



## Determination Of Refractive Indices Of Heavy Metal Ions Solutions To Evaluate Their Concentrations

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### Abstract

Surface plasmon resonance (SPR) sensors have advantages of tracing heavy metal ions content and environmental monitoring. In this work, a surface plasmon resonance structure was built. It was based on Kretschmann structure which is cost-effective. The sensing layer was gold thin film deposited by sputtering technique. The resonance angles ( $\theta_{SPR}$ ) of heavy metal ions  $Pb^{+2}$ ,  $Zn^{+2}$  and  $Cd^{+2}$  were shifted to higher values with increasing their content. Complex refractive indices of metal ions were calculated. The real and imaginary parts of refractive indices of heavy metal ions were increased while increasing their concentrations. Data curve fitting yields calculated  $\theta_{SPR}$  for any unknown concentration of heavy metal ions, also the performance factors were determined which predict the proper use of SPR sensor for different metal ions detection.

Keywords: Surface Plasmon Resonance; Kretschmann configuration; Heavy metal ions; sensor performance; gold thin film; optical properties

### 1. Introduction

Surface plasmon resonance SPR biosensors showed significance over conventional sensors, which included refractive index sensitivity, fast sensor reaction, real-time detection, and a label-free approach. Moreover, SPR sensors have great other applications in environmental tracking, security, scientific diagnostics, food safety and SPR imaging generation, hence SPR has gained vast momentum with growing of clinical publications [1]–[4].

SPR excitation typically requires high angular momentum for aquatic solution detection. Therefore, a coupling component is required in many designs to ensure the incidence of a large angle at the metal-dielectric interface [5]. The coupling method which lies between light and metal film/dielectric contact is the key component in SPR based–systems. It occurs via grating [6], waveguide, optical fiber and prism couplers which optically excite surface plasmons. Different approaches have been used for measuring SPR as wave length interrogation[7], angular interrogation[8], intensity interrogation[9], phase interrogation[7]. Although other detection techniques are high sensitive but as expensive as atomic absorption spectrometry, inductively coupled plasma mass spectrometry (ICPMS); these instruments are stationary and have complex operation[10]. Researchers studied the SPR based on fiber optics [11] and SPR sensors using smartphone for the portable use [12]. Wavelength modulation and angular modulation

are the most common methods [13] [14] where the latter includes measuring the incident angle of light compared to the surface of the prism.

Surface plasmon resonance can be used for heavy metal ions detection, heavy metals are considered harmful to the environment and organisms [13]. An excess of cadmium and mercury in humans can cause damage to liver and several organ failure, respectively [15]. In addition to, several hazardous effects of lead to humans which transferred through food, air, and water. Excess intake of lead caused incurable blood infections and disorder of the nervous system [2] [16]. SPR sensor is attractive simple and cost-effective method for heavy metal detections.

For SPR generation, the incident light must be in a transverse magnetic mode as the electric field is perpendicular to the metal thin film; under the condition of total internal reflection, surface plasmon was generated by the evanescent wave at the metal and dielectric interface. [17], the propagation constant of the incident light  $k_x$  must be equal to wave vector of surface plasmon  $k_{sp}$  for the surface plasmon excitation to occur, the resonance condition is given by:

$$k_x = k_{sp} \quad (1)$$

$$\frac{\omega}{c} n_{pr} \sin \theta_{SPR} = \frac{\omega}{c} \sqrt{\frac{n_m^2 n_s^2}{n_m^2 + n_s^2}} \quad (2)$$

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Hence, the refractive index of the sample is given by [18] :

$$n_s = \sqrt{\frac{n_m^2 n_{pr}^2 \sin^2 \theta_{SPR}}{n_m^2 - n_{pr}^2 \sin^2 \theta_{SPR}}} \quad (3)$$

Where  $n_{pr}$ ,  $n_m$ , and  $n_s$  are refractive indices of prism, gold layer, and sample, respectively.  $\omega$  is the angular frequency of light.  $c$  is the speed of light.

In this article, simple SPR sensor is built based on Kretschmann structure. The SPR angle ( $\theta_{SPR}$ ) and the optical properties for the heavy metal ions with different concentrations are determined and investigated. Also,  $\theta_{SPR}$  and other parameters were computed according to curve fitting analysis for unknown concentrations. In addition, sensor performance for heavy metal ion detection is discussed.

## 2 Experimental

### 2.1 Materials

Gold layers are deposited on glass substrates ( $25.4 \times 76.2$  mm) with thickness 1-1.2mm with 240s deposition time by sputtering (K550 sputter coater, England). The thickness of gold layer was measured after deposition by electron interference microscope and the average value was 33.5 nm.

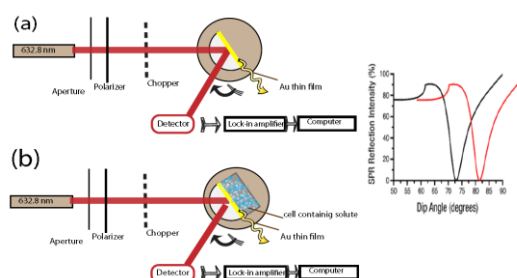
The matching immersion oil was used to contact the Au film to the prism; Prism Dimensions were (diameter 4.9 cm and height of 1.7 cm) and Prism refractive index is 1.518. The prism was used to couple p-polarized light with a thin metal film for excitation of surface plasmons.

