



## Modeling and Performance Analysis of a Quad Detector

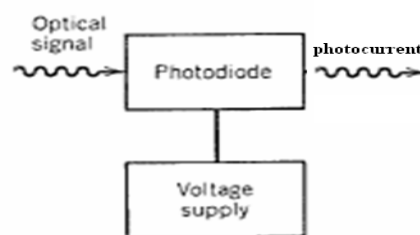
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**Abstract:** In this paper we are interested in modeling, performance evaluation, and measurement of a quadrant detector. Photodiode is modeled using its differential equations then implemented and solved using ORCAD -pspise. The model validation was performed by comparing the model results with the experimental measurements using a proposed setup. The model was used to investigate the effect of the photodiode donor concentrations, acceptor concentrations and intrinsic region concentrations. The simulation results showed that the donor concentrations should be kept as small as possible in order to improve the photodiode performance, the acceptor concentrations has a small effect on the performance, and as the intrinsic region concentration increases the photocurrent increases and the junction capacitance decreases with a small increase in the dark current.

**Keywords:** Photodiode modeling, Quad detector, photodiode performance measures

### 1. Introduction

A photo sensitive detector (PSD) is a continuous silicon photo detector used for optical position sensing and basically consists of a uniform resistive layer, which is formed on a silicon substrate. A pair of electrodes is formed at the ends of the resistive layer from which photo-currents are measured. These photo-currents are generated as a result of the incident radiation effect as shown in figure (1) and their magnitude is relative to the distance of the electrode to the center of the beam spot on the sensor's active area. The photo-currents are typically amplified and converted to form the measured voltage signal used by the control system. PSDs can be divided into two general groups: segmented PSDs and lateral effect PSDs [1].



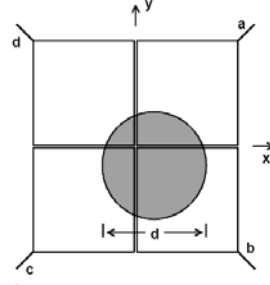
**Fig. 1 Photodiode transfer function**

As shown in figure (2) Segmented PSD are quadrature PSD each is divided into four segments, which are separated by a small gap, called the dead region. The sensor is used for positioning by measuring each segment's photocurrent. A symmetrical beam is positioned at the center of the QD if all of these currents are equal [2].

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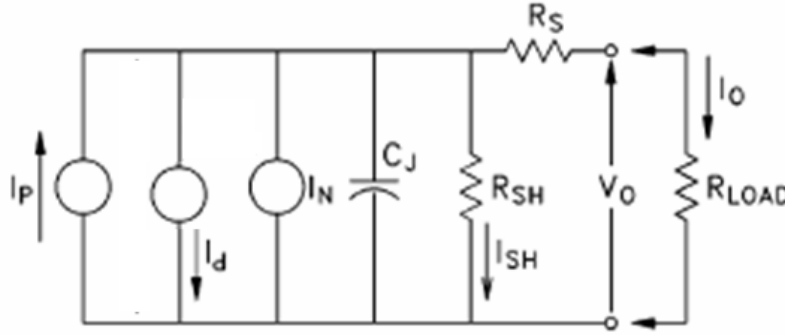
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**Fig. 2 Quadrant detector structure**

Figure (3) shows the equivalent circuit diagram for the photodiode where  $I_P$  is the photo generated current,  $I_d$  is the dark current,  $I_N$  is the internal noise current,  $R_{SH}$  is the shunt resistance,  $R_S$  is the series resistance,  $C_J$  is the junction capacitance and the output photocurrent is taken at the load of the detector [ 3 , 4 ].



**Fig. 3 Equivalent Circuit diagram for the photodiode**

## 2. Photodiode Modeling

In this paper we will present the model of a single photodiode which is considered as the building unit of the quad detector. Starting with the differential equation (1) the depletion region of a pin photodiode in reverse bias supports a constant electric field and linearly varying energy bands. From Poisson's equation we have [5]

$$\frac{d^2\Phi}{dx^2} = \frac{q}{\epsilon} (N_d^+ + N_A^- + p - n) \approx 0 \quad (1)$$

where  $q$  is the electron charge,  $\epsilon$  is the electric field,  $A$  is a linear function of position,  $N_d^+$  is the ionized donor concentration impurities,  $N_A^-$  is the acceptor concentration impurities, the density of electron in the conduction band is  $n$  and that of holes in the valance band is  $p$ .

