



## Optical Demultiplexer by Using In-Line Fiber Filter

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**Abstract-** The signal pulses will be broadened through the fiber and so we need a very sharp cutoff filters with demultiplexers. The in-line fiber filter becomes the appropriate filters. Most of these demultiplexers used after erbium-doped fiber amplifier (EDFA) which need a sharp wavelength bandpass filter (BPF) to filter out wavelengths other than the signal wavelength

Exact analysis of in-line fiber filter is occurred by derive a polynomial expression for the dopant ratios of GeO<sub>2</sub> and P<sub>2</sub>O<sub>5</sub>. The refractive index of silica doped either GeO<sub>2</sub> or P<sub>2</sub>O<sub>5</sub> is defined as a function of both the wavelength and the dopant ratio. The calculations of the dopant ratios of the pair materials (GeO<sub>2</sub> and P<sub>2</sub>O<sub>5</sub>) are done at a specific filter cutoff wavelength ( $\lambda_c$ ) for both high pass filter (HPF) and low pass filter (LPF). Two in-line fiber filters (HPF and LPF) are cascaded to make a sharp bandpass filter (BPF).

The length of in-line fiber filter must be very short to overcome the weak of the propagation constant through it.

The normalized frequency is discussed. A theoretical 8-channels demultiplexer is done. The design of demultiplexer becomes very easy.

**Keywords:** In-line fiber filter, Germanosilicate, Phosphosilicate, bandpass filter and demultiplexer.

### I. INTRODUCTION

Demultiplexer split the mixed light up into many mixed outputs (one per required output power) and then filter each port individually. There are several searches published about multiplexer/demultiplexers [1-6,7]. The signal pulses will be broadened [6] and so we need a very sharp cutoff filters with demultiplexers [8-10]. Light at a specific wavelength is filtered out of a single-mode fiber. The in-line fiber filter [8] becomes the appropriate filters. Most of these demultiplexers used after erbium-doped fiber amplifier (EDFA) which need a sharp wavelength bandpass filter (BPF) to filter out wavelengths other than the signal wavelength [11]. EDFA with operating wavelength ranged from 1540 nm to 1570 nm [11] or from 1525 nm to 1565 nm [12] or from 1570 to 1610 nm [12].

There are several techniques for optical filters [13-21]. Fiber filters have been widely used to achieve dynamic wavelength filtering in the fields of optical communication [16]. Fiber-optic filter is an optical fiber instrument used for wavelength selection, which can select desired wavelengths to pass and reject the others. It is widely used in DWDM systems dynamic wavelength selection [18]. An in-line fiber-optic bandpass wavelength filter has been demonstrated based on a single-mode fiber [19]. New types of in-line fiber filters whose core and cladding are composed of binary silica doped with either boron or fluorine are proposed. Utilizing dispersive characteristics of SiO<sub>2</sub>-B<sub>2</sub>O<sub>3</sub> and SiO<sub>2</sub>-F systems [20]. The fabrication of narrowband highly reflecting filters in single-mode step-index fibers [21]

The idea of in-line fiber filter based upon that, the difference between the refractive indexes of the silica doped material of the core and the silica doped material of the cladding. This difference is a function of both the wavelength and the dopant ratio of materials. The sign of this difference changes from negative to positive values and vice versa. The filter cutoff wavelength ( $\lambda_c$ ) is the wavelength at which the difference equals zero.

The dopants of both the core and the cladding must be from materials which increasing the refractive index of the silica such as germania (GeO<sub>2</sub>) and phosphorus pentoxide (P<sub>2</sub>O<sub>5</sub>). Also, from materials which decreasing the refractive index of the silica such as fluorine (F) and boron (B<sub>2</sub>O<sub>3</sub>). But in our study the GeO<sub>2</sub> and P<sub>2</sub>O<sub>5</sub> are used.

The refractive index of the pure silica ( $n_s$ ), the refractive index of germanosilicate ( $n_{sg}$ , silica doped  $GeO_2$ ) and the refractive index of phosphosilicate ( $n_{sp}$ , silica doped  $P_2O_5$ ) are functions upon the operating wavelength ( $\lambda$ ) and the dopant ratios ( $x_1$ ) of  $GeO_2$  and ( $x_2$ ) of  $P_2O_5$ . The rate of change of both  $n_{sg}$  and  $n_{sp}$  with wavelength are not equally. And so, the difference value between  $n_{sg}$  and  $n_{sp}$  ( $\Delta n_{sg\ sp} = n_{sg} - n_{sp}$ ) can change from a positive value into a negative value (or vice versa) according to the operating wavelength ( $\lambda$ ). The wavelength at which  $n_{sg} = n_{sp}$  is called the cutoff wavelength of the fiber ( $\lambda_c$ ). At  $\lambda = \lambda_c$ , the fiber propagation constant becomes zero ( $\beta = 0$ ), therefore, the optical fiber operates at wavelengths that make the difference  $\Delta n_{sg\ sp}$  positive. And so, the fiber acts as a filter.

In-line fiber filter uses as an optical filter (either high pass filter, HPF, or low pass filter, LPF). And by using two cascaded filters, HPF and LPF, the final bandpass filter (BPF) is designed.