A cell, for holding metal solutions, was constructed from glass. One cell side was internally coated with gold film with thickness 33.5 nm. The cell was in contact with prism through the matching oil. There was no inlet and outlet as in the flow cell. The cell was washed by double distilled water after each run of measuring SPR curves. The three different salts of metals were lead nitrate [ $Pb(NO_3)_2$ ], Zinc nitrate [ $Zn(NO_3)_2 \cdot 6H_2O$ ] and, Cadmium nitrate [ $Cd(NO_3)_2 \cdot 4H_2O$ ] were used as the source of Lead, Zinc and Cadmium stock solutions respectively. 1000 ppm stock solutions were prepared from these salts, and then diluted to 100, 250, 500, 750, 850, and 950 ppm. All the required solutions were prepared with analytical reagents and double-distilled water.

### 2.2 Surface plasmon resonance detection

The experimental set up was based on Kretschmann arrangement [19]. The optical system consisted of a He-Ne laser, a glass prism which was mounted on the rotational stage, a polarizer (p-polarised light), and an optical chopper (SR 540) as seen in Fig.1. Gold thin film deposited on one side of glass substrate and the other side was in contact to the prism by matching oil.

The glass / metal interface was illuminated with He-Ne laser ( $\lambda = 632.8$  nm, 5 mW). The reflected intensity was measured as a function of the incident angle; a conservation of energy and wave vector simultaneously were satisfied, a dip in light intensity is observed at the resonance angle ( $\theta_{SPR}$ ). The reflected beam was collected by a large area solar cell (Si) detector and then amplified via a lock-in amplifier (SR 530). From SPR spectrum; the resonance angle  $\theta_{SPR}$  could be determined. Hence, refractive indices calculations were done.



**Fig. 1** Experimental set up for achieving SPR (a) in Air, (b) in metal ion solutions.

The solutions of heavy metal salts were prepared by different concentrations from 100 to 1000 ppm and placed in the sample cell. The solution was in contact to the Au films inside the cell as seen in Fig.1b

Different parameters were determined from spr curves as the resonance angle  $\theta_{SPR}$ , the minimum value of reflected intensity  $I_{min.}$ , maximum reflected intensity  $I_{max.}$  and the angle ( $\theta_{max.}$ ) at which the reflected intensity is of maximum value. The refractive indices were calculated based on the investigated surface plasmon resonance analysis for different metal ions solution.

### 2.3 Sensor performance parameters

Performance parameters [20], [26] of SPR sensor as sensitivity (S), detection accuracy (D.A) and quality factor (Q.F) were calculated and analyzed as a function of metal ion concentrations. Performance of SPR sensors could be deduced based on the three mentioned parameters, where the sensitivity is the ratio of the change in the SPR angle to the change in the refractive index. S measures the ability of sensing the change in refractive index of sensing medium due to the molecules absorption.

$$S = \frac{\Delta \theta_{SPR}}{\Delta n} \quad (4)$$

The detection accuracy : is the ability of monitor the minimum change in the refractive index of the sensing medium. It is measured as the change in the resonance angle to the full width at half maximum FWHM.

$$D.A = \frac{\Delta \theta_{SPR}}{FWHM} \quad (5)$$

Quality factor is the quality of the sensor. It is the ratio of the sensitivity ( $S$ ) to the FWHM. The quality factor depends on  $\Delta\theta_{SPR}$ ,  $FWHM$ ,  $\Delta n$ . It is important factor to qualify the overall sensor performance with respect to the measured parameters.

$$Q.F = \frac{S}{FWHM} \quad (6)$$

Where  $\Delta\theta_{SPR}$  is the shift in SPR angle of salt with respect to that of water,  $FWHM$  is the width at half maximum of SPR curve and  $I_{min}$  is the minimum reflected intensity.

limit of detection (LOD) measures the lowest concentration of ions that the sensor can detect. it can be evaluated by the following equation:

$$LOD = \Delta\theta/S \quad (7)$$

where  $\Delta\theta=0.5^\circ$  is the minimum step of angle measurement and  $S$  is the sensitivity.

### 3 Results and discussions

#### 3.1 Surface plasmon resonance of metallic salt solutions

SPR measurements had been carried out by measuring the reflected p-polarized He-Ne laser intensity (632.8 nm, 5 mW) as a function of the incident angle as discussed in section 2.2. A gold layer was deposited on one side of the glass substrate and the other side are in contact to the prism by matching oil. Prior to metal salt measurements, we investigated the SPR for deposited gold in glass substrate and in the designed cell. The reflected intensity as a function of the incident angle was performed as shown on Fig.2. The SPR curves were the same for the two deposited layers which confirm the stability of the sensing and good quality of the prepared gold films.

