



An Enhanced Real-Time Shadow Rendering Technique in Outdoor Augmented Reality

Naira Elazab

Naghm Mekky

Ahmed Atwan

Hassan Soliman

Faculty of computers and information sciences, I.T dep.
Mansoura University, Egypt

naira.elazab@gmail.com

nona762005@hotmail.com

atwan4@gmail.com

hsoliman@mans.edu.egypt

ABSTRACT

In this paper, the point is to give steady shadows amongst virtual and genuine objects for outdoor scene without requiring any earlier data. The technique gives a real-time framework for recreating reliable virtual shadows in an outdoor scene. The proposed procedure firstly handles the shadow areas because of genuine things; secondly ensures the pixels in genuine shadow are prevented from more rendering and finally rendering shadows because of virtual things. The main research contribution, in addition to shadow refinement, is handling the overlap between real and virtual shadows. Consequently those shadows for virtual things are depend on the shadows of real things. The experimental results create the impression that the recommended system has basically upgraded that authenticity about steady outside augmented reality rendering, in this manner taking care of the issue of practical augmented reality frameworks. Results show a comparison of shadow rendering between proposed technique and other techniques in different resolutions.

General Terms

Augmented Reality, Image Processing.

Keywords

Augment Reality (AR), overlapping shadow, sun position, and real-time shadow.

1. INTRODUCTION

Certainly AR will become a widely accepted technology in few years. The growth of computer-based and smart phones make it very desirable to improve AR techniques that can facilitate augmentation of images with probable renderings of virtual geometry, entertainment, education, and information purposes. To augment the real world with real-time renderings of dragons to fight in the street, to augment the real world with images of how ancient architecture seemed or to augment the real world with path searching information, etc. [1].

In AR system, the easily blend area among genuine and virtual items is definitive. Brightening consistency is an awesome piece of the easily reconciliation process. Geometric sight and light condition indoor is unsophisticated and featureless. Not at all like the light condition indoor, open air

scenes isn't just convoluted yet also versatile. Subsequently a high proficient and constant calculation for the outside scene is needed to construe the parameters of enlightenment display, with a specific end goal to perceive brightening consistency of open air scene [2].

AR enables the people to keep interfacing with each unreal and actual things round them. A real-time combination with these unreal and actual things helps a person to evaluate numerous variables concurrently and interpret he situation with efficiency. An entire AR process ought to involve three major aspects, i.e. tracking, registration and rendering [3].

The seamless combination of the unreal world and this present reality that we stay in is a requesting point in present AR research. There would a considerable measure of primary issues that expand the immersive perception of the user. This paper concentrate on the issue for shadows associated to an AR universe. Unnecessary to state that in an AR framework a number of issues require to be solved. Among the main tasks is, obviously, that construct objects need to be positioned on the accurate location because they indeed would exist in the actual world. As stated by Naemura et. al. [4], that consistency about geometry, time also brightening is a significant issue for AR implementations. This paper concentrates on that consistency of brightening and suggests a method for shadows in a composed AR application. Shading and shadows in two worlds ought to correspond to accomplish a natural integrate [5].

A large portion of real-time shadows have been restricted to hard shadow. In hard shadow, a place is either lit or in shadow. It isn't an imperfection, yet an impediment of this sort of method. In the wake of creating hard shadows in PC diversions, realistic specialists started to concentrate on soft shadows. These days, soft shadows have turned out to be a standout amongst the most imperative impacts the present AR systems to make the situations maximally reasonable [6].

The technique introduced in this paper provides for an ongoing strategy both for taking care of those first shadow locales due to certified things, second rendering new semi-soft shadows as a result of the expansion of unreal things. Consequently overlaps among authentic and unreal shadows are managed and the shadows of unreal things are enduring with the shadows of certified items. Practical virtual objects in

open air rendering AR frameworks require complex impacts, for example, shadows, and sunlight. Realistic rendering methods have been intended to defeat this hindrance, the majority of which are identified with non-real-time rendering. This paper proposed a much more up to date, method to accomplish practical constant open air rendering, while at the same time considering the overlap between real and virtual shadow in AR frameworks as for shadows in a particular area, date and time.

