# Performance of solar dish Stirling engine systems under Egyptian operating conditions

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#### Abstract

Egypt's demand for electricity is rapidly growing, and it is becoming more urgent to develop alternative power resources to meet its own energy needs. Over recent years, development of renewable energy has become a priority for Egypt. Due to its geographical location and climate, Egypt has an average level of solar radiation between 2,000 to 3,200 kWh/m<sup>2</sup> per year. As a result, Egypt has a significant potential for the development of solar energy application. The solar dish Stirling (DS) system performance is dependent on the solar data of the location. Several studies investigated the performance of the system in different locations around the world. The objective of this study is to develop a comprehensive simulation model for the solar dish Stirling engine system. The model is used to investigate the system performance under Egyptian operating conditions. The results of 21 different zones that cover most of the Egyptian regions are calculated and compared to determine the overall performance of the system and to determine the suitable locations for project development. Results showed a yearly average power output from the simulated 6.6 m aperture diameter system that ranges from 5800W in El-Natroon area to 7100W in Aswan. A comparison between the simulated DS system model and an equivalent PV system shows that the DS system requires 37.6% less land to generate the same amount of power. Moreover, the DS system gives higher overall system efficiency than the equivalent PV system considering the shading that affects the area of land needed for the system. The results show that using the dish Stirling engine (DS) systems in Egypt will result in acceptable performance in terms of power output and efficiency.

#### **Keywords**

Solar dish Stirling engine systems, Solar energy, Concentrated solar power, CSP, Energy, Simulation, Stirling engine, Performance investigation.

# Nomenclature

		$\theta$	Crank angle (Radians)		
List o	of symbols		-		
А	Area (m)	$ heta_i$	Incident angle (Radians)		
$c_p$	Specific heat at constant pressure (J/kg.K)	$ ho_{con}$	Concentrator reflectance		
$C_{\rm V}$	Specific heat at constant Volume (J/kg.K)	σ	Stefan Boltzmann's constant		
d	Derivative with respect to crank	τ	Transmittance		
DNI	Direct normal irradiance $(W/m^2)$	(Omen	Capture fraction		
E	Unshaded concentrator fraction	Ψrec			
-		List of suffixes			
h	Convective coefficient (W/m <sup>2</sup> .K)	amb	Ambient		
k	Thermal conductivity (W/m.K)	ap	Receiver aperture		
L	Thickness of insulation (m)	c	Compression space		
'n	Mass flow rate (kg/s)	cav	Receiver cavity		
Μ	Total mass of working gas (kg)	con	Concentrator		
р	Pressure (Pa)	cond	Conduction		
Q	Heat energy (J)	conv	Convection		
Q	Heat rate (W)	e	Expansion space		
R	Gas constant (J/mol.K)	forced	Forced convection		
$\mathbf{R}_{\mathrm{th}}$	Thermal resistance	h	Heater		
Т	Temperature (K)	int	Intercepted		
V	Volume (m <sup>3</sup> )	k	Cooler		
W	Work (J)	loss	Losses		
List o	of Greek symbols				
α	Phase angle advance (Radians)	natura 1	Natural convection		
$\alpha_{eff}$	Effective absorptance	r	Regenerator		
$\alpha_{rec}$	Receiver absorptance	rad	Radiation		
8	Effectiveness	rec	Receiver		
E <sub>cav</sub>	Cavity effective emissivity	SW	Swept volume		
ε <sub>r</sub>	Regenerator effectiveness	total	Total convection		
η	Efficiency	W	Wall		
1 Int	raduction				

#### 1. Introduction

Human civilization and standards of living are very dependent on energy, which is needed for lighting, cooking, transportation, communication, production, and many other uses. Without energy, the standards of living will be affected, and civilization will collapse (Johnson, 2018).

Conventional energy sources based on fossil fuel such as coal, oil, and natural gas are badly affecting the environment, human life, and economic progress. Another problem of the mass usage of fossil fuel is the emission of greenhouse gases and the depletion of the energy resources. Those setbacks are enough reasons to use renewable energy sources like wind energy, hydroelectric, biomass, geothermal, tidal, and solar energy. This study focuses on the studying of a solar energy technology named concentrated solar power (CSP) (Akella, Saini, & Sharma, 2009).

CSP technology uses mirrors to reflect and concentrate sunlight into a single point called the focal point where it is collected and converted into heat power. CSP systems are generally used for utility-scale projects. Moreover, there are varieties of CSP systems such as parabolic trough systems, solar power towers, and dish Stirling engine (DS) systems which is the scope of this research (Lovegrove & Stein, 2012). The DS system concentrates the Direct Normal Irradiance (DNI) from the sun to operate a Stirling engine, which in turns drives an electric generator that produces electricity.

A detailed summary of every component in the dish Stirling engine system including the system description, types, numerical models, sizing, and data on existing projects can be found in (William B. Stine and Richard B. Diver, 1994). These models are used to achieve a method for integration of the component models to form a comprehensive model. The thermal, electrical, and control systems of the dish-Stirling system are presented in (Howard & Harley, 2010), along with a method for simulation based on (Urieli & Berchowitz, 1984). Typical results are provided for the instantaneous working gas pressure, torque, and temperature. The results indicated how these parameters vary with solar DNI in steady state. Simulation of a gridconnected dish Stirling solar power plant was published in (Howard, Harley, & Venayagamoorthy, 2010).