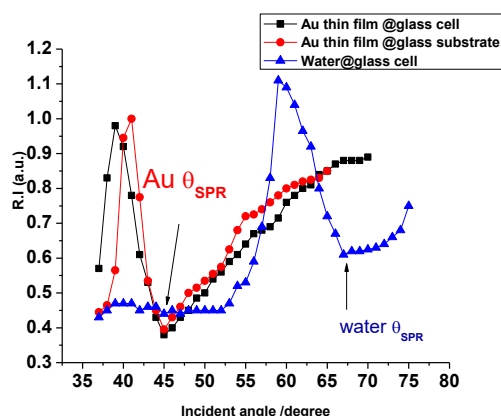


Fig. 2 SPR curves for gold layer on glass substrate, gold layer on the inside wall of the empty sample cell and cell filled with water.

SPR measurements were investigated with double distilled water in constructed cell as seen in Fig. 2. From the resonance angle, the refractive indices of prism, gold

and using equation 3, the calculated refractive index of distilled water  $n_w = 1.29448131 + 0.00981178i$ .

The reflected intensity was studied as a function of the incident angle for ( $Pb^{+2}$ ,  $Cd^{+2}$  and  $Zn^{+2}$ ) in double distilled water at the different concentrations in this section. Figure 3 (a, b, c) shows that the determined resonance angles were  $68.17^\circ$ ,  $67.39^\circ$ ,  $67.05^\circ$  for  $Pb^{+2}$ ,  $Cd^{+2}$ ,  $Zn^{+2}$  at 100 ppm respectively. And the resonance angles are shifted to  $68.99^\circ$ ,  $67.85^\circ$ ,  $67.82^\circ$  at 1000 ppm for the above-mentioned metals, respectively.

From Fig 4, It is shown that  $I_{min}$  of  $Pb^{+2}$ ,  $Cd^{+2}$  and  $Zn^{+2}$  solutions are decreased with increasing concentration from 100 to 1000 ppm for  $Pb^{+2}$ ,  $Cd^{+2}$  and  $Zn^{+2}$  solutions.  $I_{min}$  decreased from  $Zn^{+2}$  to  $Cd^{+2}$  to  $Pb^{+2}$  respectively, this may be due to the difference in atomic weight of  $Zn^{+2}$  to  $Cd^{+2}$  to  $Pb^{+2}$ . Atomic weight of  $Pb^{+2}$  is higher than that of  $Cd^{+2}$  and  $Zn^{+2}$ . The red lines represent the curve fit to the experimental results for  $Pb^{+2}$ ,  $Cd^{+2}$  and  $Zn^{+2}$  solutions. The following equations represent the fitting relations of  $I_{min}$  on the different solutions concentrations of metal ions ( $Pb^{+2}$ ,  $Cd^{+2}$  and  $Zn^{+2}$ ). Consequently  $I_{min}$ , can be determined for any concentration from the calibration curves, Fig 4. The curve fitting of  $I_{min}$  is listed in the following equations.

$$I_{min}Pb^{+2} = 0.631 + 3.872E-5 * C - 9.649E-8 * C^2 \quad (8.1)$$

$$I_{min}Cd^{+2} = 0.642 - 7.692E-6 * C - 1.828E-8 * C^2 \quad (8.2)$$

$$I_{min}Zn^{+2} = 0.663 - 2.736E-5 * C - 1.004E-8 * C^2 \quad (8.3)$$

From Fig.5, the maximum reflected intensity  $I_{max}$  (before the dip of the curve) of  $Pb^{+2}$ ;  $Cd^{+2}$  and  $Zn^{+2}$  solutions are decreased with increasing concentration from 100 to 1000 ppm. The red lines represent the curve fit to the experimental data by the following equations.

$$I_{Rmax}Pb^{+2} = 1.142 - 4.335E-5 * C + 1.325E-8 * C^2 \quad (9.1)$$

$$I_{Rmax}Cd^{+2} = 1.180 + 1.192E-5 * C - 5.712E-8 * C^2 \quad (9.2)$$

$$I_{Rmax}Zn^{+2} = 1.190 - 2.273E-5 * C - 9.622E-9 * C^2 \quad (9.3)$$

While Dependence of  $\theta_{SPR}$  on the metal ions solutions were demonstrated in the Fig. 6.  $\theta_{SPR}$  of  $Pb^{+2}$ ,  $Cd^{+2}$  and  $Zn^{+2}$  solutions were shifted to higher values with increasing metal ion solutions with the same behavior but with different values. The plot also showed that the resonance angle is increased from  $Zn^{+2}$  to  $Cd^{+2}$  to  $Pb^{+2}$  respectively. This was mainly due to the increment number of ions absorbed to the metal surface. The change in the concentration of the samples (metal ion solutions) led to the change in the refractive indices on the surface of the metals which may be due to change in the resonance conditions. Fitting to data were extracted by the following equations.

