

STRENGTHENING OF SKYLIGHT COLUMNS OF BUILDINGS TO RESIST EARTHQUAKE USING BRACING

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ABSTRACT

This research presents an investigation through a numerical study on the effect of bracing for skylights columns in multi story building. Variable parameters were taken into consideration such as number of bracing, stiffness of columns, beam cross –section. Base shear force of the building, top displacement, story drift as well as bending moment and shear force on columns were estimated under seismic loads, and the obtained results were studied and discussed. In this case of study, number of stories was taken fifteen, total plan dimensions was $20 \times 35 \text{ m}^2$ with (4×5) m bay dimensions. The commercial computer program ETABS was used in the analysis. The results showed that skylight columns bracing has a significant impact on base shear force, top displacements, story drift as well as bending moment and shear force on columns for the different parameters taken into consideration.

Keywords: Seismic designs, strengthening of multistory building, retrofit systems, strength and stiffness.

1. Introduction

Occurrences of recent earthquakes in different parts of the world and the resulting losses, especially human lives, have highlighted the structural inadequacy of buildings to carry seismic loads. There is an urgent need for strengthening existing buildings in terms of seismic performance. Since October 1992, a set of Egyptian codes have been released to prevent building collapse and control major damages of structural elements.

These buildings were not well designed to resist seismic loading [9].

Braced frames reduce lateral displacement, as well as the bending moment in columns, they are economical, easily erected and have the design flexibility to create the strength and stiffness required [15]. It helps make buildings sturdier and more likely to withstand lateral forces. Bracing can be used in strengthening most all types of concrete, masonry or steel–framed buildings. Moreover it can be also used when a tall building is subjected to lateral or torsional deflections under the action of fluctuating wind loads and the

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earthquake. Bracing is considered as available dead load of structure that can be mobilized to resist overturning uplift [6]. However, this method of strengthening was usually used in steel construction, and rarely in concrete structures. Moreover, the bracing cross-section was mostly from steel. Few previous works on using bracing in concrete structures are available. Therefore this study was made to investigate the effect of strengthening for RC buildings using bracing with reinforced concrete cross-section.

The purpose of strengthening methods is to ensure that the displacement demand of a building is to be kept below its displacement capacity [14]. There are many retrofit systems developed for RC buildings. One of these methods for the strengthening of buildings is system based strengthening [12]. In the system based strengthening methods, a structural system is modified by adding members such as reinforced concrete shear walls, [10] infill shear walls, external shear walls, adding walls to existing columns, encasing columns and steel bracing [8],[11]. Infill Strengthening, mainly improves the strength and stiffness characteristics of the system [2]. The seismic Performances of R.C building with and Without Influence of Steel Bracing were studied by Naveen et al [13]. It was found that increasing number of storey with bracings increase the stiffness and control drifts and displacement. Results showed that the reinforced concrete building with steel bracing system performs better than any other normal building under severe earthquake zones. While the bracings decrease the bending moments and shear forces in columns, they increase the axial compression in the columns to which they are connected. The bracings are provided with the steel members and are diagonally connected in the form of X at the location [7]. There is a significant reduction in the seismic vulnerability of the building after retrofitting of building with steel bracing. Seismic Retrofit of Reinforced Concrete Frame Buildings with Hysteretic Bracing Systems, controls the maximum interstorey drifts, imposes a maximum top displacement as function of the seismic demand and, if needed, regularizes the stiffness and strength of the building along its elevation [1].

The purpose of this study is to try to clarify the effect of strengthening skylights columns of RC buildings for earthquake resistance using R.C bracing. Fifteen story reinforced concrete building was designed under seismic loads, then the obtained results were analysed and discussed. The equivalent static load has been used in this study .The main objective is to assess the total base shear, top displacements and drift between stories.