If we neglect the intrinsic region background doping and assume that the generated photo charge is negligible or quasi-neutral this implies that  $\Phi$  is a linear function of position. The main contribution of the photocurrent is given by the drift current associated with carriers generated inside the intrinsic depleted region;

$$G_o(x) = \eta Q \frac{P_{in}(1-R)}{Ahf} \alpha e^{-\alpha x} = G_o(0) e^{-\alpha x} \quad (2)$$

where  $G_o(x)$  is the optical generation rate along X-axis,  $\eta Q$  is the intrinsic quantum efficiency,  $P_{in}$  is the total incident power on the left (upper) photodiode facet,  $A$  is the detector area,  $hf$  is the photon energy,  $\alpha$  is the material absorption, and  $R$  is the power reflectivity of the upper surface.

To analyze the DC pin current  $I_{PD}$  we decompose the total current into electron current (drift and diffusion) and hole current (drift and diffusion) components. The device current is constant in x and can be expressed as [5, 6]. The absorption coefficient of the material ( $\alpha$ ) can be calculated from [7].

$$\log \alpha = (13.2131 - 36.7985\lambda + 48.1893\lambda^2 - 22.7562\lambda^3) \quad (3)$$

The total photodiode current is given by:

$$-I_{PD} = \frac{qAD_{np}}{W_p} n_0' + \frac{qAD_{hn}}{L_{hn}} p_0' - \left[ \frac{qAG_0(0)L_{hn}}{1 + \alpha L_{hn}} e^{-\alpha(W+W_p)} + I_i \right] \quad (4)$$

where the first term is the dark current and the second term is the photocurrent. Expanding the generation rate  $G_0$  and using equation (2) the photocurrent can be expressed as [5, 6]

$$I_L = \eta Q \frac{q}{hf} P_{in} (1 - R) e^{-\alpha W_p} \left( 1 - \frac{e^{-\alpha W}}{1 + \alpha L_{hn}} \right) \quad (5)$$

(Equation (5) holds when  $\alpha W_p$  is small, since photocurrent generation in the top layer is explicitly neglected.) thus leading to the responsivity.

According to the general equation studied before we used the orcad pspice tool to model the photodiode and simulate the output [8 , 9], then compare the output with the datasheet or measured data. From the equivalent circuit model of the photodiode and according to the equation that represents each part in the circuit model we built the model, where each block of the model represents a set of equations which provide the simulation of the photodiode behavior, figure (4) shows ORCAD photodiode model. Every part of this equation must be in general form, so that it is possible to change its parameters. The challenge was how to solve this with the orcad tool and the analog behavior model (ABM) was the suitable solution. With the help of the electronic part to achieve the photodiode behavior, the ABM helped us to use and represent the equation for each part of the model with the accepted behavior and function. The parameters which forms the equation must be given to build the photodiode model and provide the accepted data with the real photodiode.

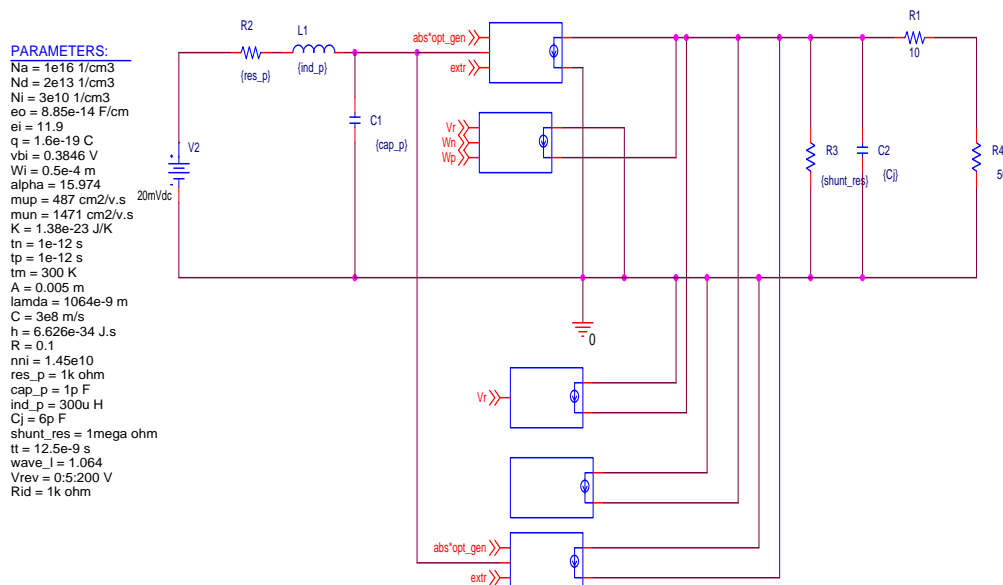
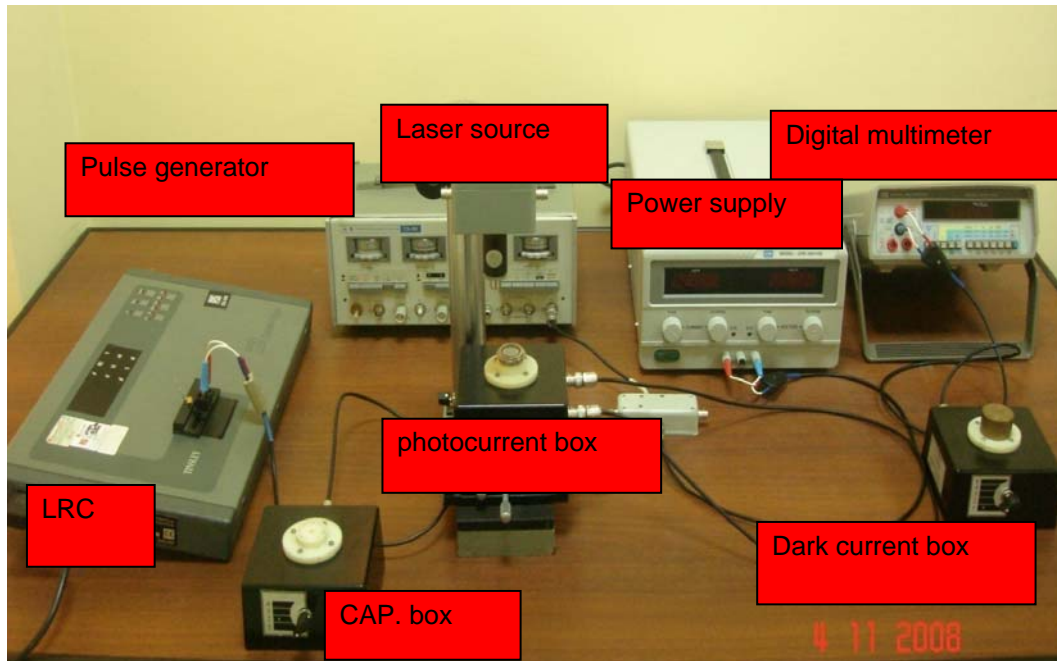