This paper is organized as follows. In Section 2, a short outline of the related work is given. Section 3, depicts the strategy producing shadow models. In Section 4, exploratory outcomes are introduced. At last, the conclusion and future work is displayed in Section 5.

2. RELATED WORK

In this section, a brief overview of techniques that are most pertinent to proposed work enclosing illumination estimation and shadow generation is given, so this section is divided to two parts as follows:

2.1 Illumination estimation

The Sunlight is the key resource of normal lighting. The sunlight is an illuminating presence that emulates the impact for daylight. It might be utilized to exhibit how those shadows throw by an entity influence the around area. The direction of light from sunlight is managed by position, day and time.

Retrieving view brightening from pictures has been presented for quite a while in reverse rendering and relighting. But these types of techniques generally expect that both a geometric design [7 and surroundings map predicated on high dynamic range (HDR) pictures of the view [8] is accessible.

While efficient for interior views, they could barely be executed to the real-time illumination source estimation of outside views. There are two motivations. Firstly, the wide range conditions and complicated things in outside views are hard to reconstruct. Next, the source of light in outdoor view is hard to manage in the manner like in a research environment [9].

Next to no meets expectations once inferring those brightening of open air scenes bring at any point been recommended. Zhou Ya et al. [10] recommended an approach to calculate sunlight place from an individual picture but didn't consider its intensity. Later, they expanded the method to clearly calculate the intensities of light from the sun [11]. However, because those two methods get temporal movie dice as input, they didn't support real-time applications, like, AR.

Sunkavalli et al. [12] built method to calculate sunlight path and view geometry by adapting a photometric style of view reflection to a time-lapse collection of an outside view. Lalonde et al. [13] utilized cues, for example, varied histograms of shading and consistency as well as a difficult classification of view geometry [14] to fit brightening of various views. But, the cues are worldwide in character and can't be applied to fit sunlight directions. That makes the method not suitable to 3-D item inclusion.

2.2 Shadow generation

Yang Liu et al. [15] created shadow models and compared them with actual shadows utilizing a higher-order graphical model. This system requires human interference to calibrate

the camera parameters and to decide the viewpoint of the objects.

Lalonde et al. [16] proposed an approach for estimating the conceivable light states the scene using a single outdoor image. Specifically, they calculated the probability distribution through the sun position and vision. Those techniques based on a set of weak cues that can be evolve from various parts of the image: the sky, the vertical surfaces, and the ground. While no single cue can dependably infer illumination by itself, each one can enhance the others to yield a more robust estimate. This is gathered with a data-driven previous computed over a dataset of 6 million Internet photos. They presented quantitative results on a webcam dataset with annotated sun positions, as well as qualitative results on consumer-grade photographs downloaded from Internet.

Numerous researchers have considered how the shadows in AR conditions can be applied and enhanced [17, 18]. Other research has concentrated on upgrade of virtual shadows, making objects more reasonable in open air AR rendering separated from any connection amongst genuine and virtual objects [19]. Collaboration between sky shading and virtual objects amid daytime is one of the most recent works that makes the AR framework more sensible, however experiences throwing shadows on genuine conditions.

Aittala [20] connected Convolution Shadow Maps (CoSMs) [21] to create delicate shadow in mixed reality (MR) utilizing both mip-map filtering and quick summed area tables [22] to upgrade obscuring with variable sweep. Castro et al. [23] proposed a technique to create delicate shadows with less associating utilizing a settled separation in respect to the marker, yet with just a single camera. The strategy additionally performed one sphere mapping; for example, [24], however chosen a source or wellsprings of light most illustrative of the scene. This is vital on account of equipment impediments of cell phones. The strategy underpinned self-shadowing and in addition delicate shadowing. They utilized separating techniques, for example, percentage closer filtering (PCF) [25] and variance shadow maps (VSM) [26] to produce delicate shadow.

