Strains of Beam-Column Joint.

J	Joint No.t	Yield strength (f _y) kg/cm²	N./ f _c A _c	Lateral load ton (V.)	Draft angle (0%)	Top lateral Displacem ent mm(8h)	Max principle strain cm/cm (&i×10 ⁴)	Jointshear distortion radian (Y%)	Energy absorption (EA) Ton×m m	Max. principle stress (kg/cm²)(ơ _i)	Max. Pristress/Max. Pr. Strain (Gr\&i)× 10 ⁴ kg/cm ²
L	J (4)C250	2400	0.15	50	2.80	56	2.73	4.08	1200	170.74	62.54
int ii	J (8)C400	2800	0.15	50	2.70	54	3.76	3.75	1480	263	70.13
joi	J (12)C600	3600	0.15	50	2.50	52	4.42	3.60	1700	359	81.22
-	J(16)C1200	4000	0.15	50	2.20	45	4.97	3.48	2170	521	104.82
	J (20)C250	2400	0.15	50	3.00	60	2.08	4.80	890	65	31.25
nt	J (24)C400	2800	0.15	50	2.90	55	3.19	4.05	1200	145.2	45.52
Exte	J (28)C600	3600	0.15	50	2.65	53	3.89	3.80	1580	214.6	55.16
щ	J (32C1200	4000	0.15	50	2.50	50	4.20	3.70	2028	318	75.71
	J (36)C250	2400	0.15	50	3.60	61	1.56	5.05	595	122.95	78.82
ner nt	J (40)C400	2800	0.15	50	3.40	58	2.73	4.95	740	218.7	80.11
joi	J (44)C600	3600	0.15	50	3.0	54	2.96	4.80	1015	245.9	83.07
-	J(48)C1200	4000	0.15	50	2.80	52	3.35	4.67	1252	323.9	96.68

8.3.W.R.T Energy absorption (E.A)point of view:

On the light of Figure 35 and Table 10, it is obvious that as the compressive strength of used concrete increases the dissipated energy considerably increases disregarding the type of joint. Mean while for a given concrete grade the dissipated energy is higher for interior joint rather than that exterior joint, at the same time the later one shows a larger value than that for corner joint.

Meanwhile for C400 and C250 it has more higher per 175% for interior joint than that for exterior and knee joint. It can also be denoted that interior joint for C1200 is stronger and possesses more ductility of than that for other joints because this joint absorbed the highest total energy amount.



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

8.4.W.R.T mode of failure of beam-column joints:

796

Based on the obtained results it is obvious that for the case of studied loading systems three different modes of failure were observed .Such modes are characterized as follows and shown in Fig. 36,37 and 38:

- 1. <u>(B)-mode</u> = beam bond failure ,If joint shear increase keeping constant bond resistance, the beam bars slip into the joint at the beam end in compressive side, while bars slip out in tensile side. By considering the deformation compatibility in beam bars and concrete (beam flexure yielding), the elongation of beam bars cause opening of crack in concrete J (2,4,6,8) for interior joint ,J(18,20,32) Exterior joint and (34,36) for Knee joint.
- 2. (J)-mode = joint shear failure, in the beam-column connection occurs when Joint shear exceeds the shear strength of the beam-column connection. Failure models using the truss mechanism or the strut mechanism regard thus rotational movements of the segments cause uneven opening of the diagonal cracks like flexural cracks J (10,12,16) for interior joint J(24,26,30) Exterior joint and (34,36) for Knee joint.
- 3. <u>(JB)-mode</u> =Plastic hinge failure The next generation of beam-column joint models decoupled the inelastic response of the beams, joint moment-rotation data from beam-column anchorage failure for longitudinal reinforcement embedded in the joint controls inelastic joint action under earthquake loading J (14) for interior joint ,J(28) Exterior joint and (42,44) for Knee joint.



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



Fig.36. *a Deformation Mode by* (B)-mode (Hitoshi Sh. 2005) (B)-mode Joint No.(2)-obtained results



(JB)-mode (Hitoshi Sh. 2005)











Fig.36.c Deformation Mode by (J)-mode (Hitoshi Sh. 2004) (J)-mode Joint No.(16) -obtained results

Fig. 36. Analytical Crack Patterns at Final Loading Stage for Interior Beam-Column Joint



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.