Fig. 4 ORCAD Photodiode model

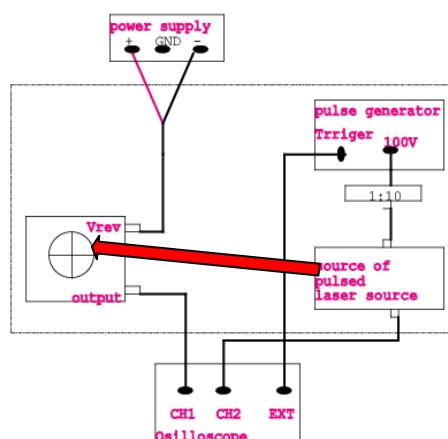
### 3. Photodiode Model Validation

This paper discusses the method and tools that are used to measure the photodiode parameters. There are three parameters that can be measured by the proposed setup: photocurrent, dark current, and junction capacitance. Figure (5) shows the proposed setups that are used to measure the above parameters. The setup consist of Γ5-88 pulse generator , GOS-6031 oscillograph , LFR Sensitivity , GDM- digital voltmeter , GPR3HIDD power supply and, laser source its wavelength is  $1.064 \mu\text{m}$



**Fig. 5 Photodiode parameter measurement setup**

Figure (6) shows the proposed setup that is used to measure the photocurrent output from the photodiode due to the incident radiation beam on the photodiode surface area.



**Fig. 6 Photocurrent measurement setup**

Figure (7) shows the proposed setup that is used to measure the dark current output from the photodiode in the absence of incident radiation. Figure (8) shows the proposed setup that is used to measure the junction capacitance of the photodiode in the absence of incident radiation.