The filter becomes low pass filter (LPF) if the passband wavelengths smaller than  $\lambda_c$  (in this case  $\lambda_c$  is named  $\lambda_{cL}$ ). While the filter becomes high pass filter (HPF) if the passband wavelengths greater than  $\lambda_c$  (in this case  $\lambda_c$  is named  $\lambda_{cH}$ ). The bandpass filter (BPF) with bandpass limits ( $\lambda_{cL}$  to  $\lambda_{cH}$ ) consists of HPF with cutoff  $\lambda_{cH}$  cascaded by LPF with cutoff  $\lambda_{cL}$ . The materials of in-line fiber filter are germanosilicate (core) and phosphosilicate (cladd) for LPF, and vice versa for HPF as shown in Fig.1.

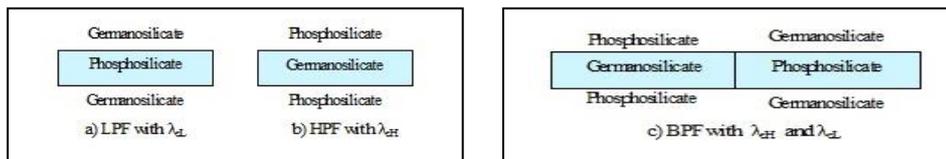


Fig.1 Structure of LPF, HPF and BPF

**In this work** : the pair of dopant materials ( $GeO_2$  and  $P_2O_5$ ) is studied. The values of these dopant ratios are calculated for LPF, HPL and BPF with different specific filter cutoff wavelengths. The normalized frequency is discussed. Theoretically design example of BPF and demultiplexer are done for 8-channels.

## II. Mathematical Analysis and Numerical Results With Discussions

### II.1. Refractive index

Due to the importance of the refractive index in this work, the different formulas which used to find the refractive index are discussed.

Germanosilicate  $\{x_1 GeO_2 + (1-x_1) SiO_2\}$  has refractive index ( $n_{sg}$ ) with dopant ratio  $x_1$ . Where Germania ( $GeO_2$ ) is an optional, but very effective component for forming a network structure and increasing the refractive index of the silica. The preferred range of  $GeO_2$  is 0 to 12.0 %. [22].

Phosphosilicate  $\{x_2 P_2O_5 + (1-x_2) SiO_2\}$  has refractive index ( $n_{sp}$ ) with dopant ratio  $x_2$ . Where Phosphorus pentoxide ( $P_2O_5$ ) is an essential component for the optical glass according to the present invention and a main component for forming a network structure of the glass, and increasing the refractive index of the silica. The preferred range of  $P_2O_5$  is 15.0 to 30.0 %. [22].

The above preferred ranges of the dopant ratios are as indicative values for the fiber as a filter but it becomes necessary for material dispersion.

Silica ( $SiO_2$ ) is a material of considerable technological important, with broad application devices containing optical fiber [23].

There are different published formulas for the index dispersion ( $n$ ) at main values of the dopant ratio [24-28]. But we need a formula which gives the index dispersion as a function of dopant ratio (i.e. refractive index as a function of both wavelength,  $\lambda$ , and the dopant ratio,  $x$ ).

#### II.1.1 For Germanosilicate : $x_1 GeO_2 + (1-x_1) SiO_2$

The refractive index of Germanosilicate ( $n_{sg}$ ) is determined from the following two equations.

The first equation is [29]; (Sellimere formula 1)

$$n^2 = 1 + \frac{a_1 \lambda^2}{\lambda^2 - b_1^2} + \frac{a_2 \lambda^2}{\lambda^2 - b_2^2} + \frac{a_3 \lambda^2}{\lambda^2 - b_3^2} \quad (1)$$

Where; [30]

$$\begin{aligned} a_1 &= a_{10} + u_1 x_1, & b_1 &= b_{10} + v_1 x_1, & a_2 &= a_{20} + u_2 x_1, & b_2 &= b_{20} + v_2 x_1, \\ a_3 &= a_{30} + u_3 x_1, & b_3 &= b_{30} + v_3 x_1, & a_{10} &= 0.6961663, & b_{10} &= 0.0684043 \\ a_{20} &= 0.4079426, & b_{20} &= 0.1162414, & & & & \\ a_{30} &= 0.8974794, & b_{30} &= 9.89616087, & u_1 &= 0.110700, & v_1 &= 0.000568306, \\ u_2 &= 0.31021588, & v_2 &= 0.03772465, & u_3 &= -0.04331091, & v_3 &= 1.94577 \end{aligned}$$

The second equation is [27, 28]; (Sellimere formula 2)

$$n^2 = 1 + \frac{a_1 \lambda^2}{\lambda^2 - b_1^2} + \frac{a_2 \lambda^2}{\lambda^2 - b_2^2} \tag{2}$$

Where the values of  $a_1, a_2, b_1$  and  $b_2$  are derived from [28] as;

$$a_1 = \frac{14.71 + 0.78 x_1}{13.38 - 3.58 x_1}, \quad b_1 = \frac{c_1}{13.38 - 3.58 x_1}, \quad a_2 = \frac{0.11251 - 0.14 x_1}{0.12536 - 0.01236 x_1}, \quad b_2 = \frac{c_1}{0.12536 - 0.01236 x_1}$$

$$c_1 = \frac{h c}{e} = \frac{6.625 \times 10^{-34} \times 3 \times 10^8}{1.602 \times 10^{-19}} = 1.24082397 \text{ (ev } \mu\text{m)} \tag{3}$$

The values of  $a_1, a_2, b_1$  and  $b_2$  for  $\text{SiO}_2$  are defined by putting  $x_1 = 0$  into Eq.(2.b).