$$\theta_{SPR}Pb^{+2} = 68.305 - 8.926E-4 * C + 1.536E-6 * C^2 \quad (10.1)$$

$$\theta_{SPR}Cd^{+2} = 67.475 - 4.719E-4 * C + 1.766E-6 * C^2 \quad (10.2)$$

$$\theta_{SPR}Zn^{+2} = 67.111 - 3.966E-4 * C + 1.104E-6 * C^2 \quad (10.3)$$

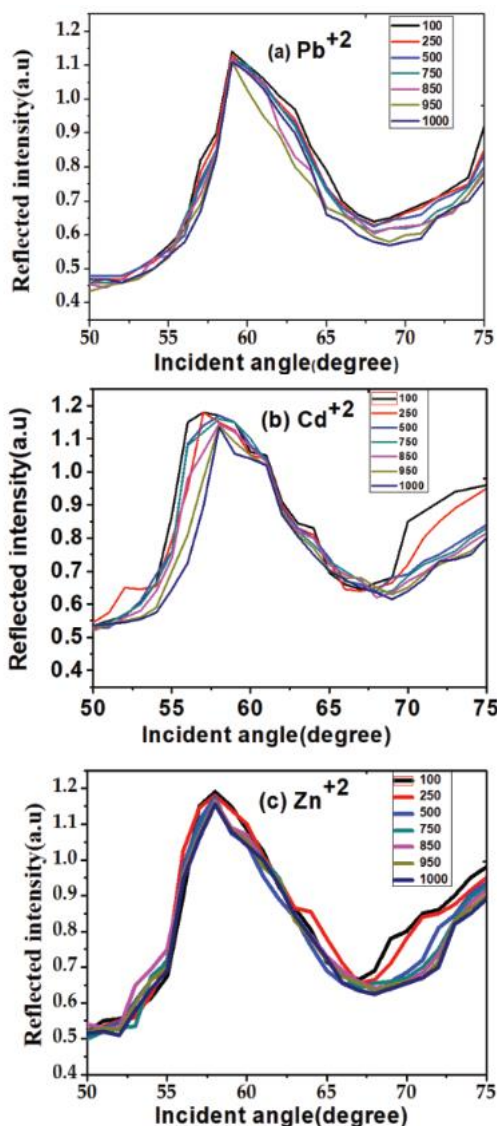


Fig. 3 SPR curves for metal ion solutions (a) Pb<sup>2+</sup>, (b) Cd<sup>2+</sup> and (c) Zn<sup>2+</sup> at different concentrations.

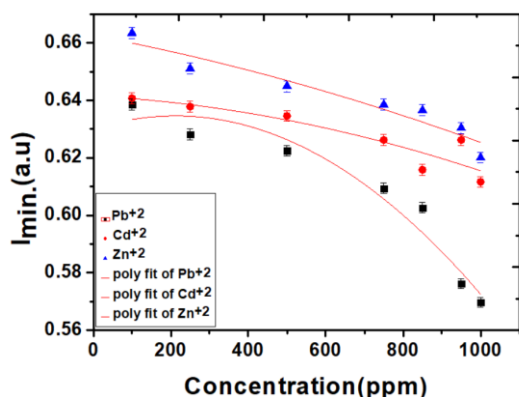


Fig. 4 The polynomial fitting of minimum reflected intensity ( $I_{min}$ ) from SPR curves of Pb<sup>2+</sup>, Cd<sup>2+</sup> and Zn<sup>2+</sup> solutions as a function of metal ion concentrations.

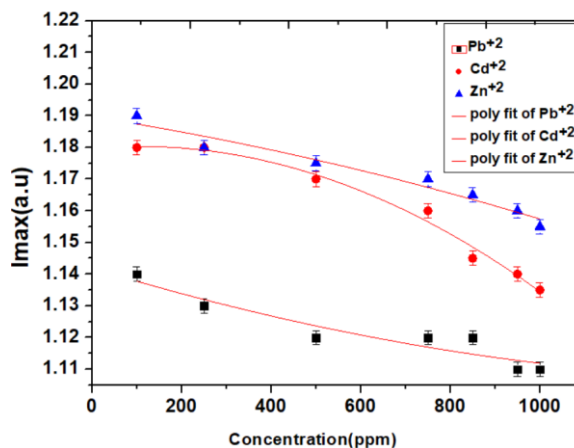


Fig. 5 The polynomial fitting of maximum reflected intensity ( $I_{max}$ ) from SPR curve of Pb<sup>2+</sup>, Cd<sup>2+</sup> and Zn<sup>2+</sup> solutions as a function of metal ions concentrations.

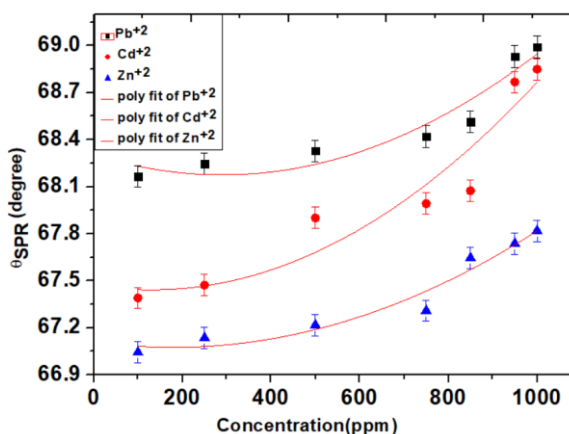


Fig. 6 The polynomial fitting of the resonance angle ( $\theta_{SPR}$ ) from SPR curve of Pb<sup>2+</sup>, Cd<sup>2+</sup> and Zn<sup>2+</sup> solutions as a function of metal ions concentrations.