(Mancini et al., 2003) reviewed the status of DS systems that are being developed for commercial markets and presented system specifications and reviewed system performance and cost data. (Reinalter et al., 2008) studied the detailed performance of the 10 kW CNRS-Promes EuroDish unit, calculating the thermal losses and performance of every component of the system. (Mancini et al., 2003) Studied the same system but in different locations in India and Italy. (Fraser & Klein, 2008) studied the model of every component individually, and then performed a case study on the overall performance of the system and compared the results with three years of data from the Wilkinson, Goldberg, and Associates, Inc. (WGA) Mod 2-2 system.

(Nepveu, Ferriere, & Bataille, 2009) presented a thermal model of the energy conversion of the  $10kW_{el}$  EuroDish Stirling unit erected at the CNRS-Promes laboratory in Odeillo and made a thermodynamic analysis of the SOLO 161 Stirling engine. (Rogdakis, Antonakos, & Koronaki, 2012) conducted a special thermodynamic analysis of the engine performance of a Solo Stirling Engine V161 cogeneration module installed in Athens. (Bataineh & Taamneh, 2017) investigated the performance of standalone solar Stirling dish system used to electrify rural houses using SAM software.

(Shazly, Hafez, El-Shenawy, & Eteiba, 2014) presented the modeling and simulation for a solar-powered Stirling engine working at low-temperature range using MATLAB. (Mansiri, Sukchai, & Sirisamphanwong, 2014) studied the possibilities of generating electricity by using a small scale solar dish Stirling engine system in Thailand using existing models and validated the results using experimental data. (Praene, Radanielina, & To, 2015) used MATLAB to generate a theoretical model to investigate the energy efficiency variation of the system for eight main sites in Madagascar.

Studying this system requires an in-depth understanding of each of its components. The DS system consists of main components like the solar tracking system, the paraboloid dish concentrator, the solar receiver, the Stirling engine, and the electric generator. The system also has some other components like the control unit and the cooling system.

The solar tracking system is a mechanism that directs the structure of the system towards the sun during operating hours. A detailed review of the different types of tracking mechanisms and the applications for every type can be found in (Racharla & Rajan, 2017).

The solar concentrator is usually a paraboloid dish that concentrates DNI into a focal point. Studying solar concentrators requires the knowledge of the different types of concentrators (Rabl, 1976), their optical (Saša Pavlović, Velimir Stefanović, Darko Vasiljević, & Emina Petrović, 2015), geometrical (Yan, Peng, Cheng, Liu, & Tang, 2017), and thermal analysis (Gholamalizadeh & Chung, 2017b). (Hafez, Soliman, El-Metwally, & Ismail, 2016) studied the effect of solar dish design features and factors such as the material and the shape of the reflector concentrators, solar radiation at the concentrator, the geometry of the concentrator including diameter, aperture area, focal Length of the paraboloid dish, the focal area diameter. Case studies for designing a paraboloid dish concentrator for certain systems can be found in (Gholamalizadeh & Chung, 2017a) and (Alarcón, Hortúa, & G, 2013).

Solar receivers aim to transfer the concentrated DNI to operate the Stirling engine. Receivers have many shapes, types, and applications (Kalogirou, 2004). The most commonly used receiver types in DS systems are cavity receivers and reflux receivers. (Fraser & Klein, 2008) and (Nepveu et al., 2009) studied the receiver geometry, losses, and the effect of the intercept factor on the amount of energy transferred to the Stirling engine. (Beltran, Velazquez, Espericueta, Sauceda, & Perez, 2012) proposed a procedure and a graphical method for designing dish/cavity systems and choosing the best materials and geometry(Reinalter et al., 2008) studied the concentrated solar flux distribution on the absorber material and the effect on its performance. (Karimi, Gheinani, & Madadi Avargani, 2018) studied the thermal performance of solar cavity receivers in a solar paraboloid dish collector using a detailed mathematical model.

Stirling engine is the component that differentiates DS systems from other CSP systems. The Stirling engine aims to convert the heat energy coming from the receiver

into thermal and mechanical power to operate the generator. Stirling engine has different types, configurations, driving mechanisms, and applications (Kongtragool & Wongwises, 2003) and (Egas & Clucas, 2018). Information about different types of thermodynamic and calculation methods can be found in (Wagner, 2008) and (Ahmadi, Ahmadi, & Pourfayaz, 2017). (Berchowitz, 2016) presented a representation of the Stirling cycle process that includes both thermodynamic processes and mechanical dynamics, resulting in a useful guide to the understanding of these machines.

(Urieli & Berchowitz, 1984) published a complete and very reliable model that describes the performance of the Stirling engines, their work is widely used by the researchers in studying the behavior of different Stirling engines. This model consists of ideal isothermal analysis, Ideal adiabatic analysis, and non-ideal analysis of the Stirling engine. (Tlili, Timoumi, & Nasrallah, 2008) also established a model of an irreversible cycle of the Stirling heat engine, using air as the working substance.

(Timoumi, Tlili, & Ben Nasrallah, 2008) studied the performance optimization of Stirling engines, and published a case study on the GPU3 Stirling engines. (Tlili & Musmar, 2013) performed a thermodynamic evaluation of a second order simulation of a Yoke Ross Stirling engine. (A. C. M. Ferreira, Teixeira, Martins, & Nunes, 2014) conducted a study on the thermodynamic analysis using mathematical models based on the ideal adiabatic analysis of (Urieli & Berchowitz, 1984). The author also studied the economic model of the system. (Alexakis, 2013) used advanced CFD methodologies for the performance characterization of solar Stirling engines with complex geometrical topologies.