2. Building description and design

The studied case is a fifteen stories reinforced concrete building. The plan dimension is 20.0 meter by 35.0 meter with a typical bay 4.0×5.0 m. The configurations of the building plan and elevation views are shown in Fig (1) to (4). The total height of the building from the ground level is 46 m, the typical story height is 3.0 m except the first story, which has a height of 4 m. The dimensions of the columns are 40cm x160cm with 20\phi20 longitudinal reinforcement and 6\phi8/m' as stirrups. The building structural elements have been first analysed and designed according to Egyptian code of practice (ECP 203-2007)[5]. The materials used in the design are C300 for concrete and St52 for steel (characteristic yield strength for steel of 3600 kg/cm²). Rectangular columns were used with different plan orientation to represent the change in lateral rigidity. Also, a different beams and slab cross-sections were used to represent the rigid diaphragm effect. These sections have been checked under seismic actions by using the Egyptian code for load and forces (ECLF 2012) [4]. The model is assumed to be a residential building with maximum live load of

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250 kg/m². ETABS 2015 analysis program automatically estimates the own weight of the structural elements and include it in the elastic and inelastic analysis [3]. Because of symmetry in both directions, the torsional effect has not taken into consideration at this case of modelling.

3. Finite element model

A three-dimensional mathematical model of the physical structure will be used to represent the spatial distribution of the mass and stiffness of the structure. A multi-storey building model of a hypothetical reinforced concrete building has been analyzed using ETABS 2015 structural analysis software package. The building is modeled as 3D building structure using building elements for columns, longitudinal beams and transverse beams and shell element for slabs with rigid floor diaphragms to distribute uniformly the lateral loads on the vertical elements.

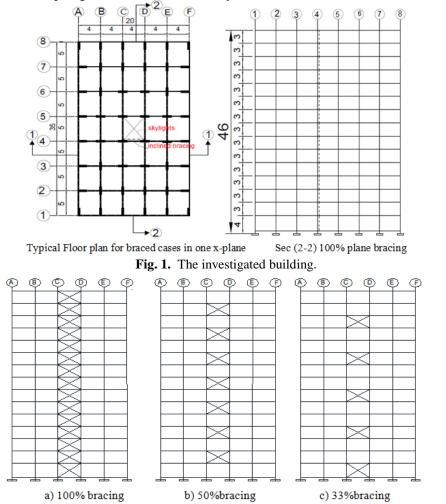
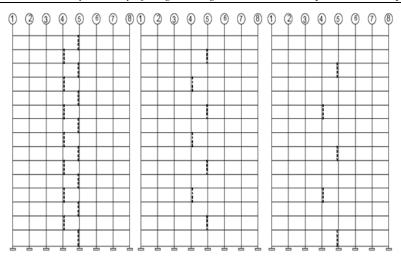


Fig. 2. SEC (1-1) [the shape of plan bracing (x- inclined) used for strengthening in building].



a) 100% bracing b) 50% bracing c) 33% bracing **Fig. 3.** SEC (2-2) [the shape of staggered bay bracing (x-inclined) used for strengthening in building].

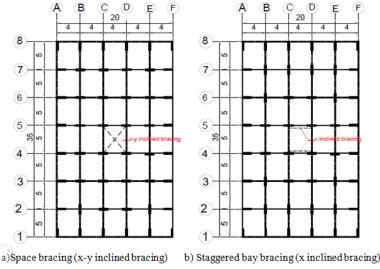


Fig. 4. The plan of bracing in building.

4. Seismic analysis procedures

The equivalent static lateral force method (ESL) has been used. According to ECP-201 (2012), the seismic base shear force, F_b for each horizontal direction in which the building is analyzed, shall be determined using the following expression:

$$F_b = S_d \left(T_1 \right) \times \lambda \times W / g \tag{1}$$

Where: S_d (T_1) is the ordinate of the design spectrum at period T_I ; T_1 is the fundamental period of vibration of the building for lateral motion in the direction considered; W is the total weight of the building, above the foundation level; g is the gravity acceleration ; λ is the effective modal mass correction factor, the value of which is equal to: $\lambda = 0.85$ for $T \le 2 T_C$, and n > 2 stories, $\lambda = 1.0$ for $T \ge 2 T_C$, where n number of stories; T_c is the upper limit of the period of the constant spectral acceleration branch as shown in Fig (5).