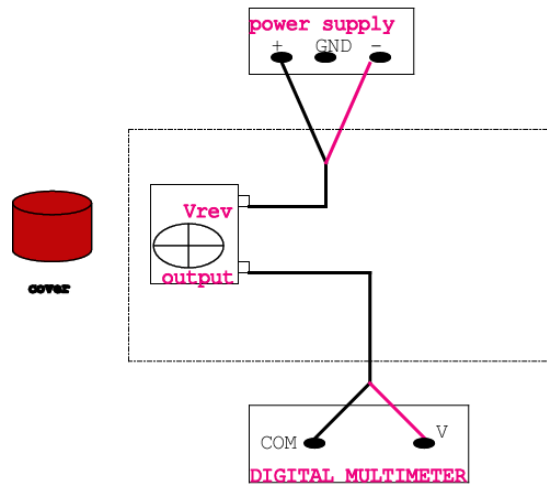


Fig. 7 Dark current measurement setup

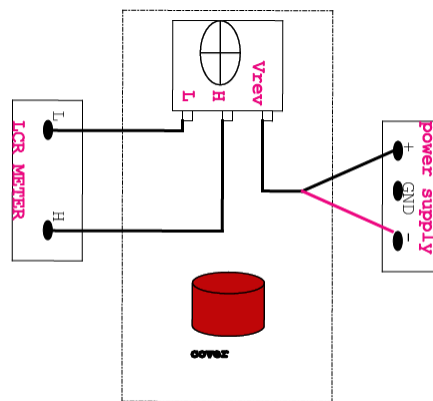


Fig. 8 Junction capacitance measurement setup

#### 4. Simulation Results and Analysis

Figures 9 and 10 show the simulated and measured output pulse at the load of the photodiode when the input pulse incident on the photodiode is the same for both measured and simulated cases. The simulated output signal has a good agreement with the measured pulse where the amplitude has the same value (around 100mV), the pulse width also has the same value (5 usec), and the period time is the same (50 usec). The measured fall time of the pulse is the same in the two pulses (fall time=0.28 usec), Fig. 9.

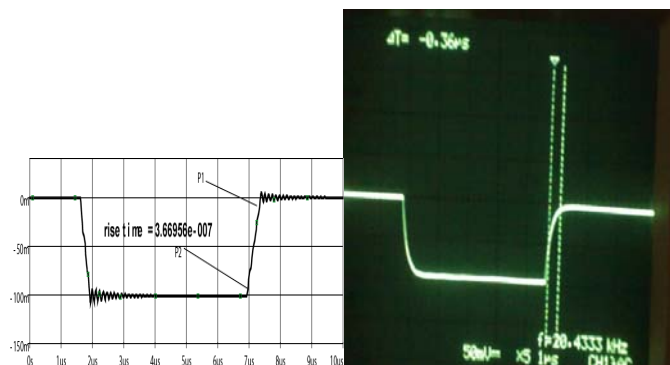
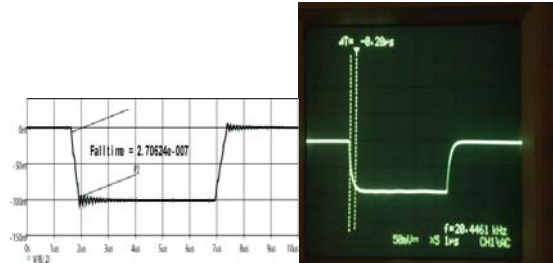


Fig. 9 Simulated and measured pulse rise time

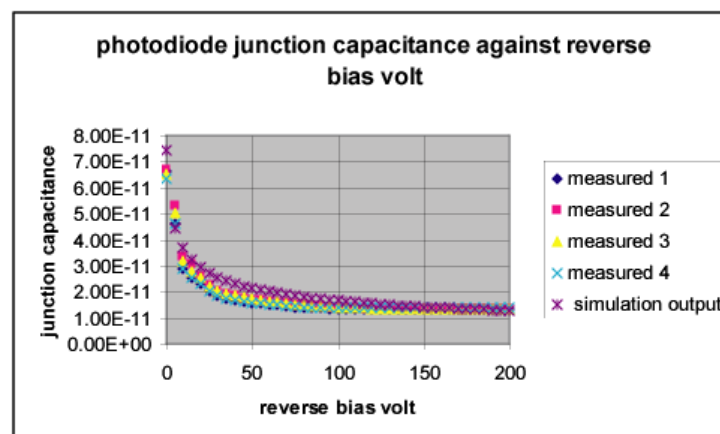
Likewise, the measured rise time of the pulse is the same in the two pulses (rise time= 0.36 *usec*), Fig. 10.



**Fig. 10 Simulated and measured pulse rise time**

Figure 11 shows the relation between the junction capacitance and the reverse bias volt for both measured and simulated values; we can see the good agreements between the four measured values and the simulation values.

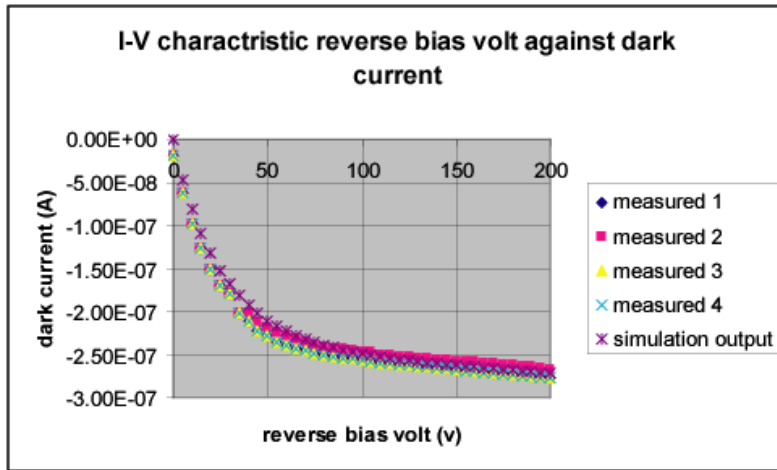
It is clear that the junction capacitance decreases as the reverse bias volt increases until it reaches value of the reverse bias near saturation value in which the decrease of the junction capacitance is very small.