(Rogdakis et al., 2012) investigated the performance of the SOLO V161 alpha type Stirling engine with experimental data and thermodynamic models. (Çinar, 2007) described and analyzed a variable phase angle alpha-type Stirling engine from the kinematic and thermodynamic point of view using a FORTRAN code. (Alaraby et al., 2018) studied the thermal and mechanical performance of a beta-type Stirling engine using a Stirling engine simulation scheme under MATLAB/SIMULINK.

The electric generator is the component that translates the output power of the Stirling engine into electrical power. A review of the types of electrical generators used in the dish Stirling engine systems can be found in (Mancini et al., 2003).

(Larchet et al., 2017) compared between the Levelized Cost of Electricity (LCOE) of different dish Stirling engine systems and other solar technologies such as Solar PV, parabolic trough systems, and central receiver systems in Morocco. Results showed that the LCOE in terms of \$/MWh of the dish Stirling engine systems is double that of the PV system.

It can be concluded from the reviewed literature that the DS system performance is dependent on the solar properties of the location. Egypt is considered to have good solar properties compared to other regions around the world. The problem is that the current studies do not give enough information about the system performance in Egypt. As a result, there are no current DS projects in Egypt.

The aim of this study is to investigate the performance of the DS systems under Egyptian operating conditions by generating a comprehensive simulation model for the system. The simulation is performed for several zones in Egypt. Finally, the results are analyzed to investigate the performance of the system in Egypt.

The methodology used in this study is covered in the next sections. an overview of the system components is presented in section 2 of this paper. The system component models are discussed in section 3. The simulation strategy and the parameters of the studied system components are presented in section 4. Simulation results are presented in section 5. Finally, the conclusion is presented in section 6.

# 2. System overview

The DS system generally consists of a structure with a solar tracking system that holds a large paraboloid dish which reflects the irradiance coming from the sun into a cavity receiver. The receiver delivers the concentrated sunlight into the Stirling engine. The Stirling engine generates thermal and mechanical power that operate an electric generator to produce electricity. Description of the main system components is presented in this section. Figure 1 shows a diagram of the DS system components.

# 2.1.Solar tracking system

The aim of the tracking system is to allow the DS system to follow the sun throughout the day to collect as much solar energy as possible. Examples of types of tracking systems include Azimuth-elevation tracking systems and polar tracking systems. It is assumed that the angle of incidence is equal to zero for paraboloid dishes, this means that the system has perfect tracking assumption (Shazly et al., 2014).

# 2.2.Paraboloid dish solar concentrator

For the typical DS systems, concentrators are large paraboloid mirrors with a structure and a tracking system to focus the sun rays on the receiver that delivers the concentrated energy to the hot side of the engine. The reflective mirrors are mounted on a paraboloid-shaped structure. The concentrators may consist of a different number of segments of a reflective material, or a reflective sheet stretched on the paraboloid shaped structure. Solar concentrators must have a reasonable weight, durability against moisture, dust, and temperature changes, hardness against deflection and wind load, long lifetime, and must be cost-effective (William B. Stine and Richard B. Diver, 1994).



Figure 1 Solar Dish Stirling engine system components (Hafez et al., 2016)

# 2.3.Receiver

The aim of the Stirling dish receiver is to absorb thermal energy concentrated by the paraboloid dish concentrator and transfer it to the working gas flowing in the Stirling engine. The receiver must accommodate a large thermal input and solar flux with a value of over a thousand times greater than the direct solar radiation from the sun (Fraser & Klein, 2008). The solar receiver used in the dish Stirling engine systems consists of an aperture and an absorber. The aperture is located at the position of the focal point of the concentrator to reduce the convection and radiation losses. Typical theoretical systems have concentration ratios of over 13,000. Typical aperture has a range of diameters ranging from 14 to 20 cm because it has to intercept a large fraction of the concentrated solar energy (Mancini et al., 2003). The intercept factor is one major parameter in the design of the solar receivers. It is the fraction of energy that enters the aperture area from the collector, which is not blocked by the receiver body. Intercept factor usually ranges between 94 and 99 percent (Fraser & Klein, 2008).

Absorbers are typically direct illumination receivers (DIR), although some heat pipe absorbers are available. Volumetric receivers are also used in hybrid dish Stirling systems that use natural gas to supply the solar energy in shady days.

# **2.4.Stirling engine**

The Stirling engine was invented by Robert Stirling in 1816. His intention was to develop an alternative for steam engines because they were not safe because of the risk of the explosion of their boilers. The Stirling engine converts heat into mechanical energy by compression and expansion of a defined quantity of a working gas usually hydrogen, helium, or air between a hot and a cold sink (Urieli & Berchowitz, 1984).

The main mechanical Stirling engine configurations are divided into three main types known as Alpha, Beta, and Gamma arrangements. Alpha-type Stirling engines have two separate cylinders that are connected in series by a heater, regenerator, and cooler. Beta-type and Gamma-type both use displacer-piston arrangements as shown in Figure 2. Gamma-type differs from Beta-type by having the displacer and the piston in an in-line cylinder system, while the Gamma-type uses separate cylinders (A. C. M. Ferreira et al., 2014).



**Figure 2 Stirling engine components** (A. C. Ferreira, Oliveira, Nunes, Martins, & Teixeira, 2014)

Stirling engine has two pistons in different arrangement and a heat exchanger called the regenerator. The spaces between the regenerator and the pistons are called the compression and the expansion spaces. The piston rods are connected to the crankshaft by connecting rods. The expansion space must be maintained at a high temperature while the compression volume must be maintained at a low temperature.