II.1.2. For Phosphosilicate:  $x_2 \text{P}_2\text{O}_5 + (1-x_2) \text{SiO}_2$

The refractive index of Phosphosilicate ( $n_{sp}$ ) is evaluated from Eq.(2). Where the values of  $a_1, a_2, b_1$  and  $b_2$  are derived from [28] as;

$$a_1 = \frac{14.71 + 18.27 x_2}{13.38 + 14.3 x_2}, \quad b_1 = \frac{c_1 (1+x_2)}{13.38 - 3.58 x_2}$$

$$a_2 = \frac{0.11251 + 0.09251 x_2 - 0.02 x_2^2}{0.12536 + 0.18464 x_2}, \quad b_2 = \frac{c_1 (1+x_2)}{0.12536 + 0.18464 x_2} \tag{4}$$

II.2. Comparison between refractive index which evaluated by Eq.(1) and by Eq.(2)

II.2.1. Refractive indexes of  $\text{SiO}_2, \text{GeO}_2$  and  $\text{P}_2\text{O}_5$ ,

Which are calculated by Eq.(1),  $n_{s1}, n_{g1}$  and  $n_{p1}$ , and by Eq.(2),  $n_{s2}, n_{g2}$  and  $n_{p2}$ , are shown in Fig.(2). Refractive index From Eq.(1) either greater or less than that by Eq.(2).

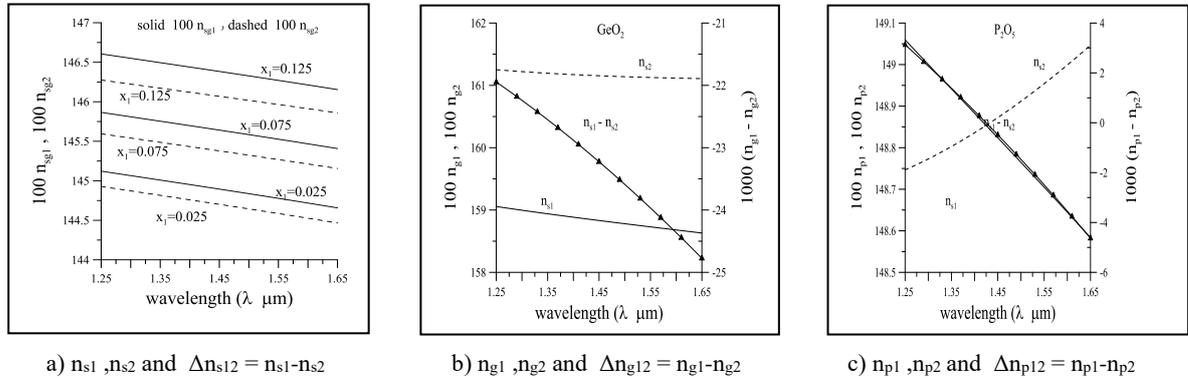


Fig.2 Comparison between Eq.(1) and Eq.(2) for  $\text{SiO}_2, \text{GeO}_2$  and  $\text{P}_2\text{O}_5$   
Coefficients of Eq.(1.a),  $a_1 \rightarrow a_3$  and  $b_1 \rightarrow b_3$ , for  $\text{SiO}_2, \text{GeO}_2$  and  $\text{P}_2\text{O}_5$  are indicated in Table (A.1)

II.2.2 Refractive index of Germanosilicate

Which calculates by Eq.(1),  $n_{sg1}$ , and from Eq.(2),  $n_{sg2}$ , with  $\lambda = 1.25 \mu\text{m}$  to  $1.65 \mu\text{m}$  and  $x_1 = 0.025, 0.075$ , and  $0.125$  is shown in Fig.(3.a).

The difference  $\Delta n_{sg12}$  ( $\Delta n_{sg12} = n_{sg1} - n_{sg2}$ ) increases with  $x_1$  but it decreases with  $\lambda$  (Fig.3.b). We also can show that, the difference ( $\Delta n_{sg12} - \Delta n_{s12}$ ) not constant with  $\lambda$  (Fig.3.c).

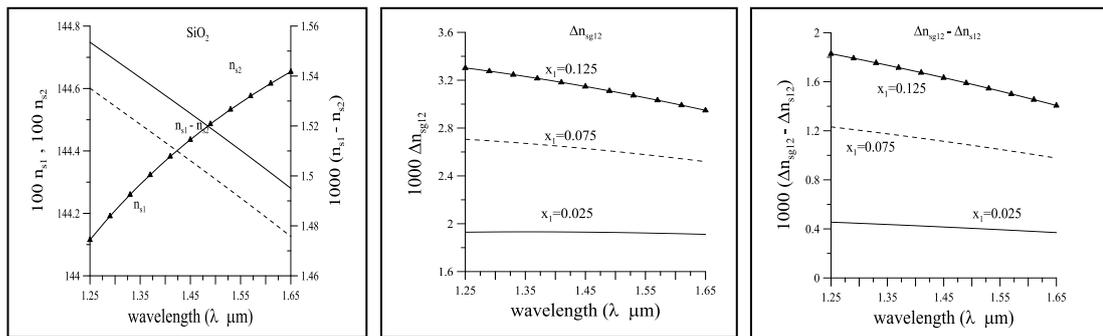


Fig.3: Comparison between Eq.(1) and Eq.(2) for Germanosilicate with  $x_1 = 0.025, 0.075$  and  $0.125$

II.2.3 Accuracy of Eq.1 for Germanosilicate

The difference between refractive index of Germanosilicate by Eq.(1),  $n_{sg\ eq1}$ , and from published coefficients,  $a_1 \rightarrow a_3$  and  $b_1 \rightarrow b_3$  (Table A.2), at special values of  $x_1$  ( $n_{sg\ pb}$ ) is denoted by  $\Delta n_{sg\ pb\ eq} = n_{sg\ pb} - n_{sg\ eq1}$ . This difference ( $\Delta n_{sg\ pb\ eq}$ ) is indicated in Table (A.3) which gives that Eq.(1) with some values of  $x_1$  does not accurate. But there isn't any other option which can be used as a general equation for Germanosilicate.