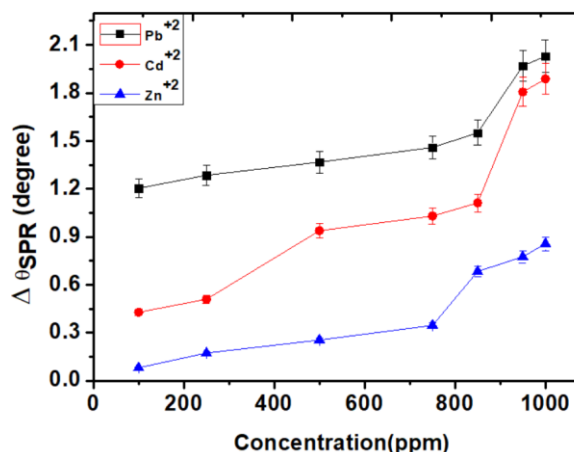


Fig. 7  $\theta_{SPR}$  shift of SPR curves of Pb<sup>2+</sup>, Cd<sup>2+</sup> and Zn<sup>2+</sup> solutions from  $\theta_{SPR}$  of double distilled water as a function of the concentrations of metal ions solutions.



Fig.7 shows that the shift in  $\theta_{\text{SPR}}$  of  $\text{Pb}^{+2}$ ,  $\text{Cd}^{+2}$  and  $\text{Zn}^{+2}$  increased with increasing concentrations. The shift in  $\theta_{\text{SPR}}$  increased from  $\text{Zn}^{+2}$  to  $\text{Cd}^{+2}$  to  $\text{Pb}^{+2}$  respectively; this mainly might be due to the difference of atomic number of these metal ions based on periodic table as mentioned before. Kamaruddin et al [10] mentioned greater shift in SPR angle was observed with metals with higher values of electronegativity  $\text{Pb}^{2+}$  and  $\text{Hg}^{2+}$ . According to Pauling scale of electronegativity, the values of electronegativity of Pb, Cd, Zn are 2.33, 1.69 and 1.65 respectively. This confirmed our results were matched with the previous one and the shift of SPR resonance angle was increased with the increase of electronegativity of metals.

To conclude, SPR experiment was carried out for  $\text{Pb}^{+2}$ ,  $\text{Cd}^{+2}$ ,  $\text{Zn}^{+2}$  from 100 -1000 ppm, for lower concentration less than 100 ppm: the resonance angles remained unchanged from the resonance angle of double distilled water. No significant change in  $\theta_{\text{SPR}}$  for concentrations in the range 0-100 ppm using equation (9). Fig.8 represents the calculation of  $\theta_{\text{SPR}}$  in 0-100 ppm concentrations where these small changes in  $\theta_{\text{SPR}}$  cannot be detected using the current configuration. This might be due to the lower sensor sensitivity. in addition to, small binding interaction to the gold film.

Fen et al [16] recorded similar unchanged in  $\theta_{\text{SPR}}$  from 0.5 to 100 ppm, they attributed this issue a small number of ions existed to be adsorbed in the gold surface in these low concentrations. Danial et al reported no change in SPR resonance angle for Zn concentration (0.1-60 ppm) using the gold thin film which might be attributed to a small binding interaction amount of  $\text{Zn}^{+2}$  with the gold surface. [21], hence they modified the gold layer with a nano-crystalline cellulose-based material to get better sensitivity. The goal of our current worked in progress is to improve the gold thin film with different materials as graphene to enhance the sensor sensitivity.

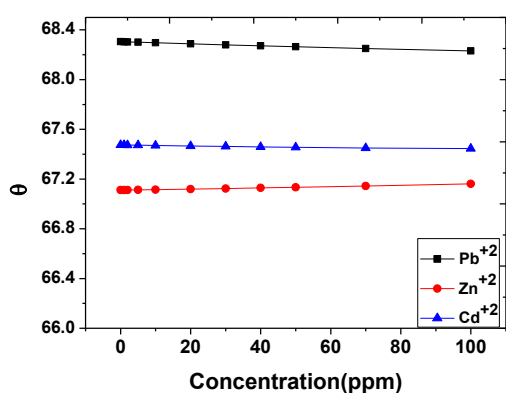


Fig. 8 Calculated  $\theta_{\text{SPR}}$  in the range 0-100ppm according to the fitting equation 9

### 3.2 Real and imaginary parts of refractive indices of metal ion solutions at different concentrations calculated at $\lambda = 632.8 \text{ nm}$