The heater is a heat exchanger that is responsible for the heat transfer from the heat source to the operating fluid throughout a mesh of tubes that absorbs the heat from the receiver to the working gas. The most used configuration for the heater is smooth pipes in a parallel arrangement.

The regenerator is the heat exchanger that distinguishes the Stirling engine from other types of engines. The regenerator usually contains a fine mesh matrix of metal wires. The aim of the matrix is to absorb and release heat from and back to the working gas.

The cooler aims to absorb heat from the working gas adjacent to the compression space and reject the heat absorbed. The most common method of cooling in Stirling engines is water cooling, while air cooling is less common (A. C. M. Ferreira et al., 2014).

The Stirling engine thermodynamic cycle for a two-cylinder Alpha-type Stirling engine is characterized by four different phases: expansion, pre-cooling transfer, compression, and pre-heating transfer as shown in Figure 3 (Urieli & Berchowitz, 1984).



Figure 3 Ideal Stirling cycle (A. C. Ferreira et al., 2014)

# 3. System models

# 3.1.Solar dish concentrator model

There are several parameters affecting the design and modelling of the solar concentrator including the type of the reflective material of the concentrator, diameter of the paraboloid dish concentrator, sizing of the aperture area of the concentrator that affect the sizing of the aperture area of the solar receiver, focal length of the dish, focal point diameter, rim angle, and finally the concentration ratio, which is the most important parameter as it shows the amount of solar energy concentrated to the receiver (Shazly et al., 2014) and (Hafez et al., 2016).

The amount of concentrated energy intercepted by the receiver from the concentrator can be calculated using the term that defines this amount from the fundamental solar collection equation (William B. Stine and Richard B. Diver, 1994).

$$Q_{rec,int} = DNI A_{rec} E \cos \theta_i \rho_{con} \varphi_{rec} \tau \alpha_{rec}$$
(1)

Where  $\tau$  is the transmittance of anything between the concentrator and the receiver, such as window covering of the receiver.

# **3.2.Receiver Model**

Conduction, convection, and radiation are having a large fraction of the total energy losses of the DS system through the receiver. Conduction losses are a small proportion of the total losses and can be controlled by modifying the insulation thickness of the receiver. Natural convection losses contribute about forty 40% of the total receiver losses and is dependent on wind velocity Long-wave length radiation losses form about 60% of the total losses in a DS system and are minimized by increasing the absorptance of the cavity, maximizing the surface area of the cavity, adding a transparent glass window aperture cover, or by minimizing the aperture diameter. Figure 4 shows the cavity receiver geometry and energy balance of the receiver.



Figure 4 Cavity receiver geometry (left) and energy balance (right) diagrams (Fraser & Klein, 2008)

#### **3.2.1.Conduction Losses**

Receiver conduction losses represent a small percentage of the overall receiver thermal losses. Conduction through the receiver housing occurs at a high rate when the temperature of the receiver and absorber walls increases. Conduction losses are dependent on the convective heat transfer on the exterior of the receiver housing. A series resistance model can be used to obtain the total conductive losses.

$$\dot{Q}_{cond} = \frac{T_w - T_{amb}}{R_{cond} + R_{conv}}$$
(2)

Where  $R_{cond}$  and  $R_{conv}$  for planar geometries can be described as:

$$\boldsymbol{R}_{th,cond} = \frac{L}{k A_{cond}} \tag{3}$$

$$\boldsymbol{R}_{th,conv} = \frac{1}{h A_{conv}} \tag{4}$$

#### **3.2.2.** Convection losses

Convection losses represent a significant percentage of the total DS system losses. Convection losses are a function of cavity geometry, cavity temperature, aperture orientation and diameter, and wind velocity. It is also dependent on the time of the year and location (William B. Stine and Richard B. Diver, 1994).

$$Q_{total,conv} = Q_{natural} + Q_{forced}$$
(5)

$$h_{total,conv} = h_{natural} + h_{forced}$$
 (6)

#### 3.2.3. Radiation Losses

Radiation losses in the receiver represent a significant percentage of the total losses in the receiver losses. According to experimental results from Sandia National Labs (Hogan, Diver, & Stine, 1990), it represents nearly 60% of the receiver losses during morning and evening and about 75% at noon. Unlike the convective losses, radiation losses are relatively constant throughout the day (Hogan et al., 1990).

Radiation losses contribute to losses from the receiver through two ways. The first is radiation due to emission from the aperture due to the large temperature difference between the cavity walls and the paraboloid mirror (Hogan et al., 1990).

$$\dot{Q}_{radiation} = \varepsilon_{cav} \sigma A_{ap} \left( T_{cav}^4 - T_{amb}^4 \right)$$
(7)

The radiation losses due to the reflection off the cavity surface are determined by the effective absorptance of the cavity receiver. Which is estimated to be 0.87 (Hogan et al., 1990).

$$\alpha_{eff} = \frac{\alpha_{cav}}{\alpha_{cav} + (1 - \alpha_{cav}) \left(\frac{A_{ap}}{A_{cav,tot}}\right)}$$
(8)

$$\dot{Q}_{rad,reflect} = \left(1 - \alpha_{eff}\right) \dot{Q}_{in,receiver} \tag{9}$$

### 3.2.4. Cavity Geometry Influence on Radiation

The cavity geometry influences the radiation losses. The receiver cavity has several geometries used. The geometry of the receiver has less than three percent effect on the receiver performance (Harris & Lenz, 1985) and just modifies the flux distribution on the absorber (Hogan et al., 1990).