II.2.4 Accuracy of published data for Phosphosilicate at  $x_2=9.1\%$  and  $x_2 = 10.5\%$

Published coefficients of Eq.(1) for Phosphosilicate (Table A.4) at  $x_2= 9.1\%$  [31] are not corecte. Where  $n_{sp1}$  (with  $x_2= 9.1\%$ ) greater than  $n_{sp1}$  (with  $x_2 = 10.5\%$ ) (Fig.A.1), and so, these coefficients are rejected.

III In-line Fiber Filter With the Pair of Germanosilicate and Phosphosilicate

Due to the difference between the rate of changes of  $n_{sg}$  and  $n_{sp}$  with respect to  $\lambda$ , there is a specific wavelength (filter cutoff wavelength,  $\lambda_c$ ) at which  $n_{sg} = n_{sp}$  with main dopant values  $x_1$  and  $x_2$ .  $r$  are equals at  $\lambda_c$ .

III.1 Claculation of  $x_1$  corresponding to  $x_2$  from Eq.(2),

For Germanosilicate , Eq.(2) is converted into the following polynomial equation;

$$A_0 + A_1x_1 + A_2x_1^2 + A_3x_1^3 + A_4x_1^4 = 0 \tag{5}$$

Where; the coefficients  $A_0 \rightarrow A_4$  depend upon the parameters  $\lambda_c$ ,  $n_{sg}$ , and  $a_1, a_2, b_1$  and  $b_2$  from Eq.(3). Therefore with main values of  $\lambda_c$  and  $x_2$  the value of  $n_{sp}$  is evaluated from Eq.(2) and by putting  $n_{sg} = n_{sp}$ , the corresponding value of  $x_1$  is the root of Eq.(5), where  $0 < x_1 < 1$ .

III.2 Claculation of  $x_2$  corresponding to  $x_1$  from Eq.(2)

For Phosphosilicate, Eq.(2) converted into the following polynomial equation;

$$B_0 + B_1x_2 + B_2x_2^2 + B_3x_2^3 + B_4x_2^4 + B_5x_2^5 = 0 \tag{6}$$

Where; the coefficients  $B_0 \rightarrow B_5$  depend upon the constants inside the parameters  $\lambda_c$  and  $n_{sp}$ , and  $a_1, a_2, b_1$  and  $b_2$  from Eq.(4). Therefore with main values of  $\lambda_c$  and  $x_1$  the value of  $n_{sg}$  is evaluated from Eq.(2) and by putting  $n_{sp} = n_{sg}$ , the value of  $x_2$  is the root of Eq.(6), where  $0 < x_2 < 1$ .

III.3 Claculation of  $x_1$  corresponding to  $x_2$  from Eq.(1),

For Germanosilicate Eq.(1) can be converted into the following polynomial equation

$$C_0 + C_1x_1 + C_2x_1^2 + C_3x_1^3 + C_4x_1^4 + C_5x_1^5 + C_6x_1^6 = 0 \tag{7}$$

Where; the coefficients  $C_0 \rightarrow C_6$  depend upon the values of  $\lambda_c$  and  $n_{sg}$ , and  $a_{10} \rightarrow a_{30}, b_{10} \rightarrow b_{30}, u_1 \rightarrow u_3$  and  $v_1 \rightarrow v_3$  from Eq.(1). Therefore with main values of  $\lambda_c$  and  $x_2$  the value of  $n_{sp}$  is evaluated from Eq.(1) with coefficients from Table (A.3) and by putting  $n_{sg} = n_{sp}$ , the value of  $x_1$  is the root of Eq.(7), where  $0 < x_1 < 1$ .

As expected the value of  $x_1$  increases with the value of  $x_2$  (Fig.4.a) also  $x_2$  increases with  $x_1$  (Fig.4.b). Also, the required values of  $x_2$  usually greater than the corresponding values of  $x_1$  (i.e.  $GeO_2$  increases the index of  $SiO_2$  more than  $P_2O_5$ ) and the ratio of  $x_2$  to  $x_1$  increases with  $x_2$ . The pair of  $x_2$  and  $x_1$  is coincide with the pair  $x_1$  and  $x_2$  (Fig.4.c).