Fig.37.a Deformation Mode by (B)-mode (Hitoshi Sh. 2005) (B)-mode Joint No.(21)-obtained results



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



Fig.37.b Deformation Mode by (JB)-mode (Hitoshi Sh. 2005) (JB)-mode Joint No.(28)-obtained results



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



Fig.37.c Deformation Mode by (J)-mode (Hitoshi Sh. 2005) (J)-mode Joint No.(32)-obtained results





Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



Fig.38.a Deformation Mode by (B)-mode (Hitoshi Sh. 2010) (B)-mode Joint No.(36)-obtained results



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.



Fig.38.b Deformation Mode by (JB)-mode (Hitoshi Sh. 2010) (JB)-mode Joint No.(42)-obtained results



Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg



Fig.38.c Deformation Mode by (J)-mode (Hitoshi Sh. 2010) (J)-mode Joint No.(48)-obtained results

Fig.38. Analytical Crack Patterns at Final Loading Stage for Corner Beam-Column Joint

9. Conclusions and Recomendations

The following conclusions can be drawn out from the performance-based study concerning the parameters affecting the mechanical static behavior of interior, exterior and knee (roof corner) joints, for the case of study of loading.

9.1.W.R.T stresses point of view:

9.1.1. Joint Shear Strength (τ_J):

- 1. The obtained results on interior, exterior and knee connections indicated that the governing factor influencing the joint shear strength is the concrete compressive strength alone. The concrete strength is considered as the main parameter in determining the ultimate shear capacity.
- 2. Generally as the compressive strength of concrete increases the corresponding joint shear stress increases too for all types of joint. Also it obvious that the interior joints posses higher joint shear stress in comparison with that for both exterior or corner joint.

806

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

- 3. The (J) mode strength, defined by (τ_i/f_c) , for the various joints was calculated and plotted against the corresponding compressive strength (f_c) declared that the (τ_i/f_c) mode strength decreases by increasing the grade of concrete. Higher values were corresponding to interior joints rather than that for exterior joints and finally smaller values were for corner joints.
- 4. Based on our results for the studied joints the following equations 24, 25 and 26 are proposed:
 - $\tau_{ju} = 1.56 \times f_c^{0.673}$ $\tau_{ju} = 1.13 \times f_c^{0.573}$ $\tau_{ju} = 1.09 \times f_c^{0.573}$ For interior beam-column joint (24)
 - For exterior beam-column joint (25)
 - For knee beam-column joint (26)

A comparison of our results for joint shear strength for the studied joints with that given by available codes recommendations declared that :

- For Interior Joint the maximum shear stress capacity for the studied connections 1. is 69% lower as per ACI 318M-02 and is lower as 52% per ECCS 203 (2001), however it is higher than that provided by NZS 3101:1995 per 67% as well as it is higher than that provided by AIJ 1997 per 52% and finally it is the same per EN 1998-1:2003.
- 2. For exterior Joint the maximum shear stress capacity for the studied connections is 45% lower as per ACI 318M-02 and is lower as 74% per NZS 3101:1995 however it is higher than that provided by EN 1998-1:2003 per 85% and , finally it is higher than that provided by AIJ 1997 per 95%.
- 3. For knee Joint the maximum shear stress capacity for studied connections is 63% lower as per ACI 318M-02 and higher than that provided by ALJ 1997 per 77%.

9.1.2. Joint bond stress (u_b) :

- 1. The increase of concrete compressive strength with yielding of the beam reinforcement are effective parameters to increase the bond strength of beam reinforcement over the column width.
- 2. Based on our results the bond strength can be represented by the equations 27 to 32 for studied joints as follows:
- 3. For interior joint: The beam bar bond index (BI) was defined by dividing the average bond stress (μ_b) by the square root of the concrete and given by Eqs. 27and 28:

(BI) =
$$\frac{\mathbf{u}_b}{\sqrt{\mathbf{f}_c'}} = \frac{\mathbf{f}_y}{3.5\sqrt{\mathbf{f}_c'}} \frac{\mathbf{d}_b}{\mathbf{h}_c}$$
 for $2400 \le f_y < 3600$ (kg/ cm²) (27)

(BI) =
$$\frac{\mathbf{u}_{b}}{\sqrt{\mathbf{f}_{c}}} = \frac{\mathbf{f}_{y}}{2\sqrt{\mathbf{f}_{c}}} \frac{\mathbf{d}_{b}}{\mathbf{h}_{c}}$$
 for 3600 < $f_{y} \le 4000$ (kg/ cm²) (28)

where f_v : yield strength of beam bars in kgf/cm², d_b : diameter of beam bars, h_c : column width and f_c : concrete compressive strength in kgf/cm².