### **3.3.Stirling engine model**

The Stirling engine analysis consists of elaboration and validation of an ideal isothermal model, an ideal adiabatic model, and non-ideal analysis to evaluate the heat transfer and the flow-friction effects of the heater, regenerator, and cooler.

### 3.3.1. Ideal Isothermal (Schmidt) analysis

There are a set of assumptions for the ideal isothermal analysis. The compression and expansion spaces are considered to have constant temperatures. The regenerator temperature is a linear function between  $T_k$  and  $T_h$ . The compression space temperature  $T_c$  is constant and equal to  $T_k$ . The expansion space temperature  $T_e$  is constant and equal to  $T_h$  as shown in Figure 5. The total mass of the working gas is constant.



**Figure 5 Ideal isothermal analysis temperature flow diagram (Alpha-type engine)** (A. C. M. Ferreira et al., 2014)

Considering the previous assumptions, the Schmidt ideal isothermal analysis aims to calculate the total mass of the working gas using the ideal gas law, the regenerator temperature, sinusoidal compression, and expansion space volumes are calculated to obtain the working gas pressure equation.

$$p = M R / \left[ s + \left( \frac{V_{swe} \cos \alpha}{2 T_h} + \frac{V_{swc}}{2 T_k} \right) \cos \theta - \left( \frac{V_{swe} \sin \alpha}{2 T_h} \right) \sin \theta \right]$$
(10)

where,

$$s = \left[\frac{V_{swc}}{2T_k} + \frac{V_{clc}}{T_k} + \frac{V_k}{T_k} + \frac{V_r \ln(T_h/T_k)}{(T_h - T_k)} + \frac{V_h}{T_h} + \frac{V_{swe}}{2T_h} + \frac{V_{cle}}{T_e}\right]$$
(11)

The net work done by the Stirling engine is the sum of the work done by the expansion and compression spaces over the cycle.

$$Q_e = W_e = \int_{0}^{2\pi} \left( p \; \frac{dV_e}{d\theta} \right) d\theta \tag{12}$$

$$Q_c = W_c = \int_0^{2\pi} \left( p \; \frac{dV_c}{d\theta} \right) d\theta \tag{13}$$

$$W = W_c + W_e \tag{14}$$

For the ideal isothermal analysis, the heat transfer Q is equal to the work done W. For the three heat exchangers, Q is equal to zero. Like the Carnot efficiency, the total Stirling engine efficiency is said to be equal to the total work divided by the heat transferred to the expansion space.

$$\eta = \frac{W}{Q_e} \tag{15}$$

In the isothermal analysis neither the heater nor the cooler contributes to any heat transfer over the cycle. The main disadvantage of this analysis is that it doesn't predict the real cycle.

#### **3.3.2. Ideal adiabatic analysis**

In the ideal adiabatic analysis, the compression and expansion spaces are adiabatic. This leads to a set of assumptions. There is no leakage happens from the working gas. The temperatures  $T_c$  and  $T_e$  are not constant and vary over the compression and expansion phases of the Stirling cycle as shown in Figure 6. The total mass of the working gas M is constant. Work is done by the volume variations of the compression space  $V_c$  and the expansion space  $V_e$  respectively.  $Q_k$  and  $Q_h$  are only transferred between the external environment and the working gas in the cooler and heater respectively.  $Q_r$  is transferred internally between the regenerator matrix and the working gas. Each engine compartment is considered as a separate cell as shown in Figure 7, Enthalpy is transported into and out of the cell by means of mass flow and temperature.



**Figure 6 Ideal adiabatic analysis temperature flow diagram (Alpha-type engine)** (A. C. M. Ferreira et al., 2014)



Figure 7 Stirling engine generalized cell (A. C. M. Ferreira et al., 2014)

Energy transferred for each heat exchangers can be calculated by applying the energy equation to each heat exchanger and substituting for the equation of state.

$$dQ_{k} = \frac{V_{k} \, dp \, c_{v}}{R} - c_{p} \left(T_{ck} \, \dot{m}_{ck} - T_{kr} \, \dot{m}_{kr}\right)$$
(16)

$$dQ_r = \frac{V_r \, dp \, c_v}{R} - c_p \left( T_{kr} \, \dot{m}_{kr} - T_{rh} \, \dot{m}_{rh} \right) \tag{17}$$

$$dQ_{h} = \frac{V_{h} \, dp \, c_{v}}{R} - c_{p} \left(T_{rh} \, \dot{m}_{rh} - T_{he} \, \dot{m}_{he}\right)$$
(18)

The work done in the compression and expansion spaces can be given by.

$$W = W_c + W_e \tag{19}$$

$$\boldsymbol{dW} = \boldsymbol{dW}_c + \boldsymbol{dW}_e \tag{20}$$

$$\boldsymbol{d}W_c = p \, \boldsymbol{d}V_c \tag{21}$$

$$\boldsymbol{d}W_e = p \, \boldsymbol{d}V_e \tag{22}$$

The independent differential equations are solved simultaneously for the seven unknown variables ( $T_c$ ,  $T_e$ ,  $Q_k$ ,  $Q_r$ ,  $Q_h$ ,  $W_c$ ,  $W_e$ ). The objective of the simulation is to find an unknown function that satisfies both the differential equations and the initial conditions. Classical fourth-order Runge-Kutta method is used to numerically solve the equations until convergence conditions are reached. The equation set consists of 22 variables and 7 derivatives to be solved over a complete Stirling cycle.