**Fig. 11 Simulated and measured values of a junction capacitance**

Figure 12 shows the relation between the dark current and the reverse bias volt for both measured and simulated values, we can see that there is a good agreement between the four measured and the simulated values.

It is clear that the dark current increases as the reverse bias volt increases, we can conclude that from the photodiode measured and simulated results shown in the previous pages.



**Fig. 12 Simulated and measured values of dark current**

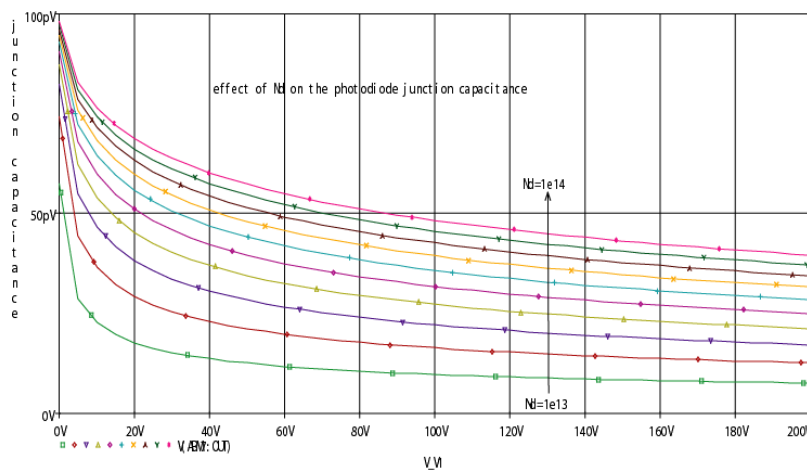
From figures 9, 10, 11, and 12 it is clear that we must apply a reverse bias to the photodiode to decrease the capacitance and increase the photocurrent which will increase the photodiode sensitivity with the small increase on the dark current.

The effect of the photodiode material parameters on the photodiode performance will be discussed in the remainder of this paper.

The photodiode material has a great effect on the performance of the detector we will discuss this parameter and its effect in terms of donor concentration, acceptor concentration and intrinsic region concentration.

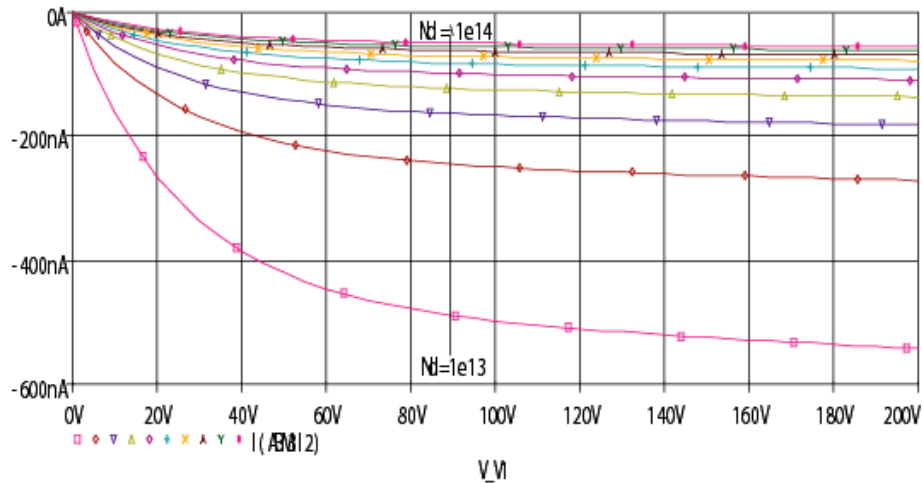
We will show the effect of each parameter on the junction capacitance, dark current and photocurrent.

Figure 13 shows the effect of the donor concentration on the photodiode junction capacitance,  $N_d$  was swept from  $N_d=1e13$  to  $N_d=1e14$  with the step  $N_d=1e13$ . It is clear that the junction capacitance value shifted to higher values with the increase of the  $N_d$ .