The real and imaginary parts of refractive index of  $\text{Pb}^{+2}$ ,  $\text{Cd}^{+2}$  and  $\text{Zn}^{+2}$  are calculated analytically from resonance angle  $\theta_{\text{SPR}}$  and complex refractive index of gold layer at wave length 632.8 nm in equation (3), The complex refractive index of gold layer (Au) at wave length 632.8 nm is  $0.18377 - 3.4313i$  [22], and the calculated refractive indices parts are represented as a function of concentration in Fig. 9. the real and the imaginary parts of refractive indices are increased with increasing the concentrations of  $\text{Pb}^{+2}$ ,  $\text{Cd}^{+2}$  and  $\text{Zn}^{+2}$  solutions from 100 to 1000 ppm, this is due to with increasing metal ions concentrations in solutions, the resonance angle is shifted to a higher value so refractive index is increased. The real and imaginary parts of refractive indices are increased from  $\text{Zn}^{+2}$  to  $\text{Cd}^{+2}$  to  $\text{Pb}^{+2}$ , as  $\theta_{\text{SPR}}$  of  $\text{Pb}^{+2} > \theta_{\text{SPR}} \text{ Cd}^{+2} > \theta_{\text{SPR}} \text{ Zn}^{+2}$ .

### 3.3 Performance of surface plasmon resonance detection

As mentioned in section 2.3, performance parameters were calculated as sensitivity, detection accuracy and the quality factor of the sensor. Based on spr curves analysis (fig.3) and calculation of the refractive indices, we extract the following parameters as tabled in table 1.  $\Delta\theta$ ,  $\Delta n$  are the change of the SPR angle and the refractive index of metal ion solution with respect to the SPR angle of doubled distilled water. FWHM is the full width at half maximum of surface plasmon resonance angle.

Table 2 summarizes the calculated sensor parameters according to equations 4-6, we noticed a slight variation in the performance parameters for each metal solution, the higher sensitivity was found for  $\text{Pb}^{+2}$  metal ions, this may due to the higher electronegativity value of  $\text{Pb}^{+2}$ . The quality factor has the same range for all measured metal ions in contrast to Detection accuracy D.A of sensor values are increased for  $\text{Pb}^{+2}$  and  $\text{Cd}^{+2}$  more than that of  $\text{Zn}^{+2}$ .

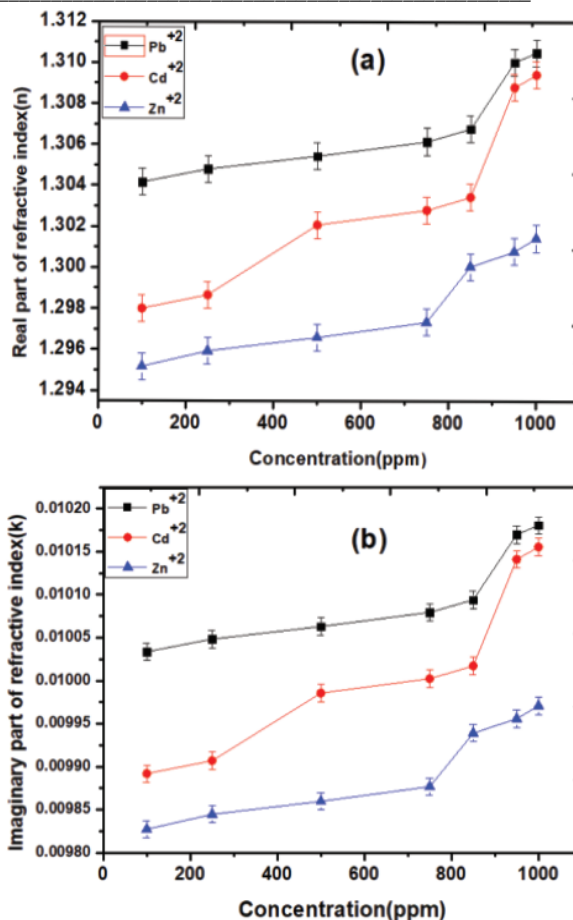
Table 3 show a comparison of this work with others using sensing layers such as gold, silver, and bimetallic silver-gold film. the sensitivity of our sensing layers for  $\text{Pb}^{+2}$  was 124 deg./RIU. this is in a good agreement with other work in Table 3. The SPR sensor is simple and cost effective in comparisons to other metal detection techniques; however, the sensing is limited with angle modulation and the thickness of gold layer. Further improvement to the sensing probes is under investigation; our current work is building SPR sensor via wavelength modulation as optical fiber sensing[23], [24], [25].

Different conventional techniques have been established for sensing heavy metal ions in solution. These techniques consist of atomic absorption spectroscopy (AAS), inductively coupled plasma mass spectrometry (ICPMS), X-ray fluorescence spectrometry (XRF), anodic stripping voltammetry (ASV), and instrumental neutron activation

analysis (INAA). these techniques are listed in Table 4. AAS and ICPMS are destructive and high-cost devices. the other techniques such as XRD, ASV, and INAA are non-destructive techniques. however XRF needs long measuring time, while ASV has low detect limit and severe interference problems but in INAA , samples must be exposed to a neutron flux to produce radioactive nuclides.[26]

Table 5 represents the analytical performance of different analytical techniques for heavy metal ions detection. we calculated the limit of detection according to equation 7. we calculated the limit of detection, linearity, and relative standard deviation RSD. moreover, we compared it to different techniques such as dual electrochemical and colorimetric detection, ASV, XRF, and ICP-PS.