#### 3.3.3. Non-Ideal analysis

The heat exchanged inside the heater and the cooler is non-ideal. As a result, the gas temperature inside the heater decreases while the gas temperature inside the cooler increases for a given set of wall temperatures. The temperature difference between the walls and the working gas is evaluated by means of heat exchange coefficient, assuming forced convection inside the heat exchangers. This leads to a more realistic analysis that permits a sensitivity analysis as required for an optimal heat exchangers design. Figure 8 shows the temperature distribution between the Alpha-type Stirling engine compartments.



**Figure 8 non-ideal analysis temperature flow diagram (Alpha-type engine)** (A. C. M. Ferreira et al., 2014)

In the non-ideal analysis, the heat capacity of the regenerator is very small. This leads to an increase in the temperature difference between the hot source and cold sink temperature. This non-ideal effect of the regenerator happens due to the convective thermal resistance between the regenerator surface and the working gas (Urieli & Berchowitz, 1984). This can be computed using the Number of Transfer Units (NTU) defined as a function of the heat exchanger size. the NTU method is used to calculate the heat transfer in the heat exchangers.

$$NTU = \frac{h A_{wg}}{\rho \, u \, c_p \, A} \tag{23}$$

NTU is used to compute the regenerator effectiveness  $\varepsilon_r$  which can be defined as the ratio between the real amount of exchanged heat between the working fluid and the regenerator matrix, and the maximum amount of heat transferred in the regenerator adiabatically.

$$\varepsilon_r = \frac{NTU}{(1+NTU)} \tag{24}$$

The regenerator heat transfer reduction ( $Q_{rloss}$ ) can be obtained as a function of regenerator effectiveness and the amount of heat transferred by the regenerator in the adiabatic analysis  $\dot{Q}_{r,ideal}$ .

$$\dot{Q}_{rloss} = (1 - \varepsilon_r) \, \dot{Q}_{r,ideal} \tag{25}$$

The effectiveness of the heater and cooler are the same and can be defined as by means of NTU.

$$\varepsilon = 1 - e^{-NTU} \tag{26}$$

The actual heat for the cooler and heater can be described as.

$$\dot{Q}_h = \dot{Q}_{h,ideal} + \dot{Q}_{rloss} \tag{27}$$

$$\dot{Q}_k = \dot{Q}_{k\,deal} + \dot{Q}_{rloss} \tag{28}$$

The flow-friction effect of the working gas flowing through the heat exchangers affects the engine performance because it results in a pressure drop or pumping loss. The pumping loss corresponds to the work required to let the working gas move through the heat exchangers and results in the reduction of the power output of the engine. The pressure drop is calculated for the three heat exchangers, then the value of the corresponding work can be formulated by integrating over the complete cycle.

$$W = \int_0^{2\pi} p \left( dV_e + dV_c \right) - \int_0^{2\pi} \left( \sum_{i=1}^3 \Delta p_i \; \frac{dV_e}{d\theta} \right) d\theta \tag{29}$$

Where the first term of the previous equation represents the ideal adiabatic work done per cycle, while the second term represents the work losses.

### 4. Simulation Strategy

In the previous section, the model of every component of the system is discussed. A comprehensive model using MATLAB software was created using different models of components as shown in Figure 9. The system input is the Direct Normal Irradiance (DNI) coming from the sun at certain locations, while the system outputs are the efficiency, output power and heat transferred in different Stirling engine compartments.



**Figure 9 Simulation strategy flow chart** 

### 4.1.System model parameters

Table 1 presents the concentrator and receiver parameters, engine dimensions, working gas type, and operating parameters. The concentrator and receiver sizing are based on the size of the Stirling engine which is a theoretical model presented by (A. C. Ferreira et al., 2014) which has the same geometry of the SOLO V161 Stirling engine, but has smaller piston swept volume. The SOLO V161 Stirling has swept volume of 160 cm<sup>3</sup>, while the modelled engine has swept volume of 130 cm<sup>3</sup>. It was assumed that both engines have the same materials. This leads to scaling both the concentrator and the receiver dimensions. The modelled concentrator dish has 6.6m aperture diameter which was calculated in order to choose a dish size suitable for the size of the Stirling engine. The concentrator dish of the Eurodish unit that uses SOLO V161 has a concentrator aperture diameter of 8.8 m (Keck, Schiel, Reinalter, & Heller, 2002). This leads to choosing smaller aperture diameter in order to prevent overheating of the engine.

The MATLAB model uses the data to define the engine parameters for every engine component and operating conditions. After the definition of parameters and conditions, a Schmidt ideal-isothermal analysis to calculate the mass of the working gas and other isothermal based analysis data. An ideal-adiabatic analysis is then performed on the modeled engine. Finally, a non-ideal analysis to calculate the pumping losses and obtain accurate results is performed. The three types of analysis are based on (Urieli & Berchowitz, 1984).