The value of Fundamental period of vibration of the building in the direction of the analysis is determined using the following expression:-

$$T = C_t \times H^{3/4} \tag{2}$$

Where C_t is a factor determined according to the structural system and building material and was taken equal to 0.050; *H* is the height of the building (*m*); from the foundation or from the top of a rigid basement. The ordinate of the design spectrum, S_d (T_1), can be determinate from:-

$$s_d(T) = \frac{2.5}{R} \times a_g \times \gamma \times S\left[\frac{T_c}{T}\right] \ge [0.2] \times a_g \times \gamma \tag{3}$$

Where a_g is the design ground acceleration for the reference return period; *S* is the soil factor. γ : Importance factor (for ordinary buildings $\gamma = 1$, as it was taken in the present study). The seismic zone considered in this study is zone 3. *R* is the reduction factor according the statical system of the structure(R = 5). η :Design damping factor for elastic response spectrum (In case of reinforced concrete $\eta = 1$,

 T_B , T_C : Constant value limits of elastic response spectrum

 T_D : limited value for the starting of fixed spectrum movement.

In the present study, the Elastic response spectrum curve type one is considered (this type is used for all republic areas) and soil classification is assumed to be medium soil class "C"

So, S = 1.5, $T_B = 0.1$, $T_C = 0.25$, $T_D = 1.2$

It should be noted that, ECLF 2012 recommends that in the application of the ESFM method, the building should meet the criteria for regularity in both plan and elevation, and with calculated structural period T not greater than 2 sec or 4Tc (1 sec for the selected soil class (class "C"). The total base shear, F_b , shall be determined by applying horizontal forces F_i to each story mass m_i and shall be distributed as follows:-

$$F_{i} = \left[\frac{z_{i} \times W_{i}}{\sum_{j=1}^{n} z_{j} \times W_{j}}\right] \times F_{b}$$

$$\tag{4}$$

Where F_i is the horizontal force acting on story *i*; F_b is the seismic base shear force (Eq. [1]); z_i , z_j are the heights of the masses m_i , m_j above the foundation level respectively; W_i , W_i are the weights of masses m_i , m_j ; *n* is the number of stories above foundation level.

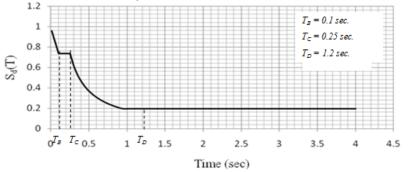


Fig. 5. Design response spectrum for all regions of Egypt except coastal areas.

5. Results and discussions

Twenty one different models, 15-story building, given in 5 groups A,B,C,D,E, in table 1 and table 2, have been studied to evaluate the effect of the bracing on the value of the induced base shear and the resulted displacement as well as story drift. In all groups the beam and bracing cross-section are constant (25×50), columns cross-section is constant (40×160), thickness of slab is constant (15cm) and area of skylights is constant (4×5), except group E the beam cross-section is variable and the area of skylight is (4×15).

5.1. Effect of the ratio of the braced stories

In groups A, B, C, the main parameter was the ratio of the braced stories for different cases. The obtained results showed that, with increasing the percentage of braced stories, the ratio (δ/δ all) and maximum story drift decreased and this is shown in Fig (6). Fig (7) shows that, when using staggered bay bracing, on two axes (Model B 4, 5, 6) the ratio of $(\delta/\delta \text{ all})$ as well as story drift decreased compared with that of plane bracing. This decrease increased with increasing the bracing ratio. The percentage of story drift will decrease by 36.9% when using staggered bay bracing 200% compared with the model without bracing. The using of staggered bay bracing 200% seems to have small effect compared with the using of staggered bay bracing 100%. The percentage of story drift will decrease by 3.4% when using staggered bay bracing 200% compared with the model using staggered bay bracing 100%. The maximum efficiency occurred when using staggered bay bracing 100% as shown in Model B6. The percentage of story drift decreased by 19.4% when increasing in the ratio of (x-inclined) plan bracing, but when using (x-y inclined) space bracing, story drift decreased by 23.3% compared with the model without bracing. The percentage of decrease in maximum story drift will increase with increasing in the number of bracing stories. Maximum percentage of decrease in maximum story drift will get it from using staggered bay bracing 200% in area of skylights. From Fig (8) shows that, with increasing in the number of braced stories in two axis x- bay direction, the maximum story drift and maximum displacement decreased. It shall be noted that, when using staggered bay bracing 100% with increasing in the number of braced stories, the maximum story drift and maximum displacement will be decreased. Fig (9) shows that, with increasing in the number of braced stories in one x- bay direction, the maximum story drift and maximum displacement decreased. From Fig (10) it is clear that the effect of space bracing, (three dimensional) is slightly more effective than the plane bracing, especially in the upper stories of the building. Fig (11) shows that, the using of staggered on two bay bracing decreased both the ratio (δ / δ all) and the ratio ($\delta r / \delta r$ all), It can change the unsafe values of the ratio (δ / δ all) and the ratio ($\delta r / \delta r$ all) to be within the allowed limit.