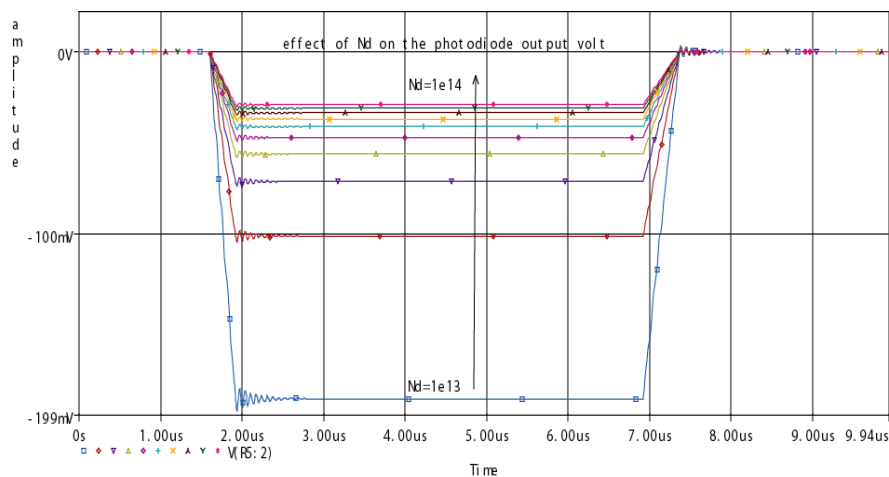
**Fig. 13 Junction capacitance vs. reverse volt for different donor concentration**

Figure 14 shows the effect of the donor concentration on the photodiode dark current,  $N_d$  was swept from  $N_d =1e13$  to  $N_d =1e14$  with the step  $N_d =1e13$ . It is clear that the dark current value shifted to lower values with the increase of the  $N_d$ .



**Fig. 14 Dark current vs. reverse volt for different donor concentration**

Figure 15 shows the effect of the donor concentration on the photodiode output photocurrent pulse,  $N_d$  was swept from  $N_d = 1e13$  to  $N_d = 1e14$  with the step  $N_d = 1e13$ . It is clear that the photocurrent value shifted to lower values with the increase of the  $N_d$ .



**Fig. 15 Output pulse vs. time for different donor concentration**

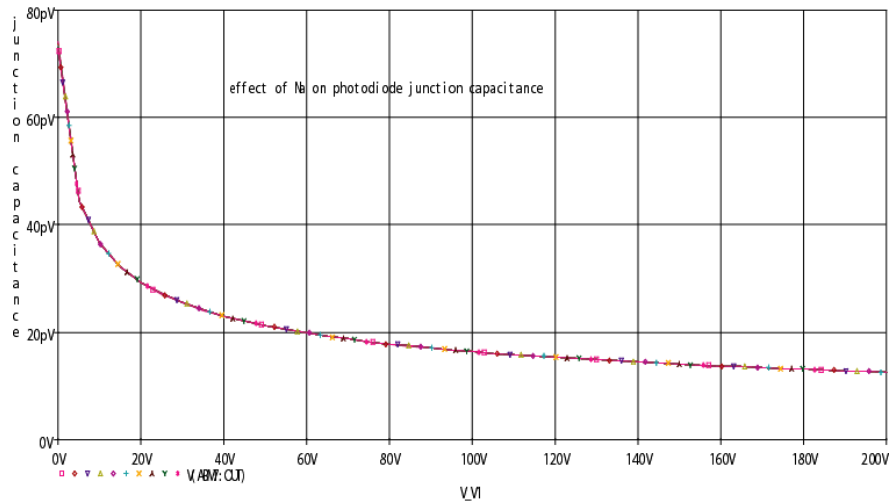
We can conclude the effect of the donor concentration on the photodiode from figures 13, 14, and 15 that as the donor concentration increases the value of the junction capacitance increases, and both of the dark current and photocurrent decreases.

To improve the photodiode performance we must decrease the junction capacitance and dark current with the increase of the photocurrent, so we have to choose the donor concentration as small as possible.

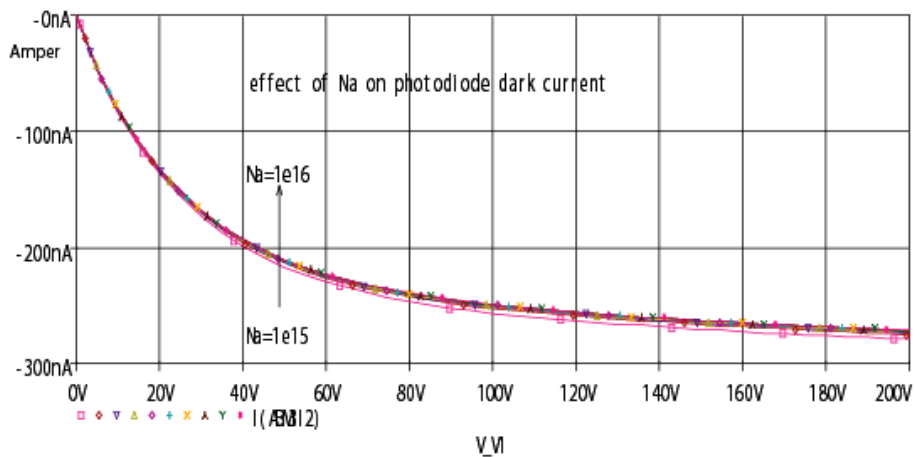
Figure 16 shows the effect of the acceptor concentration on the photodiode junction capacitance,  $N_a$  was swept from  $N_a = 1e16$  to  $N_a = 1e17$  with the step  $N_a = 1e16$ . It is clear that from the figure the junction capacitance value appears to be constant.