4. For Exterior Joint : the bond index (BI) is given by Eqs. (29) and (30):

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814

$$(BI) = \frac{u_{b}}{\sqrt{f_{c}}} = \frac{f_{y}}{4.50\sqrt{f_{c}}} \frac{d_{b}}{h_{c}} \qquad \text{for } 2400 \le f_{y} < 3600(\text{kg/ cm}^{2})$$
(29)

$$(BI) = \frac{u_{\rm b}}{\sqrt{f_{\rm c}}} = \frac{f_{\rm y}}{3.20\sqrt{f_{\rm c}}} \frac{d_{\rm b}}{h_{\rm c}} \quad \text{for } 3600 < f_{\rm y} \le 4000(\text{kg/ cm}^2)$$
(30)

5. <u>For Knee Joint</u>: The bond index (BI) is given by Eqs. (31) and (32):

(BI)=
$$\frac{u_{\rm b}}{\sqrt{f_{\rm c}}} = \frac{f_y}{6.20\sqrt{f_{\rm c}}} \frac{d_b}{h_c}$$
 for $2400 \le f_y < 3600 \, (\text{kg/ cm}^2)$ (31)

(BI)=
$$\frac{u_{\rm b}}{\sqrt{f_{\rm c}}} = \frac{f_y}{3.20\sqrt{f_{\rm c}}} \frac{d_b}{h_c}$$
 for 3600 < $f_y \le 4000$ (kg/ cm²) (32)

6. Finally the value of of the bond index (BI) was suggested for the chosen modeling of bond capacity as follows using the following equation for different types of joints is given by Eqs. (33);

(BI)=
$$\frac{\mathbf{u}_b}{\sqrt{\mathbf{f}_c}} = k = cons \tan t$$
 (33)

Where (k) is a constant depend on both used grade of concrete as given in the following Table. Suggested Values of (k) for Calculating Average

Bond Capacity of R.C Joints.

Type of Loint	(k) values of (f_c)						
Type of Joint	C250 and C400	C600 and C1200					
Interior joint	1.80	3.20					
Exterior joint	1.58	1.70					
Knee joint	1.20	1.92					

- 9.1.3. Axial Principle Stress (σ 1):
 - 1. The increase of concrete compressive strength is effective to increase the induced principle stresses. The induced principle stresses considerally affected by both grade of concrete and type of joint.
 - 2. Also the ratio of (σ_1 / f_c) usually decreases with the increase of the corresponding concrete compressive strength (f'_c) . However, interior joints posses higher joint ratio of (σ_1 / f_c) in comparison with that for corner then exterior joint respectively

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

9.2.W.R.T Deformations and Strains point of view:

9.2.1. Joint deformation (lateral displacement $\{\delta h\}$):

- 1. Generally as the compressive strength increases the horizontal displacement decreases for the studied joints. Concrete compressive strength has a beneficial effect to decrease horizontal displacement.
- 2. The interior joint possesses the smallest value of horizontal displacement (δ_h) in comparison with that for exterior or corner joint. The corner joint possess the higher value of (δ_h).

9.2.2. Joint deformation (drift ratio angle $\{\theta\%\}$):

- 1. The increase of concrete grade (f_c) is usually accompanied with a decrease for the induced drift angle (θ %) for the studied types of R.C joints. Also the induced drift angle (θ %), for a given grade of concrete (f_c), mainly depends on the type of joint.
- 2. The interior joint possesses the smallest value of drift angle (θ %) in comparison with that for exterior or corner joint. The corner joint possess the higher value of drift angle (θ %).

9.2.3. Joint deformation (shear strain {distortion γ %}):

1. The increase of concrete grade (f_c) is usually accompanied with a slight decrease of joint shear distortion ($\gamma\%$). At the same time the corner joint possess higher value compared with that for both exterior and interior joints. The minimum value of joint shear distortion ($\gamma\%$) is corresponding to the interior joints.