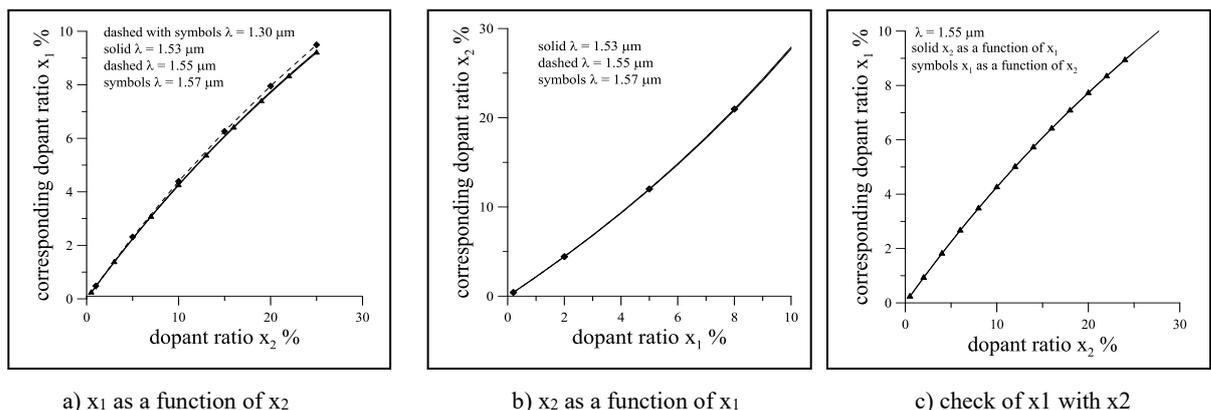


Fig.4 Values of  $x_2$  (corresponding to  $x_1$ ) and the value  $x_1$  (correspondind to  $x_2$ ) by Eq.2

The values of both  $x_2$  and the corresponding values of  $x_1$  are in invers relationship with filter cutoff wavelength,  $\lambda_c$ , (Fig.4). Also, the dependence of  $x_1$  or  $x_2$  on wavelength is very little.

As a numerical example of in-line fiber filter with cutoff wavelength ( $\lambda_c = 1.30\mu\text{m}$ ) the values of pairs  $x_1$  and  $x_2$  can be are ( $x_2 = 0.05$  and  $x_1 = 0.02318144$ ) or ( $x_2 = 0.15$  and  $x_1 = 6.263270$ ). But with  $\lambda_c = 1.55\mu\text{m}$ , the values of these pairs become ( $x_2 = 0.05$  and  $x_1 = 0.0224478$ ) or ( $x_2 = 0.15$  and  $x_1 = 0.06064417$ ) (Fig.4).

The in-line fiber filter becomes high pass filter (HPF) with fiber core (Germanosilicate ) and fiber cladding (Phosphosilicate ) and vice versa for low pass filter (LPF) (Fig.5). The bandpass filter (BPF) is structured from cascaded highpass filetr by lowpass filter

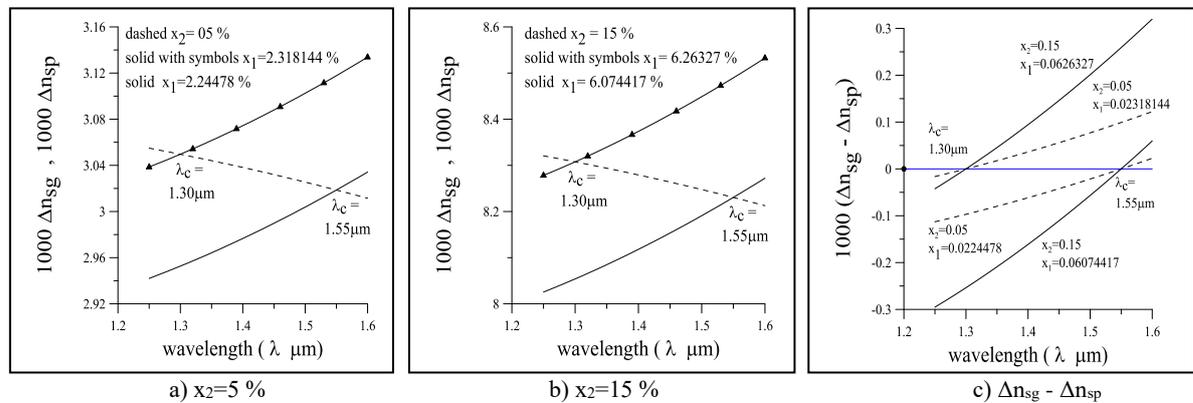


Fig.5 The cutoff wavelength ( $\lambda_c$ ) and the corresponding pair values of  $x_2$  and  $x_1$  ( $\Delta n_{sg} = n_{sg} - n_s$  and  $\Delta n_{sp} = n_{sp} - n_s$ )

**IV Theoretical Application : In-Line Fiber BPF (after EDFA) and Demultiplexer**

BPF is a micro optics device [32] and it is used with DWDM system and after EDFA. It is consists of HPF cascaded by LPF.

Number of chaneels, bandwidth of each channel and the guard between the channels of the demultiplexers depend upon the applied system. Such as 8-channels (200 GHz bandwidth,  $\lambda=1471 \rightarrow 1611$  nm, 1.6 nm band, 0.4 nm guard) [33], ITU-T currently recommends 81-channels (25 GHz bandwidth,  $\lambda = 1528.77 \rightarrow 1560.17$  nm, 0.2 nm band, 0.19 nm guard) [34], and 8-channels (200 GHz bandwidth, with band =1.6nm, spacing =1.61 nm, and guard= 0.01nm) [2] Table (1).