Figure 17 shows the effect of the acceptor concentration on the photodiode dark current,  $N_a$  was swept from  $N_a = 1e15$  to  $N_a = 1e16$  with the step  $N_a = 1e15$ . It is clear that the dark current slightly decreases with the increase of  $N_a$ .





**Fig. 16 Junction capacitance vs. reverse volt for different acceptor concentration**



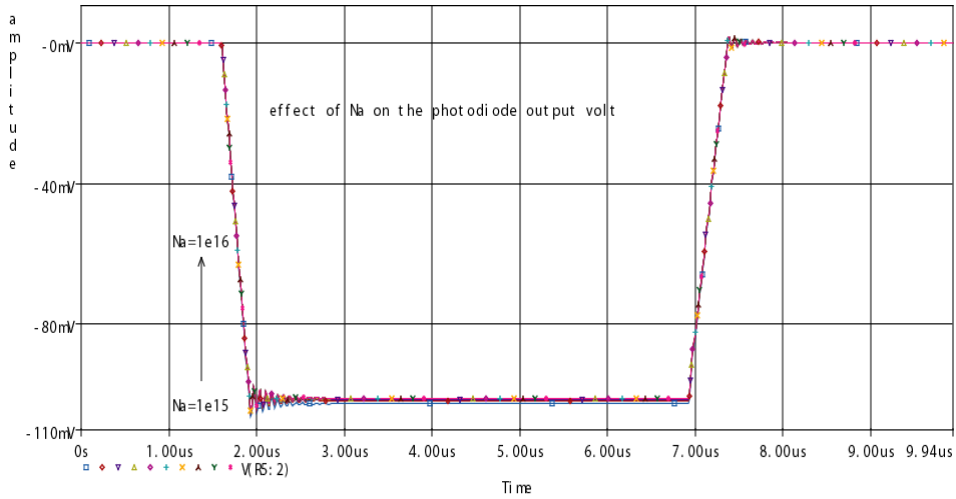
**Fig. 17 Dark current vs. reverse volt for different acceptor concentration**

Figure 18 shows the effect of the acceptor concentration on the photodiode output photocurrent pulse,  $N_a$  was swept from  $N_a = 1e15$  to  $N_a = 1e16$  with the step  $N_a = 1e15$ . It is clear that the photocurrent slightly decreases with the increase of  $N_a$ .

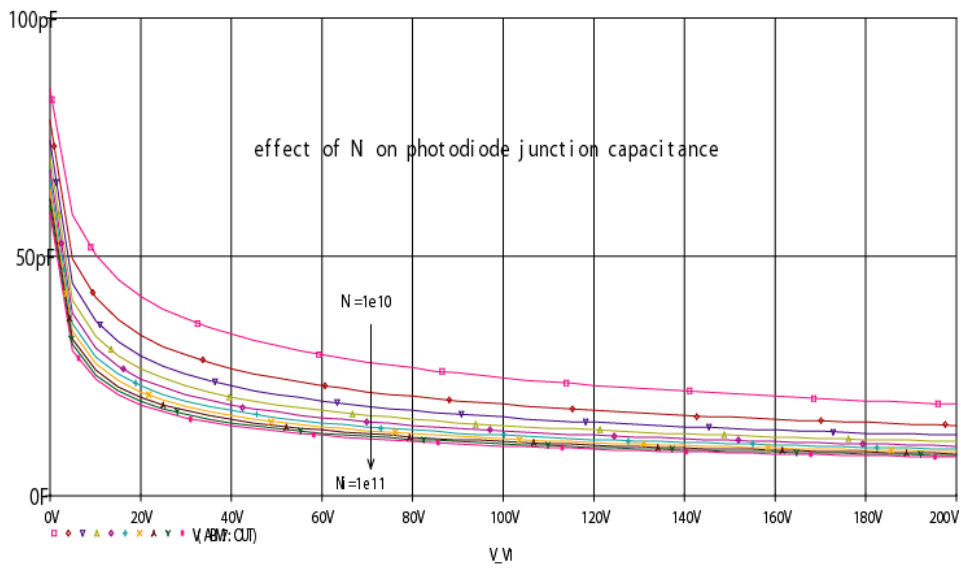
We conclude the effect of the acceptor concentration on the photodiode from Figures 16, 17, and 18 that with the increase of the acceptor concentration the value of the junction capacitance remains nearly the same, the dark current decreases slightly, and photocurrent remains nearly the same, so that we must chose the value of the acceptor concentration with the smallest dark current value.