<b>Fable 1 Simulation parameters an</b>	d system component dimensions
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Concentrator parameters							
Poflactivo motorial	Aluminum	Reflectivity	<b>+x</b> 7	02 5 %	Apertu diamet	ire ter	6.6 m
Kenecuve material	Aluiiniuni		92.3 %	Apertu area	ire	34.2 m <sup>2</sup>	
Receiver parameters							
Receiver material	Inconel	Absorptance	93 %	Apertu diamet	ire ter	0.178 m	
	meoner	Emittanc	e	88.9 %	Apertu area	ire	$0.025 \text{ m}^2$
Insulation	Ceramic						
Stirling	g engine dime	ensions and	ope	erating par	rameters		
Engine Type			A	Alpha-type	e		
Ex	pansion and	compressio	n sp	aces (sim	ilar)		
Clearance volume				$2.5e-5 m^3$			
Swept volume			0	.00013 m	3		
Cylinder bore				63.5 mm			
Cylinder Stroke	Cylinder Stroke 41 mm						
	H	eat exchang	gers				
Heat exchanger	Co	ooler		Heater			
Heat exchanger type	Smooth pipes			Smooth pipes			
Internal diameter	0.0	03 m		0.003 m			
Number of tubes	1	.50		80			
Heat exchanger length	0.	1 m		0.15 m			
	Regene	rator heat e	exch	anger			
Regenerator Configuration	Tubular reg	ibular regenerator de Regenerator matrix type		r matrix	Mesh matrix		
External diameter	0.056	ó m	1	Number of	f tubes	1	
Internal diameter	0.046	ó m	Matrix porosity			0.7	
Regenerator length	0.06 m			Wire matrix diameter		0.0003 m	
Working gas							
Working gas type Hydrogen							
Operational parameters							
Hot source temperature Receiver output K							
Cold sink temperature	353 K (80°C)						
Phase angle	Phase angle 90 degrees						
Mean pressure 8e+6 Pa							
Engine speed (frequency)		3000	0 rpm / 50	) Hz			

### 4.2. Model validation and verification

Validation was performed by comparing the model output with published experimental results. The concentrator and receiver model was validated by comparing the results with the experimental results of (Reinalter et al., 2008) as

shown in Table 2 By applying the same parameters of concentrator and receiver dimensions and operating conditions, and an input DNI of 907 W/m<sup>2</sup>, the thermal power transferred into the Stirling engine was resulted as 20.73 kW, while the experimental output was 30.77 kW with an error percentage of 32.6%. The large error percentage is due to the assumptions made in the receiver losses model and can be solved by performing an accurate heat transfer analysis with experimental measurements, which was not possible during the research.

#### Table 2 Concentrator and receiver model validation

Concentrator and receiver models						
Output Parameter	Output value	Reference output	Unit	% error		
Thermal power transferred to the Stirling engine by the receiver	20.73	30.77	kW	$\approx 32.6\%$		

The Stirling engine model was verified by comparing the model results by the results obtained by (A. C. M. Ferreira et al., 2014). The engine parameters were originally obtained from this reference. (A. C. M. Ferreira et al., 2014) performed a detailed economic and thermodynamic modeling of the Stirling engine, and used several operating parameters to obtain the best parameter values such as mean pressure and operating frequency. The comparison was performed on the engine working with 25 Hz frequency, 3 bar mean working gas pressure, and 725 K heater temperature. The results were very close to the reference results as shown in Table 3.

Output Parameter	Output value	Reference output	Unit	% error			
Schmidt analysis							
Power	1573	1572	W	pprox 0%			
indicated efficiency	51.3	51.3	%	pprox 0%			
Ideal Adiabatic analysis							
Total power output	1517.88	1471	W	pprox 3.2%			
Thermal efficiency	45.8	43.0	%	pprox 6.5%			
Non-ideal analysis							
Actual power	1284.9	1390.4	W	$\approx$ -10.1%			
Actual efficiency	28.3	31.6	%	$\approx$ -10.44%			

### Table 3 Stirling engine model validation

# 5. Simulation results

The simulation was conducted using different input DNI for different zones assigned by the Egyptian government for renewable energy projects. The locations of these zones and the yearly average DNI for CSP applications are published in the Solar Atlas of Egypt by the National Renewable Energy Agency (El-Askary, Kosmopoulos, & Kazadzis, 2018). The DNI data of these zones in addition to three more zones to cover the Egyptian map was obtained using METEONORM software.

# 5.1.DS system performance in different zones in Egypt

The data of the zones that were studied using the system model, their location, their yearly average DNI, the output power in Watts and the engine efficiency are presented

in Table 4. Figure 10 presents a graphical comparison between the different zones by means of the output pressure. Figure 11 presents a comparison between the locations by means of engine efficiency.



Figure 10 Yearly average output power for the studied zones



Figure 11 Yearly average engine efficiency for the studied zones

#	Logation Nama	Coordinates	DNI (Yearly	Output	Engine			
#	Location Name	Coordinates	$(W/m^2)$	(W)	(%)			
Red	Red sea coast zone							
1	Hurghada (Al Ahyaa)	27.16°E, 33.46°N	313.58	6950.7	23.7			
2	Hurghada (Kilo 10)	27.18°E, 33.42°N	304.79	6858.9	23.5			
3	Marsa Alam location	26.50°E, 33.54°N	309.6	6909.3	23.6			
4	Gebel El-Ziet location	28.12°E, 33.20°N	332.07	7135.5	24.1			
5	Sharm El-Sheikh	27.71°E, 34.18°N	319.9	7015	23.9			
Suez	z Governorate		•					
6	El Zaafarana	27.16°E, 33.46°N	315.9	6974.4	23.8			
Nor	thern Coast							
7	Ras El Hekma	31.122°N, 27.52°E	256.8	6308.4	22.3			
8	Baghoush	31.925°N, 27.395°E	275.4	6532.2	22.8			
9	El- Mathany	31.232°N, 26.474°E	278.9	6573.2	22.9			
10	El Galalah	31.145°N, 28.11°E	282.9	6619.1	23			
11	Al Rowaysat	30.48°N, 29.19°E	284.4	6636	23.1			
Al Kuraymat								
12	Al Kuraymat	29.163°N, 31.148°E	262.1	6373.8	22.5			
Wes	st and East Nile							
13	Land number three	28.3°N, 30.15°E	322.4	7040.1	23.9			
14	Land number two	27.8°N, 31.1°E	321.8	7034.1	23.9			
15	Location 1	28.3°N, 31.15°E	318.6	7001.9	23.8			
East	East Nile Zone							
16	East Nile Zone	28°N, 31°E	325	7066	24			
Aswan								
17	Benban	24.25°N, 32.43°E	329.34	7108.8	24.1			
18	Fares	24.37°N, 32.5°E	330.47	7119.9	24.1			
Other locations								
19	El Natroon	30.4°N, 30.35°E	219	5799.5	21.1			
20	El Arish	31.08°N, 33.83°E	227	5913.8	21.4			
21	Kharga	25.45°N, 30.53°E	254.2	6275.7	22.2			