Table 1: The limits of 8-channels demultiplexer ( $\lambda = 1540.5 \rightarrow 1553.37$  nm, with band =1.6 nm and spacing = 1.61 nm) [2]

Ch.	1	2	3	4	5	6	7	8
$\lambda_s$	1540.50	1542.11	1543.72	1545.33	1546.94	1548.55	1550.16	1551.77
$\lambda_e$	1542.10	1543.71	1545.32	1546.93	1548.54	1550.15	1551.76	1553.37

The special available value of  $x_2 = 10.5\%$  (Table A.4) is used to apply both Eq.(1) and Eq.(2).

- In-Line Fiber BPF after EDFA*, to pass 8-channels, from Table (1);  
 $\lambda_{cHPF} = 1540.50$  nm so  $x_1 = 4.491799$  with Eq.(1), but  $x_1 = 4.453913$  with Eq.(2)  
 $\lambda_{cLPF} = 1553.37$  nm so,  $x_1 = 4.490390$  with Eq.(1), but  $x_1 = 4.445769$  with Eq.(2).
- In-Line Fiber BPFs to demultiplex 8- channels*,(Fig.6) and Table (1); the values of  $x_1$  for 8 LPF and 8 HPF (i.e. 8 BPF) are calculated from Eq.(1) (Table 2) and from Eq.(2) and (Table 3) with  $x_2 = 10.5\%$ .

Figure 7 obveuses  $\Delta n_{sg}$  and  $\Delta n_{sp}$  for 8 BPFs with Eq.(1) and Eq.(2).

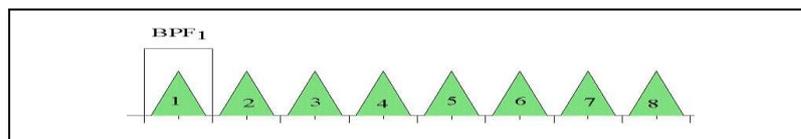


Fig.6 A 8-channels demultiplexer

Table 2: The ratios of GeO<sub>2</sub> % for the 8-channels demultiplexer with P<sub>2</sub>O<sub>5</sub> =10.5% either core or cladding (\* clad and \*\* core) Eq.(1)

Ch.	1	2	3	4	5	6	7	8
HPF *	4.491799	4.491624	4.491448	4.491272	4.491096	4.490920	4.490743	4.490566
LPF **	4.491625	4.491449	4.491274	4.491097	4.490921	4.490744	4.490567	4.490390

Table 3: The ratios of GeO<sub>2</sub> % for the 8-channels demultiplexer with P<sub>2</sub>O<sub>5</sub> =10.5% either core or cladding (\* clad and \*\* core) Eq.(2)

Ch.	1	2	3	4	5	6	7	8
HPF *	4.453913	4.452899	4.451883	4.450867	4.449848	4.448829	4.447808	4.446786
LPF **	4.452905	4.451890	4.450873	4.449855	4.448835	4.447814	4.446792	4.445769

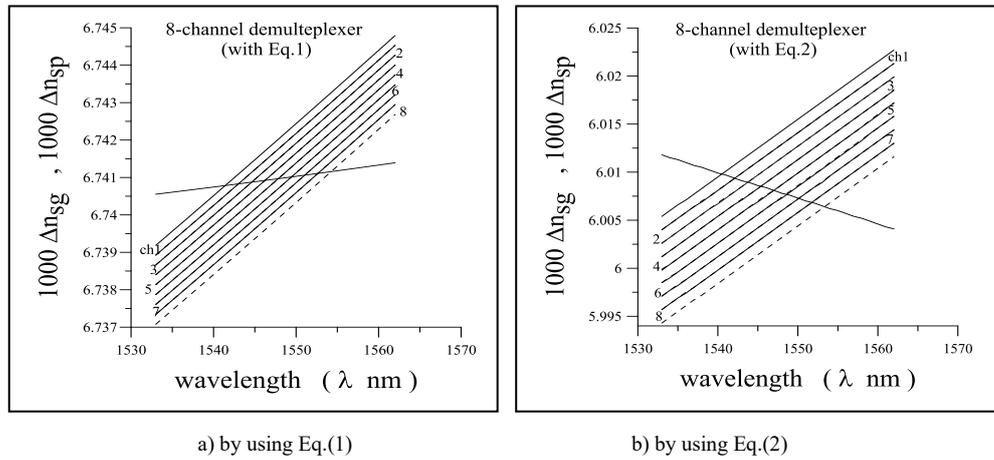


Fig.7 8-channels demultiplexer by applied both Eq.(1) and Eq.(2)

We must be noticed that, with any value of  $x_2$ , the corresponding value of  $x_1$  by Eq.(1) differs with that calculated from Eq.(2) because the value of  $n_{s1} > n_{s2}$  and  $n_{sp1} \neq n_{sp2}$ .

To indicate that, with the available value of  $x_2 = 0.105$ , the corresponding value of  $x_1 = 0.04514289$  from Eq.(1) and  $x_1 = 0.04589308$  from Eq.(2) with  $\lambda = 1.30\mu\text{m}$ . Also,  $x_1 = 0.04490761$  from Eq.(1) and  $x_1 = 0.04447910$  from Eq.(2) with  $\lambda = 1.55\mu\text{m}$ . Where  $n_{sp1} = 1.453656$  and  $n_{sp2} = 1.451497$  ( $\lambda = 1.30\mu\text{m}$ ), and  $n_{sp1} = 1.450765$  and  $n_{sp2} = 1.448502$  ( $\lambda = 1.55\mu\text{m}$ ).