9.2.4. Axial principle strains (ɛ1):

- 1. The increase of concrete grade is usually accompanied by an increase in the induced principle strains disregarding the type of joint.
- 2. Also it is interesting to note that Interior joint usually possess higher values of maximum induced principle strain for any grade of concrete. The smallest values of maximum principle strains are corresponding to corner joints.
- 3. Increase of concrete grade is usually accompanied by an increase in the induced (σ_1/ϵ_1) ratio. Also its obvious that an interior joints and exterior joint posses the same ratio of increasing the (σ_1/ϵ_1) corresponding to the increasing of concrete grade (f_c^{-}) . Also it is indicated that the rate of increase of maximum principle strain with respect to the increase of concrete grade is more or less equal for all kinds of studied joints.

9.3. W.R.T energy absorption (E.A):

As the compressive strength of used concrete increases the dissipated energy considerably increases disregarding the type of joint.Mean while for a given concrete grade

the value of dissipated energy is higher for interior joint rather than that for exterior joint, and at the same time the later one shows a larger value than that for corner joint.

9.4. W.R.T Mode of Joint Failure:

Three modes of joint failure were recorded in the case namely:

(**B**)-mode = beam bond failure :J (2,4,6,8) for interior joint ,J(18,20,32) Exterior joint and (34,36) for Knee joint.

(**J**)-mode = joint shear failure: J (10,12,16) for interior joint J(24,26,30) Exterior joint and (34,36) for Knee joint.

(JB)-mode = plastic hinge failure: J (14) for interior joint ,J(28) Exterior joint and (42,44) for Knee joint.

10. Recommendations

The following topics can be recommended as subjects for future research study.

- 1. To modify the joint failure into more ductile beam yield failure mode, it is effective to increase the moment capacity of joint, by increasing of longitudinal reinforcement in joint core inevitably also increase the beam moment capacity relative to the induced moment at beam ends yield in flexure,
- 2. High strength concrete when used in columns connection needs large quantities of confining reinforcement to ensure ductile behavior, which can be provided by high strength transverse reinforcement. The spacing recommendation for confinement reinforcement from **Comittee 352** appears to be valid for high-strength joints so that it is found that the high-strength concrete grades achieved higher levels of ductility, with better energy absorption and an increased initial stiffness in comparison to identically detailed normal strength for internal, external and knee specimens.
- 3. More experimental tests for RC beam-column connections are needed with specific conditions such as using headed bars or fiber reinforced concrete will be beneficial in the extension of understanding behavior of RC beam-column connections.
- 4. The suggested joint shear behavior model was constructed based on standard Theoretical tests of RC beam-column connection subassemblies. Because the boundary conditions of RC beam-column connections are often different in real RC moment resisting frames (MRF), the effect of boundary conditions on joint shear behavior could be further investigated
- 5. Nonlinearity due to concrete spalling and reinforcement buckling has not been taken into account in the present analysis ,hence it is needed further study.
- 6. More experimental tests is required to take into account the different section geometry of columns beams ,it is suggested that circular columns is to may be taken in beam-column connections at the future investigation

810

L. K	. Idriss	et al.,	Static	behaviour	• of different	types of	R.C bea	ım-column	connections	as affected	by both
valu	e acting	latera	l horiz	ontal force	e and grade	of used c	oncrete (i	theoretical	study) part t	wo, pp.746 -	814.

11. Notation	
$A_{ m h}$	Gross area of cross section of beam
A_{bs}	Area of the other beam reinforcement
A_{a}, A_{c}	Gross area of cross section of column
A_{cs}^{g}	Area of the column reinforcement
A;	Horizontal sectional area of joint core
A_{ih}	Total cross-sectional area of horizontal joint transverse
JII	reinforcement
A_{s1}, A_{s2}	Top and bottom reinforcements of beam respectively
$A_{\rm st}$ 32	Area of longitudinal reinforcement
A *	Greater of the area of top or bottom beam reinforcement
Λ_{s}	passing through the joint
$\mathbf{b}_{\mathrm{b}}, \mathbf{b}_{\mathrm{c}}$	Width of beam, width of column
bi	Effective width of joint
$d_{c} d_{b}$	Effective depth of beam, effective depth of column
D_i	Effective joint depth
$(_{d}d_{d})$	Diameter of longitudinal reinforcing bar
E.A	Energy absorption
E_c	The concrete static modulus
Es	The steel elastic modulus
E_0	The plastic strain
$\dot{f}_{ m 'c}$, $\dot{f}_{ m c}$, $f_{ m cd}$	Compressive cylinder strength of concrete
f_y	Yield strength of steel reinforcement
f_{jy}	Yield stress of horizontal joint transverse reinforcement
$f_{ m by}$	Yield stress of longitudinal beam reinforcement
Н	The total height of the columns above and below the joint
h_c, h_{col}	Depth of column
\mathbf{h}_{j}	Effective depth of joint
J	Range of mode strength
k	Averaged bond strength in beam-column joint
L_b, L	Length of the beam right and left the joint
L _c	The heights of the columns above and below the joint
N_{c}	Axial column loads
V_b	Beam shear force
V_c	Column shear force
$V_{ m j}$	Joint shear stress
v_{jh}	Nominal shear stress
γ	Nominal strength coefficient
Ŷaci	Joint shear strength factor
φ	Reduction factor for effect of plane geometry
η	De notes the reduction factor on concrete compressive strength
2	due to tensile strains in transverse direction
δ_h	Lateral top displacement