Table 4 Studied zones with inputs (DNI) and outputs (output power and efficiency)

The highest results obtained from zone number 18 in Fares, Aswan with coordinates of 24.37N, 32.5E. The outputs of Fares zone were 7119.9 W of output power and 24.1% efficiency (yearly average), while the work loss due to pressure drop was calculated as 189.1 W. El-Natroon zone (30.4°N, 30.35°E) showed the least power output value of 5799.5W with 21.1% engine efficiency and 197 W work loss due to pressure drop. The overall results show good indications for using the DS systems under Egyptian operating conditions. Figure 12 and Figure 13 shows the Pv and energy vs crank angle diagrams for Fares and El-Natroon zones respectively.



Figure 12 Pressure-Volume diagram for Fares zone



Figure 13 Pressure-Volume diagram for El-Natroon zone

#### 5.2. Comparison between DS and PV system performance

The DS system is considered to have one of the highest efficiencies compared to other solar energy technologies. A comparison is done between the simulated DS system and a simulated PV system by means of the total land occupied by the systems, and the overall system efficiencies. The simulation of the PV systems was done using System Advisor Model (SAM) software, which is a reliable renewable energy simulation tool developed and distributed by the U.S. Department of Energy's National Renewable Energy Laboratory. The selected location to conduct the comparison is Aswan. The latitude and longitude are 23.97°N and 32.78°E respectively. The SAM database gave a DNI of 6.67 kWh/m<sup>2</sup>/day, which means that the simulation will run at 277.91 W/m<sup>2</sup>. Using the given DNI, the DS simulation model gave 5.6kW output power. The simulation of the PV system using Sam to produce the same power output. the solar module model used is JKMS300M-72 produced by Jinko Solar, which is a polycrystalline solar module that produce 300W with nominal efficiency of 15.47%.

The PV simulation using SAM software results gave a total of 2 strings in parallel with 9 modules per each string with tilt angle of 30 degrees and ground coverage ratio (GCR) of 0.5 as shown in Figure 14. The total module area is  $34.9 \text{ m}^2$ , and the total PV system land area is  $69.8 \text{ m}^2$ . The DS system requires system land area of  $43.56 \text{ m}^2$  with concentrator dish aperture area of  $34.2 \text{ m}^2$ . Therefore, the DS system requires equivalent 18 PV modules, with 37.6% more land required for the PV system (Culligan & Botkin, 2007).



Figure 14 Different tilt angles and their corresponding GCR (Culligan & Botkin, 2007)

The total land area occupied by the systems is calculated considering the spacing (GCR) between either the PV modules or the DS system units to overcome the shading effects. The results of this comparison show that the DS system needs less land area than the widely used PV systems.

Comparing the PV and DS systems by means of the Levelized Cost of Energy (LCOE) which is the measure of a power source that allows the comparison of different electricity generation methods on a consistent basis. LCOE is the economic assessment of the average total cost to implement and operate a power generation system over its lifetime divided by the total energy output of the system over that lifetime (Larchet et al., 2017).

There is no enough data for conducting this comparison in Egypt because of the absence of current DS projects in Egypt and the various parameters to calculate the value of LCOE. As a result, the comparison was done based on the data obtained from (Larchet et al., 2017) which compared between the LCOE value of the DS and PV systems in Morocco, which is a country located in the same region of Egypt and nearly has the same economical and geographical properties.

The results showed that the LCOE of DS system ranges from 77.7 \$/MWh to 91.8 \$/MWh depending on the production volume of the system, while the PV systems has a LCOE value of 65.4 \$/MWh (Larchet et al., 2017).

### 6. Conclusion

In this research, the DS system components and models are studied to generate a comprehensive simulation model. The simulation was conducted to investigate the DS system performance in 21 different locations that cover Egypt. The yearly average output power of the engine ranges from 5.799kW to 7.12kW at El-Natroon and Fares zones respectively. Whereas, the engine efficiency ranges from 21.1% in El-Natroon to 24.1% in Fares. Generally, the engine performance does not show great variation across Egypt. A comparison was conducted between DS and PV systems at the same operating conditions. The DS technology has better efficiency and generates more power than PV technology. Results shows that the DS system requires 37.6% less land area than an equivalent PV system, while the PV systems is better in terms of levelized cost of energy (LCOE). The results obtained from the simulation provides promising indications for the use of dish Stirling engine systems in Egypt. Finally, future developments of DS system components with enhanced performance present a very promising opportunity for developing DS projects in Egypt.

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