If we take in account of  $x_1$  the difference between  $n_{s1}$  and  $n_{s2}$  ( $\Delta n_{s12} = n_{s1} - n_{s2}$ ) the values of  $x_1$  become;  $x_1 = 0.03516976$  at  $\lambda = 1.30\mu\text{m}$  (where,  $\Delta n_{s12} = 0.00148610$ ), and  $x_1 = 0.03470022$  at  $\lambda = 1.55\mu\text{m}$  (where,  $\Delta n_{s12} = 0.0015293$ ). Then, the results from Eq.(2) not equal with that from Eq.(1).

Also, if we take in account of  $x_1$  the difference between  $n_{sp1}$  and  $n_{sp2}$  ( $\Delta n_{sp12} = n_{sp1} - n_{sp2}$ ), the values of  $x_1$  become;

$x_1 = 0.03065721$  at  $\lambda = 1.30\mu\text{m}$  (where  $\Delta n_{sp12} = 0.002159$ ), and  $x_1 = 0.02980713$  at  $\lambda = 1.55\mu\text{m}$  (where,  $\Delta n_{sp12} = 0.002263$ ). Then, the results from Eq.(2) not equal with that from Eq.(1).

### V Normalized Frequency (v) of In-Line Fiber Filter

At cut-off wavelength, the corresponding normalized frequency (v) equals zero and the value of v increases with wavelengths apart from  $\lambda_c$  toward the active region of the filter (Fig.6). But, v stills very low, and so, the propagation constant is very weak. To increase the value of v, we need a large core radius of filter within single mode ( $v < 2.4$ ). In this case, the splicing between the filter and the fiber link becomes difficult because the core radius of filter ( $a_{\text{filter}}$ ) very large than the core radius of fiber link ( $a_{\text{link}}$ ).

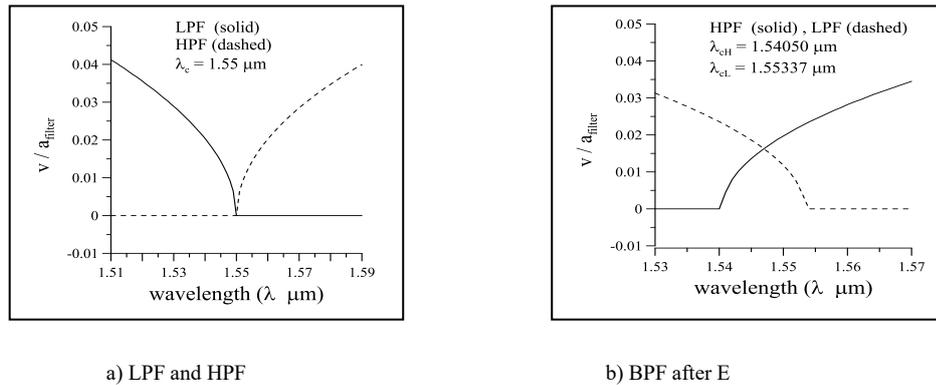


Fig.6 Normalized frequency ( $v$ ) as a function of wavelength ( $\lambda$ ). Where  $a_{\text{filter}}$  is the core radius

As example for BPF with bandwidth from  $\lambda = 1540.50\text{nm}$  to  $\lambda = 1553.37\text{nm}$  (Fig.6.b), the maximum value of  $v = 0.0163a_{\text{filter}}$  and it occurs at  $\lambda = 1547.1\text{ nm}$ . So, with single mode,  $a_{\text{filter}}$  can be reach  $147\mu\text{m}$  and so, the radius  $a_{\text{filter}}$  can be 30 times  $a_{\text{link}}$  ( $a_{\text{link}}$ , approximately  $5\mu\text{m}$ ). Therefore the maximum additional splicing losses due to the ratio  $a_{\text{filter}} / a_{\text{link}}$  becomes  $14.77\text{dB}$  (where, splicing losses =  $10\log(a_{\text{filter}} / a_{\text{link}})$ ).

Finally, the length of the in-line fiber filter must be very short to overcome the very small propagation constant through it.

## VI. CONCLUSION

Exact analysis of in-line fiber filter is occurred by derive a polynomial expression for the dopant ratio of  $\text{GeO}_2$  or  $\text{P}_2\text{O}_5$ . The in-line fiber high pass filter (HPF) consists of Phosphosilicate (core) and Germanosilicate (cladding) and vice versa for the in-line low pass filter (LPF).

For each specific filter cutoff wavelength ( $\lambda_c$ ) there is one value of dopant ratio of the core correlated with that of the cladding. The in-line fiber BPF is constructed by cascaded the in-line fiber HPF and the in-line LPF.

The length of in-line fiber filter must be very short to overcome the weak of the propagation constant through it. The design of the demultiplexer becomes very easy. The refractive indices of BPFs which are used for 8-channels demultiplexer are evaluated.

The dopants of both the core and the cladding must be from materials which increasing the refractive index of the silica such as germania ( $\text{GeO}_2$ ) and phosphorus pentoxide ( $\text{P}_2\text{O}_5$ ). Also, from materials which decreasing the refractive index of the silica such as fluorine (F) and boria ( $\text{B}_2\text{O}_3$ ).

The normalized frequency ( $v$ ) of the in-line fiber filter is very small so, the corresponding propagation constant becomes very weak.