Journal of Engineering Sciences, Assiut University, Faculty of Engineering, Vol. 41, No. 3, May, 2013, E-mail address: jes@aun.edu.eg

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814

ε ₁	Principal axial strains
θ	Story drift %
$\mu_{\rm B}$	Joint bond stress
γ	Joint shear strain distortion,
$\sigma_{\rm B}$	Concrete compressive strength
σ_{o}, σ_{col}	Column axial stress
σ_{c}	Concrete stress block
$\tau_{\mathrm{J}},\tau_{iu}$	Joint shear stress
σ_1	principle axial stress
$\tau_{\rm J}$	Joint shear stress
ρ_w	Joint shear reinforcement

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" السلوك الاستاتيكي للانواع المختلفة من الوصلات الخرسانية المسلحة بين الكمرةوالعمود تحت تأثير كلا من القوة الافقية العرضية والرتب الخرسانية المستخدمة " دراسة نظرية

الملخص:

تم في هذا البحث عمل دراسة نظرية لمجموعة نماذج مقترحة ثلاثية الأبعاد من مناطق إتصال الكمرات بالأعمدة الداخلية والخارجية والركنية باستخدام برنامج كمبيوتر للتحليل الإنشائي ABAQUS\CAE 6.7 لدارسة العوامل المؤثرة على السلوك الاستاتيكي لهذه الوصلات تحت تأثير القوة الافقية العرضية ومن أهمها رتبة الخرسانة المسلحة ونسبة حديد التسليح الرئيسي والثانوي والحمل المحوري ومساحة منطقة الإتصال و كذلك حالة النهايات الطرفية لمنطقة الإتصال تم التحميل عند قمة العمود بحمل رأسي محوري للعمود بنسبة ثابتة من مساحة مقطعة ورتبة الخرسانة ماتحميل عند قمة العمود بحمل رأسي محوري للعمود بنسبة ثابتة من مساحة مقطعة ورتبة الخرسانة 0.15AcFc مصحوب بقوة قص أفقية متغيرة VC)تم تقييم كلا من إجهادات القص وإجهادات التماسك بين حديد التسليح والخرسانة وكذلك التشكلات الناتجة في منطقة إتصال الكمرات بالأعمدة بالإضافة إلى كمية الطاقة الممتصة وحالة الأنهيار المتوقعة. ولدراسة سلوك هذه الوصلات ومقارنة النتائج النظرية تم دراسة 48 عينة لمناطق أتصال الكمرات بالأعمده الخرسانية والخارجية والركنية حيث تم تثبيت البيانات التالية:

مساحة مقطع الكمرة (Ac) (Ac) مساحة مقطع العمود (bbxdb) mm (250×300) mm, (Ab) مساحة مقطع العمود (Ac) (bbxdb) mm (250×300) mm مساحة منطقة الاتصال الكمرة بالعمود (HxL) m (2.0×3.0) m, (Aj) مساحة حديد تسليح العمود (As1) m (2.0×3.0) m (Aj) مساحة حديد تسليح الكمرات علوي و سفلي (As1) 4 Φ 16 (As1), حديد تسليح الكمرات علوي و سفلي (As1) 6 Φ 16 (As1) ونسبة توزيع الكانات Φ 6 (As1) وكذلك حالة النهايات الطرفية لمنطقة الاتصال الكمرات ولأعمدة مع ثبوت سمك البلاطة الاتصال الكمرات علومات (As2) ونسبة توزيع الكانات Φ 16 (As1) وكذلك حالة النهايات الطرفية لمنطقة الاتصال الكمرات ولأعمدة مع ثبوت سمك البلاطة ts = 120mm

المحالي في عير على (المحالي عنه) المحالي المحالي المحالي المحالي المحالي المحالي المحالي المحالي المحالي المحال (الأعمدة على سلوك منطقة الاتصال بين (الأعمدة والكمرات) الخرسانية والتحليل المرن اللدن لجميع الهياكل الخرسانية المسلحة واختبار السعة القصية لاحمال الزلازل بالتحليل الغير خطى الديناميكي لبرنامج ABAQUS .