Figure 19 shows the effect of the intrinsic region concentration on the photodiode junction capacitance,  $N_i$  was swept from  $N_i = 1e10$  to  $N_i = 1e11$  with the step  $N_i = 1e10$ . It is clear that the junction capacitance decreases with the increase of  $N_i$ .

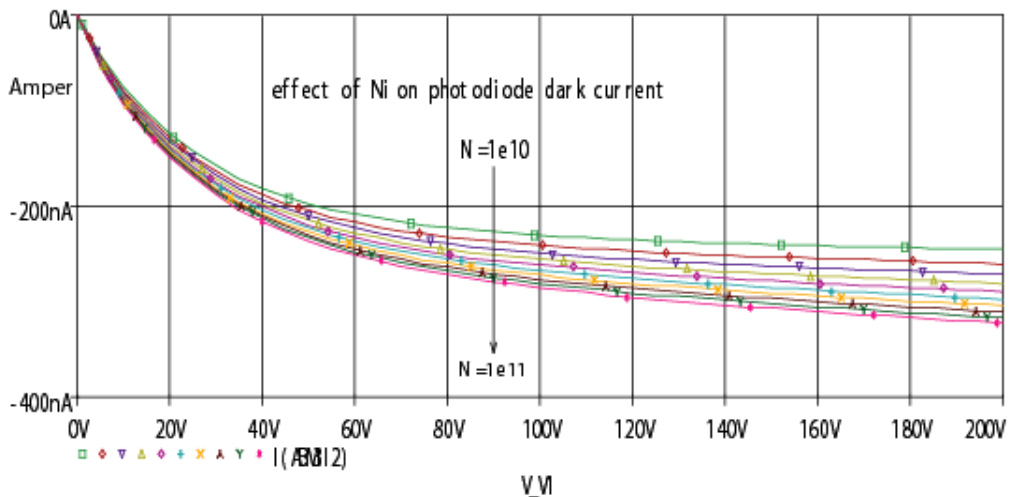
Figure 20 shows the effect of the intrinsic region concentration on the photodiode dark current,  $N_i$  was swept from  $N_i = 1e10$  to  $N_i = 1e11$  with the step  $N_i = 1e10$ . It is clear that the dark current increases with the increase of  $N_i$ .



**Fig. 18 Output pulse vs. time for different acceptor concentration**

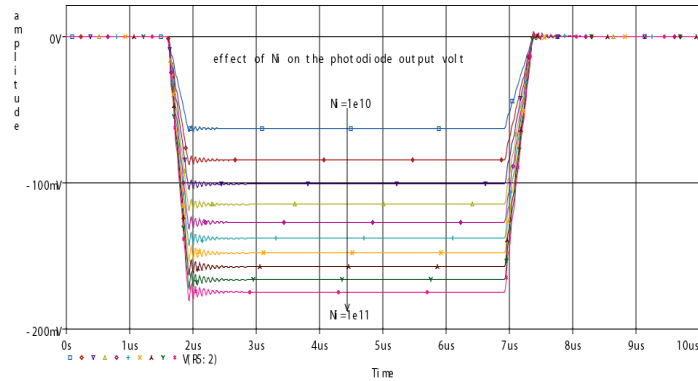


**Fig. 19 Junction capacitance vs. reverse volt for different intrinsic region concentration**



**Fig. 20 Dark current vs. reverse volt for different intrinsic region concentration**

Figure 21 shows the effect of the intrinsic region concentration on the photodiode output photocurrent pulse,  $N_i$  was swept from  $N_i = 1e10$  to  $N_i = 1e11$  with the step  $N_i = 1e10$ . It is clear that the photocurrent increases with the increase of  $N_i$ .



**Fig. 21 Output pulse vs. time for different intrinsic region concentration**

We can conclude the effect of the intrinsic region concentration on the photodiode from figures 19, 20, and 21 that with increasing of the intrinsic region concentration the value of the junction capacitance decreases and the photocurrent increases but the dark current slightly increases. To improve the photodiode performance we must increase the photocurrent with the decrease of the dark current and the junction capacitance so that we have to choose the largest possible value for the intrinsic region concentration.

## 5. Conclusion

Photodiode model was implemented in ORCAD pspice tool, the validation of the model using a proposed setup was performed, a good agreement was achieved between the measured and simulated results. The model was used to analyze the performance of the photo diode where the effect of the different parameters of the photodiode material on its performance were investigated.

## 6. References

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