Du	bunding with bracing for various columns righting groups.												
Groups	Models	n _x	ny	Bracing Type	Percentage of Braced Stories	ð (cm)	$\delta /\delta_{\rm all}$	ðr (cm)	$\delta \mathbf{r} / \delta \mathbf{r}_{\mathrm{all}}$	Max column Shear (Ton)	Max column Moment (Ton .m)	% decrease in &r	
А	M _{A0}	24	24			11.8	1.28	1.0542	1.230	17.36	142.46		
	M _{A1}	24	24	Р	33%	10.8	1.17	0.9537	1.113	17.36	115.75	9.5%	
	M _{A2}	24	24	Р	50%	10.7	1.16	0.9297	1.085	17.3	118.1	11.8%	
	M _{A3}	24	24	Р	100%	10.5	1.14	0.9123	1.065	14.52	110.6	13.5%	
В	M_{B0}	30	18	_		10.74	1.17	0.9504	1.109	15.09	121.7		
	M_{B1}	30	18	Р	33%	9.8	1.07	0.855	0.998	15.6	98.13	10.0%	
	M_{B2}	30	18	Р	50%	9.7	1.05	0.8397	0.980	15.7	99.6	11.6%	
	M _{B3}	30	18	Р	100%	9.6	1.04	0.825	0.963	12.42	93.12	13.2%	
	M _{B4}	30	18	SP	33%	8.55	0.93	0.7554	0.881	15.32	94.64	20.5%	
	M_{B5}	30	18	SP	50%	8.15	0.886	0.69	0.805	15.37	96.89	27.4%	
	M _{B6}	30	18	SP	100%	7.7	0.84	0.6321	0.738	11.95	84.32	33.5%	
	M_{B7}	30	18	SP	200%	7.4	0.81	0.5994	0.699	11.1	77.36	36.9%	
C	M _{C0}	34	14			10.26	1.12	0.9072	1.059	14.29	112.83		
	M _{C1}	34	14	Р	33%	8.8	0.96	0.7572	0.884	14.48	90.24	16.5%	
	M _{C2}	34	14	Р	50%	8.7	0.95	0.7437	0.868	14.57	91.7	18.0%	
	M _{C3}	34	14	Р	100%	8.6	0.94	0.7308	0.853	11.4	86.54	19.4%	
D	M _{D1}	34	14	S	100%	8.2	0.89	0.696	0.812	12.01	90.55	23.3%	

Table 1.

Building with bracing for various columns rigidity groups.

Where that:-

 \mathbf{n}_x , \mathbf{n}_y : Number of columns oriented in x and y direction respectively .

 $\boldsymbol{\delta} :$ Maximum top displacement for the building .

δr: Maximum story drift for building.

 δ_{all} : The maximum safe displacement for building given by the code =H /500=9.2

 δr_{all} : The maximum safe story drift for building given by the code.

H : The building height above the foundation level .

Percentage of Braced Stories (-): no bracing in building.

(33%): bracing each three stories in x –bay 4-4 of the skylight.

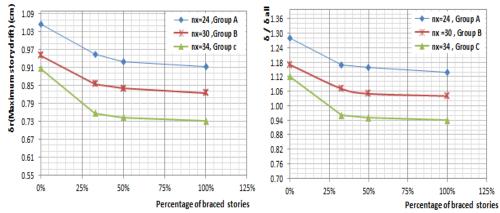
(50%): bracing each two stories in x –bay 4-4 of the skylight.