VSM is extremely invaluable contrasted with its forerunners shadow mapping and PCF. The fundamental issues of this technique are identified with testing and associating depths. These issues are firmly associated and relied upon the determination for computing visibility. Kolivand et al. [27] utilized hybrid shadow maps (HSMs) to position delicate shadows on other virtual and genuine items.

Kolivand et al. [28] gave a review of the issues and procedures associated with shadow age in mixed reality situations. Shadow age procedures in virtual situations are clarified quickly. The key variables portraying the outstanding procedures are depicted in detail and the upsides and downsides of every system are examined.

3. METHODOLOGY

This paper introduces a shadow generation technique in AR in which the overlap between genuine and unreal shadows is solved. Some techniques to render the virtual shadows of unreal objects present a solution like the one shown in fig 1(a), where the shadows of the unreal items placed perfectly on the ground as expected, however overlap wrongly with the shadow of the authentic object. The accurate outcome ought

to be likewise in fig 1(b) which is estimated using the method shown in this paper. At the point, when those unreal shadows will be added using shadow maps the individual's pixels that locate in the unreal shadow get the intensity scaled using a suitable rate variable.



Fig 1: (a) Formation of the unreal shadows using particular case rate variable. (b) At using a suitable rate variable and guaranteeing the shadow pixels recognized toward those shadow location step, those unreal shadows are compatible with the actual shadow.

Whenever unreal and genuine shadows incompletely cover one have to choose the suitable rate variable. If the rate variable is 1 (no rating), the individuals pixels in the covering area have a shading predictable for the genuine shadow pixels, the non-covering pixel, in any case, will be shining than needed for a dependable shadow.

If the rate variable is less than 1, the pixels in the non-covering zones will have shading like that of the authenticate shadow pixels, however the pixels in the covering zone will be too much diminish, making the shadow once more, conflicting. So the proposed way is producing a practical constant outdoor environment is planned. The proposed approach is illustrated in Fig 2. It comprises of three major segments: (1) shadow location (2) shadow insurance, and (3) shadow rendering.

3.1 Detection of Genuine Shadow Location

The shadow location step manages the location and contours of the genuine shadows of the genuine items in the sight. In proposed calculation, for the shadow location part, the approach of [29] is took after .The distinction is that, rather than joining the scene design to evacuate false positives, false positives is disposed of utilizing object areas. Along these lines, the proposed approach decreases the inquiry space in the shadow induction step.

Once the genuine shadow form is obvious, it will be possible to compute a rating variable for each item on shadow that mirrors the power in the shadow area. . This variable refers the shade of the items in shadow with this not in shadow. An extra itemized clarification of the shadow discovery step will be introduced in the following.

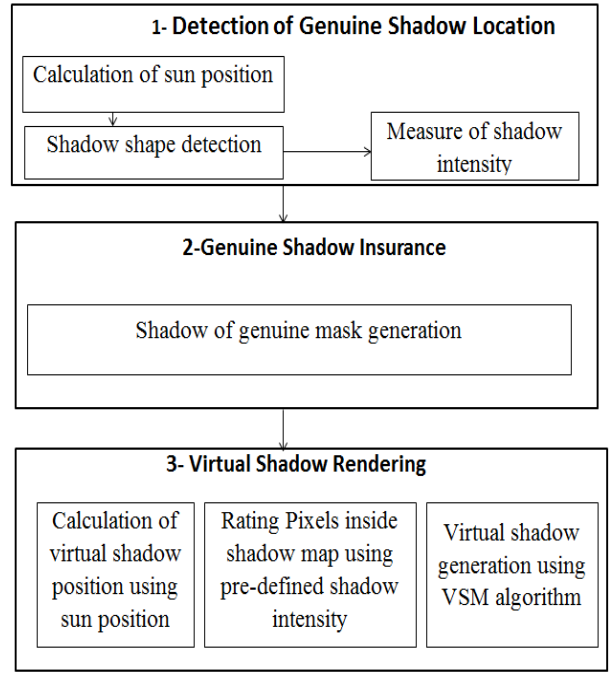


Fig 2: A proposed framework for outdoor overlapping shadow.