According to fig.7 the linearity range were found to be 100-850, 250-500, 100-750 ppm for  $Pb^{+2}$ ,  $Cd^{+2}$ ,  $Zn^{+2}$ , respectively. these ranges are corresponding to 0.3019-2.66, 0.8104-1.62, 0.336-2.5 mM for  $Pb^{+2}$ ,  $Cd^{+2}$ ,  $Zn^{+2}$  respectively.



**Fig. 9** (a) The real part of refractive index  $n$ , and (b) The imaginary part of refractive index  $k$  as a function of  $Pb^{+2}$ ,  $Cd^{+2}$  and  $Zn^{+2}$  concentrations.

Table 1: The change in surfac plasmon resonance angle  $\Delta\theta$ ,  $\Delta n$  the change of refractive index of metal ions (with respect to distilled water), FWHM,  $I_{min}$  minium intensity for  $Pb^{+2}$ ,  $Cd^{+2}$ ,  $Zn^{+2}$  of different concentrations.

Metal conc.(ppm)	$\Delta\theta_{spr}$			$\Delta n$			FWHM			$I_{min}$		
	$Pb^{+2}$	$Cd^{+2}$	$Zn^{+2}$	$Pb^{+2}$	$Cd^{+2}$	$Zn^{+2}$	$Pb^{+2}$	$Cd^{+2}$	$Zn^{+2}$	$Pb^{+2}$	$Cd^{+2}$	$Zn^{+2}$
100	1.2058	0.43	0.0836	0.00968	0.00352	0.00069	11.07	10.04	11.58	0.6385	0.6407	0.6634
250	1.287	0.51	0.175	0.01032	0.00418	0.00144	9.26	11.67	11.66	0.6304	0.6378	0.6511
500	1.369	0.94	0.257	0.01095	0.0076	0.00211	9.43	12	12.61	0.6224	0.6346	0.6449
750	1.4608	1.03	0.34885	0.01166	0.00832	0.00286	9.45	12.34	12.01	0.6093	0.6262	0.6385
850	1.5425	1.11	0.6855	0.01229	0.00896	0.00557	11.65	12.51	12.35	0.6026	0.6158	0.6366
950	1.9709	1.81	0.777	0.01555	0.01431	0.0063	12.53	13.57	12.53	0.5762	0.6262	0.6304
1000	2.0309	1.89	0.8589	0.016	0.01493	0.00695	10.4671	13.7317	12.4361	0.5697	0.6116	0.62

Table 2 Calculated sensor performance parameters: Sensitivity (s), Detection Accuracy (D.A), and Quality factor (Q.F.)

Metal conc.(ppm)	Sensitivity S			Detection Accuracy (D.A.)			Q.F		
	$Pb^{+2}$	$Cd^{+2}$	$Zn^{+2}$	$Pb^{+2}$	$Cd^{+2}$	$Zn^{+2}$	$Pb^{+2}$	$Cd^{+2}$	$Zn^{+2}$

<b>100</b>	124.566116	122.15909	121.15942	0.1089	0.0428	0.0072	11.2526	12.1672	10.4628
<b>250</b>	124.709302	122.00957	121.52778	0.1390	0.0437	0.0150	13.4675	10.4550	10.4226
<b>500</b>	125.022831	123.68421	121.80095	0.1452	0.0783	0.0204	13.2580	10.3070	9.6591
<b>750</b>	125.283019	123.79808	121.97552	0.1546	0.0835	0.0290	13.2575	10.0323	10.1562
<b>850</b>	125.508544	123.88393	123.07002	0.1324	0.0887	0.0555	10.7733	9.9028	9.9652
<b>950</b>	126.745981	126.48498	123.33333	0.1573	0.1334	0.0620	10.1154	9.3209	9.8430
<b>1000</b>	126.93125	126.59076	123.58273	0.1940	0.1376	0.0691	12.1267	9.2189	9.9374

Table 3 a comparison of SPR sensors performance based Kretschmann configuration.

Sensing layers	Analyte	Real part of refractive index	Imaginary part of refractive index	Sensitivity	ref
gold	Cu <sup>+2</sup> (100-1000ppm)	1.3321-1.3381	0.0042-0.0108		[27]
gold	Pb <sup>+2</sup> (100-1000ppm)	1.3321-1.3388	0.0002-0.0086		[27]
gold	Pb <sup>+2</sup> (0-100) ppm	1.3317-1.3321	0-0.0027		[16]
Ag film, low index prism		1.328-1.332	-	500 deg./RIU	[28]
Au and Si, ZrO <sub>2</sub> thin film		1.325-1.335	-	50-230 deg./RIU	[29]
Bimetallic Ag-Au	Sucrose(0-5%wt)	1.33-1.34		7.85 × 10 <sup>-6</sup> RIU	[30]
Au, Ag metal film		1.33-1.34		100-300 deg./RIU	[31]
gold	Pb <sup>+2</sup> (100-1000ppm)	1.304-1.312	0.0102-0.01018	124 deg./RIU	this work