تم عرض وتحليل للنتائج النظرية المتحصل عليها من وجهات النظر الاتية :

الاجهادات والمقاومات لمناطق اتصال الكمرات بالاعمدة الداخلية والخارجية والركنية وهي. مقاومة القص (τJ) ;اجهادات التماسك بين الحديد والخرسانة (μb):والتشكلات والانفعالات المختلفة لمناطق اتصالات الكمرات بالاعمدة الداخلية و الخارجية و الركنية; الطاقة الكلية الممتصة (E.A)و اخيرا حالات الانهيار المختلفة للوصلات الخرسانية (انهيار في قوة التماسك بين الحديد والخرسانة (B),انهيار قصي في منطقة الاتصال(J) والانهيار في المفصلة اللدنة للكمرات (JB)

L. K. Idriss et al., Static behaviour of different types of R.C beam-column connections as affected by both value acting lateral horizontal force and grade of used concrete (theoretical study) part two, pp.746 - 814.

التوصيات:

1-لزيادة قدرة و سعة تحمل الوصلات و لتطوير انهيار مناطق الاتصال الكمرات بالأعمدة بأن تكون أكثر لدونة للكمرات فانه يوصي بزيادة سعة عزم الانحناء لمناطق الاتصال نسبة الى عزم الانحناء عند نهاية الكمرات بزيادة نسبة الحديد لطولي في منطقة اتصال الكمرات بالأعمدة.
2-استخدام خرسانة عالية المقاومة في الأعمدة في مناطق الاتصال تحتاج الي حديد تحزيم للتأكد من لدونة للكمرات بزيادة نسبة الحديد لطولي في منطقة اتصال الكمرات بالأعمدة.
2-استخدام خرسانة عالية المقاومة في الأعمدة في مناطق الاتصال تحتاج الي حديد تحزيم للتأكد من لدونة السلوك الذي يمكن ان يتطور باستخدام حديد ثانوي عالي المقاومة مع مراعاة المسافة للحديد التحزيم لاعطاء الدونة عالية وزيادة في الطاقة المعتصة مع متانة عالية بالمقارنة باستخدام مقاومة مع مراعاة المسافة للحديد التحزيم لاعطاء الدونة عالية وزيادة في الطاقة المعتصة مع متانة عالية بالمقارنة باستخدام مقاومة عادية لمناطق الاتصال الخريف وراحية الحياي العماع العربي العطاء الحديد الخولي لاعطاء الحديد الحولي في منطقة المقاومة مع مراعاة المسافة للحديد التحزيم لاعطاء الدونة عالية وزيادة في الطاقة المعتصة مع متانة عالية بالمقارنة باستخدام مقاومة عادية لمناطق الاتصال لدونة عالية وزيادة في الطاقة المعتصة مع متانة عالية بالمقارنة باستخدام مقاومة عادية لمناطق الاتصال الدونة عالية والخارجية والركنية.

داخلي أو حرسات مستعة دات أي عدر الله سوف معاطى الولعارك الحرسانية المستعة. 4- سلوك الوصلات القصي يعتمد على الدراسات النظرية القياسية لمناطق الأتصال الكمرات بالأعمدة الخرسانية المسلحة بسبب النهايات الطرفية لمناطق الاتصال فيجب دراسة تأثير تغيير النهايات الطرفية لمناطق الاتصال.

5-الاخذ في الاعتبار التحليل الغير خطي عند تقشير الخرسانة وحدوث انحناءحيث ان ذلك غير مأخوذ في الحسابات الخاصة بالبحث.

6- بعض الدراسات الأخرى مع الاخذ في الاعتبار اختلاف شكل قطاعات الاعمدة عند الوصلات اي القطاعات الدائرية للأعمدة يجب دراستها