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Appendix A

Table A.1: Sellmeier's Coefficients of Eq.(1),  $a_1 \rightarrow a_3$  and  $b_1 \rightarrow b_3$  for  $SiO_2$ ,  $GeO_2$  and  $P_2O_5$

	$a_{1\text{ sg pb}}$	$a_{2\text{ sg pb}}$	$a_{3\text{ sg pb}}$	$b_{1\text{ sg pb}}$	$b_{2\text{ sg pb}}$	$b_{3\text{ sg pb}}$	references
$SiO_2$	0.6961663	0.4079426	0.8974794	0.0684043	0.1162414	9.89616087	[8,24,35]
$GeO_2$	0.80686642	0.71815848	0.85416831	0.069972606	0.15996605	11.841931	[27]
$P_2O_5$	0.78838154	0.43993784	0.87648797	0.103867	0.08992564	9.89616572	[24]

Table A.2: Sellmeier's Coefficients of Eq.(1),  $a_1 \rightarrow a_3$  and  $b_1 \rightarrow b_3$  for Germanosilicate at special values of  $x_1$

$x_1$	$a_{1\text{ sg pb}}$	$a_{2\text{ sg pb}}$	$a_{3\text{ sg pb}}$	$b_{1\text{ sg pb}}$	$b_{2\text{ sg pb}}$	$b_{3\text{ sg pb}}$	
0.030	0.7052977	0.4111432	0.8717021	0.0780876	0.1256396	9.896154	[27]
0.031	0.7028554	0.4146307	0.8974540	0.0727723	0.1143085	9.896161	[35]
0.035	0.7042038	0.4160032	0.9074049	0.0514415	0.12916	9.896156	[31]
0.041	0.68671749	0.43481505	0.89656582	0.072675189	0.11514351	10.002398	[31]
0.058	0.7088876	0.4206803	0.8956551	0.0609053	0.1254514	9.896162	[35]
0.063	0.7083952	0.4203993	0.8663412	0.08538421	0.10248385	9.89617501	[24]
0.070	0.6869829	0.44479505	0.79073512	0.078087582	0.1155184	10.436628	[35]
0.079	0.7136824	0.4254807	0.8964226	0.0617167	0.1270814	9.896161	[35]
0.135	0.711040	0.451885	0.704048	0.064270	0.129408	9.425478	[27]
0.193	0.7347008	0.4461191	0.8081698	0.07646793	0.1246087	9.8962033	[24]

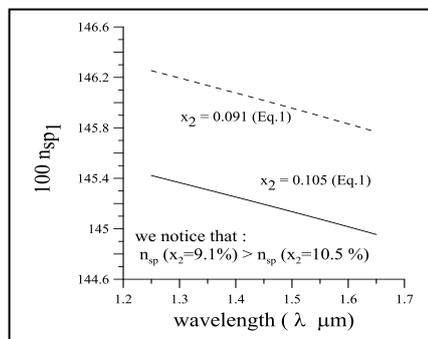
Table A.3: Difference between index of Germanosilicate by Eq.(1) and by published data Table (A.2)

$x_1$		0.030	0.031	0.035	0.041	0.058
$\lambda=1.25$ $\mu\text{m}$	$10^3 \Delta n_{\text{sg pb eq}}$	0.3699	0.0678	0.1391	0.2407	0.2830
	error %	0.0255	0.0047	0.0096	0.0165	0.0195
$\lambda=1.65$ $\mu\text{m}$	$10^3 \Delta n_{\text{sg pb eq}}$	0.2592	0.0042	0.1311	0.1492	0.2403
	error %	0.0179	0.0003	0.0090	0.0103	0.0140
$x_1$		0.063	0.070	0.079	0.135	0.193
$\lambda=1.25$ $\mu\text{m}$	$10^3 \Delta n_{\text{sg pb eq}}$	-0.5364	0.4409	1.1771	-1.2882	0.4844
	error %	-0.0368	0.0302	0.0801	-0.0874	0.0323
$\lambda=1.65$ $\mu\text{m}$	$10^3 \Delta n_{\text{sg pb eq}}$	-0.5378	1.0589	1.3999	1.2984	0.3405
	error %	-0.0370	0.0728	0.0956	-0.0883	0.0234

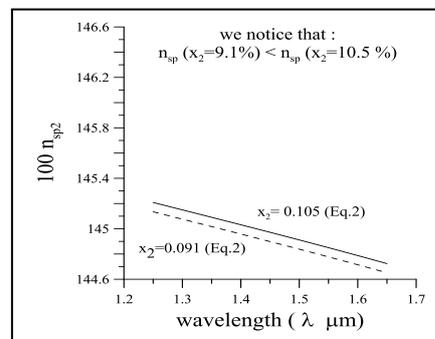
Note 1; Coefficients which calculated by Eq.(1) not satisfied with that from published data, Table (A.2)

Table A.4: Sellmeier's coefficients of Eq.(1),  $a_1 \rightarrow a_3$  and  $b_1 \rightarrow b_3$  for Phosphosilicate at special values of  $x_2$

$x_2$	$a_1$	$a_2$	$a_3$	$b_1$	$b_2$	$b_3$	
0.091	0.6957900	0.4524970	0.7125130	0.0615680	0.1199210	8.6566410	[31]
0.105	0.7058489	0.4176021	0.8952753	0.07212788	0.1134782	9.8961614	[24]



a) With Eq.(1)



b) with Eq.(2)

Fig.A.1 Check for published coefficients of Phosphosilicate with  $x_2=9.1\%$  and  $10.5\%$