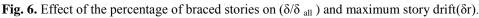
(100%): bracing in all stories in x –bay 4-4 of the skylight.

P: plane bracing i.e. inclined bracing in x-direction.

S: space bracing i.e. inclined bracing in x-y direction.

SP: staggered bay bracing in x-bay axis 4-4&5-5 of the skylight.





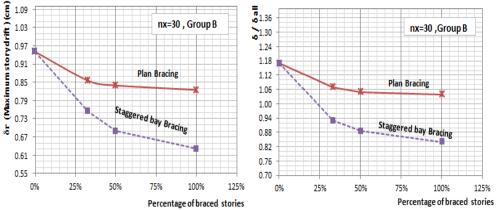


Fig. 7. Effect of the staggered bay bracing (x- inclined) on (δ/δ_{all}) and maximum story drift(δr).

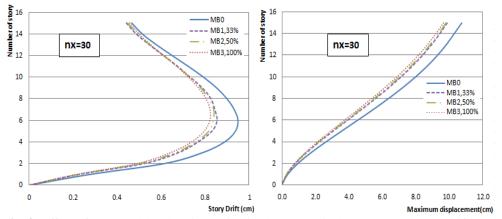
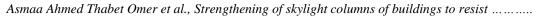


Fig. 8. Effect of staggered bay bracing (x-inclined) on top displacements and story drift models.



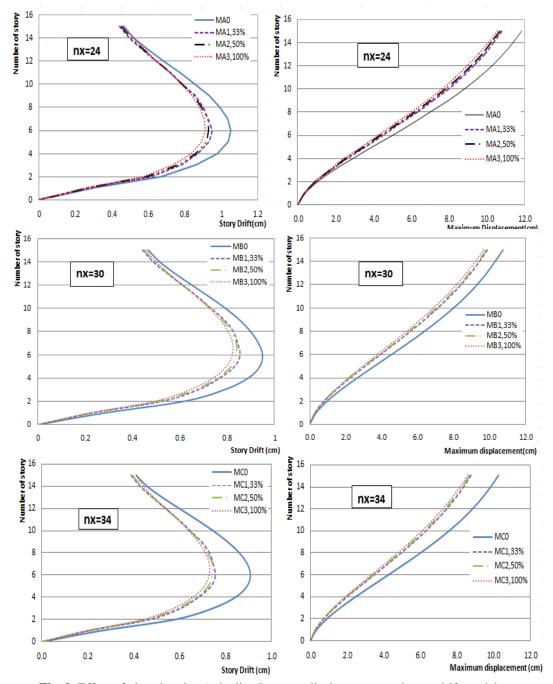


Fig. 9. Effect of plane bracing (x-inclined) on top displacements and story drift models

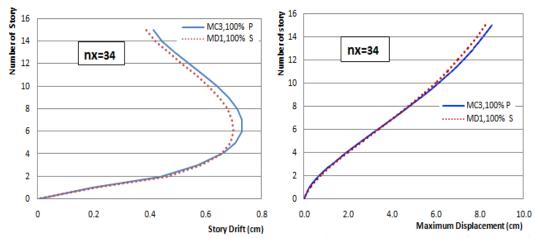
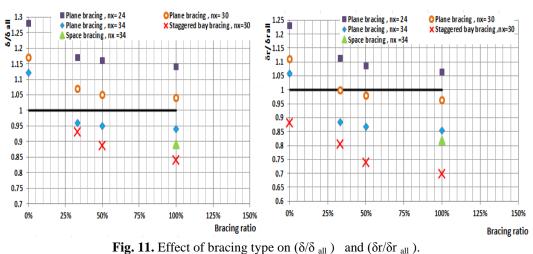


Fig. 10.Effect of space bracing(x-y inclined) of full bracing on top displacement and story drift models