Table 4: a comparison of spr techniques with other conventional techniques for heavy metal ions detections

Technique	Detection range	Sensitivity	Destructive or not	Cost	measurement time	limitation
atomic absorption spectroscopy (AAS)	Nanomolar range (nM)	High sensitivity	destructive	High cost	long measuring period	working at high temperatures (2,500-3,000°C)
inductively coupled plasma mass spectrometry (ICPMS)	picomolar to nanomolar range (pM-nM)	Very high sensitivity	destructive	Very high cost		complicated sample pretreatment
X-ray fluorescence spectrometry (XRF)	nanomolar to micromolar (nM- $\mu$ M)	Good selectivity	non-destructive		long measuring period	High self-absorption of emitted radiation limiting the analysis of surface layers
anodic stripping voltammetry (ASV)	nanomolar range to micromolar (nM- $\mu$ M)	high sensitivity	non-destructive	low cost		Interferences problem
instrumental neutron activation analysis (INAA).	nanomolar to micromolar (nM- $\mu$ M)	High sensitivity and selectivity	non-destructive			needing nuclear irradiation
SPR spectroscopy	picomolar to micromolar (pM- $\mu$ M)	very high sensitivity	non-destructive	low cost	fast measurement	relatively low selectivity (improving)

Table 5 a Comparison of analytical performance of different analytical techniques for the determination of Pb<sup>+2</sup>Cd<sup>+2</sup>, and Zn<sup>+2</sup>

Spr Kretschmann configuration	Pb <sup>+2</sup>	0.00398	100-850 ppm	0.475	This work
	Cd <sup>+2</sup>	0.00403	250-500 ppm	0.8371	
	Zn <sup>+2</sup>	0.00403 (RIU)	100-750 ppm	0.4639	
dual electrochemical and colorimetric detection	Pb, Cd	0.1 ng/mL			[32]
ASV (microfabricated bismuth (Bi) electrode)	Pb <sup>+2</sup> ,	8ppb	25-400 ppb		[33]

	Cd <sup>+2</sup>	9.4 ppb	28-280 ppb	
ASV	Pb	0.3 µg l <sup>-1</sup>	1-80 µg/L	[34]
ASV	Pb <sup>+2</sup>	0.1 µg/L		
	Cd <sup>+2</sup>	0.1 µg/L		[35]
	Zn <sup>+2</sup>	1 µg/L		
XRF	Pb <sup>+2</sup>	0.71 µg cm <sup>-2</sup>		[36]
	Zn <sup>+2</sup>	0.49 µg cm <sup>-2</sup>		
ICP-MS	Pb <sup>+2</sup>	8.8 ng/L	7.4	[37]
	Cd <sup>+2</sup>	1.7 ng/L	4.6	
AAS	Pb <sup>+2</sup>	0.29 µg/L	4	
	Cd <sup>+2</sup>	0.01 µg/L	2.22	[38]
	Zn <sup>+2</sup>	0.994 µg/L	4.7	

Recent studies are reporting heavy metal ions detection via different techniques and innovative materials[39]–[41]. The role of using nanomaterial with the metallic film for spr enhancement is recently discussed in [42], where several nanoparticles such as gold and silver, magnetic nanoparticles, nanostructures based on graphene and graphene oxide can be applied. They reported the enhancement is due to the coupling between localized surface plasmon resonance LSPR of nanomaterial and the SPR of the metallic film which results in inducing a large electric field on the surface of the nanomaterial and consequently, there will be an increase in spr sensitivity. In our future work, We will fabricate new plasmonic materials for spr enhancement.

#### 4 Conclusions

In this work, we built SPR sensor which is based Kretschmann setup. The sensor is used characterize various heavy metal ion solutions as Pb<sup>+2</sup>, Cd<sup>+2</sup> and Zn<sup>+2</sup>. The resonance angle is shifted to higher values with increasing their content. The optical properties of metal ions solutions Pb<sup>+2</sup>, Cd<sup>+2</sup> and Zn<sup>+2</sup> were calculated analytically using the resonance angle measurements. Both real and imaginary parts of refractive indices of heavy metal ions are increased with increasing concentration. ( $\theta_{SPR}$ ), ( $I_{min}$ ) and ( $I_{max}$ ) were determined for any concentration in the range of the calibration curves using the fitting equations for Pb<sup>+2</sup>, Cd<sup>+2</sup> and Zn<sup>+2</sup> solutions.  $\theta_{SPR}$ ,  $I_{min}$ , and  $I_{max}$  were determined for any concentration in the range of

the calibration curves using the fitting equations for Pb<sup>+2</sup>, Cd<sup>+2</sup> and Zn<sup>+2</sup> solutions. The sensitivity, detection accuracy, and quality factor parameters of proposed SPR sensor were studied; these parameters show good quality of sensor measurements over different metal ions. The sensor is simple and has efficient cost among other sensing techniques. However, the setup is limited with angle modulation and the sensing layer of gold; the enhancement of SPR sensing layers via wavelength modulation is under study.

**Conflicts of Interest:** The authors declare no conflict of interest.

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