5.2. Effect of Bracing for various column rigidities

In all models the total number of columns was 48. In group A (M_{A1} , M_{A2} , M_{A3}) with variable x bay bracing ratio, the number of columns oriented in x direction was 24. In group B (M_{B1} , M_{B2} , M_{B3}) with variable x bay bracing ratio, the number of columns oriented in x direction was 30. In groups C (M_{C1} , M_{C2} , M_{C3}), D (M_{D1}) with variable x bay bracing ratio, the number of columns oriented in x direction was 34. Model M_{A0} , M_{B0} , M_{C0} , were taken without any bracing. In M_{D1} had space bracing with inclined in x-y plane to the horizontal in all stories. The obtained test results are included in Table 1. From this table it can be seen that the presence of bracing in general reduces each of the maximum induced shear, maximum moment, the top displacement and the maximum story drift. The effect of bracing seems to be increased with increasing the stiffness of columns in the load direction Fig (12). The total base shear and bending moment for columns decreased when using bracing in all stories with increasing in the columns rigidity in the load direction as shown in Model C3.

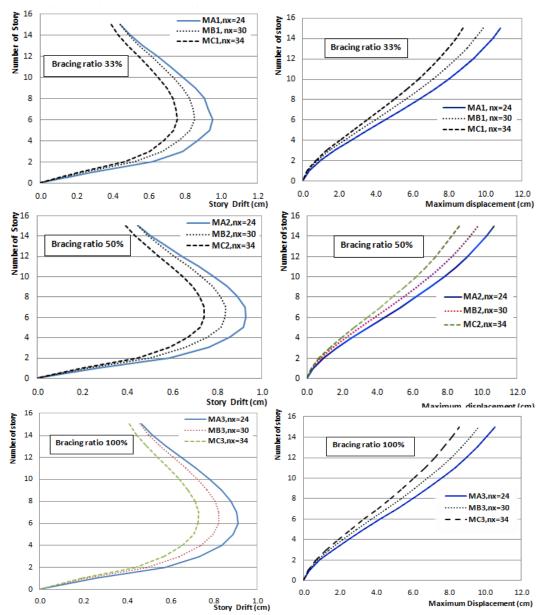


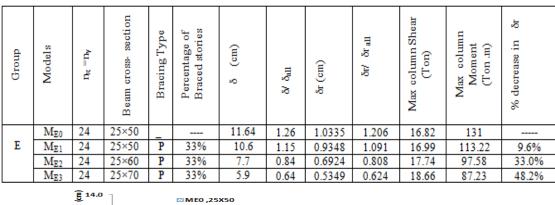
Fig. 12. Effect of bracing of various columns rigidity on top displacements and story drift models

5.3. Effect of bracing for different beam cross- section

In group E the main parameter was the beam –cross-section for x braced ratio 33% and the area of skylight used in this group is (4×15). The beam cross –section used in the M_{E0} , M_{E1} is 25×50, in the M_{E2} is 25×60 and in the M_{E3} is 25×70. Model E_0 was taken without any bracing. From Fig (13) it can be noted that, when using 33% bracing ratio with increasing of the beam cross-section, the top displacement and maximum story drift decreased. The rate of decrease was larger as the beam dimension increased. The percentage of the reduction in story drift for Model M_{E3} compared with that of the un braced Model M_{E0} was 48.2%. The minimum bending moment occurred when using 33% bracing ratio with increase in beam cross –section.

Table 2.

Building with 33% bracing ratio for various beam cross-section group



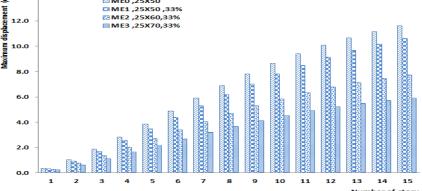
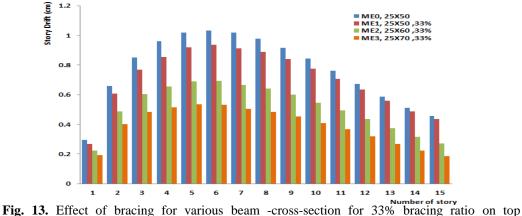


Fig. 13. Effect of bracing for various beam -cross-section for 33% bracing ratio on top displacements and story drifts model and contain.



displacements and story drifts model.

6. Summary and conclusion

In this study R.C bracing had been used to strengthen skylight columns of RC buildings for earthquake resistance. The analysis was done by equivalent static load (ESL), which was adopted on the Egyptian code for load and forces (ECLF2012). The main findings of the study can be summarized as follows:

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- The R.C bracing system with various columns rigidities in the load direction significantly reduced the top displacements, story drift as well as bending moment and shear force on columns. Using the R.C bracing bring the unsafe values of top displacement and story drift to be within the allowed values.
- The influence of bracing decreased as the ratio of braced stories decreased.
- The staggered plane bracing on two axes was more effective than the bracing in one axis for the same bracing ratio.
- The effect of bracing with increasing beam cross-section gives almost large decrease in top displacement, maximum story drift, maximum moment and maximum shear.

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"تقوية أعمدة المناور في المباني لمقاومة الزلازل بأستخدام الشكلات"

الملخص العربى

وفي يوم الاثنين 12 أكتوبر 1992، ضرب زلزال قوي مصر في منطقة لم يكن لها نشاط زلزالي في الآونة الأخيرة. إلا أن زلزال عام 1992 قد ترك أعمق الصور على الجميع، ليس فقط لأنه أسفر عن مقتل وجرح المئات، بل أيضا لأنه تكبد خسارة اقتصادية تقدر بحوالي مليار ولم تكن هذه المبانى مصمما بشكل جيد لمقاومة التحميل الزلزالي . في هذا البحث تم دراسة تقوية المباني لمقاومة الزلزل بربط أعمدة المناور بأستخدام (Bracing) الشكلات ، حيث تم إجراء التحليل الزلزالي بطريقة الحمل الأستاتيكى المكافئ لمبني بأستخدام (Bracing) الشكلات ، حيث تم إجراء التحليل الزلزالي بطريقة الحمل الأستاتيكى المكافئ لمبني خرساني مستطيل الشكل مكون من (15) دور . تم دراسة هذا المبني قبل وبعد التقوية (Bracing) بالشكلات بأستخدام (Bracing) الشكلات ، حيث تم إجراء التحليل الزلزالي بطريقة الحمل الأستاتيكى المكافئ لمبني فرساني مستطيل الشكل مكون من (15) دور . تم دراسة هذا المبني قبل وبعد التقوية (Bracing) بالشكلات خرساني مستطيل الشكل مكون من (15) دور . تم دراسة هذا المبني قبل وبعد التقوية (Bracing) بالشكلات فرساني مستطيل الشكل مكون من (21) دور . تم دراسة هذا المبني قبل وبعد التقوية (Bracing) بالشكلات فرساني مستطيل الشاط ون وزالي على السلوك خرساني ومتطلبات القص وتوزيع قوي القص على كل الطوابق وأيضا أزاحة الذروة العلوية للمنشأ وانجراف وانجرافات الطوابق والازاحة الكلية للمبني مع أستخدام الشكلات و التغير في عدها وأيضا عند التغير في قطاع وانجراف الفوابق والازاحة الكلية للمبني مع أستخدام الشكلات والتغير في مصاحة المنور ، والتغير في قطاع وانم الطوابق والازاحة الكلية للمبني ما لمحدة والمكلات والتغير في مساحة المنور ، والتغير في قطاع وانمكلاتوذلك عند التغير في مطاع وانمي والقوابق والازاحة الكلية المبني ما يراحما الشكلات والتغير في مساحة المنور ، والتغير في قطاع والمكلاتوزاك عاروني في في محمدها وأيضا عند التغير في قطاع وانم والوابق والازاحة الكلية المبني ما والموابق وأقل قيم للازاحة الكلية للمبني سوف يتم الحمول الشكلاتوذلك عند التغير في مطاع وألمكلات وأقل قيم للازاحة الكلية المبني مو سكا المكلات وألف ما زيادة صاكلية المبني ما ملوبي ما وألف ما زيادة مالماني رالفو القيم الموابق وأقل قيم للازاحة الكلية المبني ما محمول الشكلاتوذلك عند التغير في الحموا ما مي الطوابق وأقل قيم اللازاحة الكلية الممب