3.1.1 Calculation of sun position

To ascertain position of the sun, zenith and azimuth are sufficient. To have zenith and azimuth, area, longitude, latitude, date and time are required. Zenith is the edge that demonstrates the measure of dawn while the azimuth is the edge that shows the sun point that sun pivots the earth.

Iqbal [30] proposed an equation to ascertain the sun's position and Preetham et al. [31] enhanced it. It is a typical equation to ascertain the position of the sun in material science. The time of day is computed using the following Equation 1.

$$t = t_s + 0.17 \sin\left(\frac{4\pi(J-180)}{373}\right) - 0.129 \sin\left(\frac{2\pi(J-8)}{355}\right) + 12 \frac{SM-L}{\pi} \quad (1)$$

where: t is solar time; t_s is Standard time; J is Julian date; SM is Standard meridian; and L is Longitude.

The sun oriented declination is ascertained using Equation 2. The time is computed in decimal hours and degrees in radians. Finally, zenith and azimuth can be ascertained (Equation 3 and 4):

$$\delta = 0.4093 \sin \frac{2\pi(J-8)}{368} \quad (2)$$

$$\theta_s = \frac{\pi}{2} - \sin^{-1}(\sin l \sin \delta - \cos l \cos \delta \cos \frac{\pi t}{12}) \quad (3)$$

$$\phi_s = \tan^{-1}\left(\frac{-\cos \delta \sin \frac{\pi t}{12}}{\cos l \sin \delta - \sin l \cos \delta \cos \frac{\pi t}{12}}\right) \quad (4)$$

Where θ_s is solar zenith, ϕ_s is solar azimuth, and l is latitude. With count of zenith and azimuth suns position will end up plainly self-evident.

3.1.2 Shadow shape detection

Should secure the present shadows in the sight starting with any post-handling, those shadow pixels in the outside should be recognized. Two kinds of shadows exist: delicate shadows

and hard shadows. In a perfect world the two kinds of shadows are distinguished, however it is significantly less demanding to recognize hard shadows. This paper does not go for building up another best in class shadow detection strategy yet rather asserts that the three-advance system is free of the decision of shadow location in this initial step.

The point of the shadow identification process is to recognize thrown shadow areas. Late methodologies have chiefly utilized light invariants which can come up short when the nature of pictures is poor. Lalonde et al. [29] presented a calculation to naturally identify shadows threw by objects on the ground. The strategy depends on the perception that the sort of materials constituting the ground in run of the mill open air scenes are constrained, most generally including solid, black-top, grass, mud, stone, and block. They expected that these shadows can be gained from an arrangement of marked pictures of genuine scenes. Truth be told, they exchanged the location issue as an arrangement amongst shadow and non-shadow limits. As appeared in [29], reflections, self-shadowing, and complex geometry are normal wonders that may befuddle the classifier. In their usage, they join scene formats to expel false positives. Rather than fusing the scene design to evacuate the false outcomes, proposed approach utilizes areas that are as of now decided for rendering virtual question.

3.1.3 Measure of shadow intensity

When the shadow part is described, such is viable after determine a rating variable for each item in shadow. Those rating variable is in actuality a triplet $[\rho_R; \rho_G; \rho_B]$, characterized by separating the three color values of pixels over the pixels inward those shadow for the individuals out the shadow. In present execution, a little area of pixels in what's more a little area about pixels out those shadow were chosen then utilized to infer a mean rating variable. The following mathematical statement clarifies how that triplet is ascertained. $C = \{R; G; B\}$ speaks to those color value: red, green or blue; SA remains for shadow area, while NSA stands for non -shadow area; PSA furthermore PNSA are those number about pixels on separately those shadow and non-shadow area:

$$\rho_c = \frac{\sum_{p \in SA} C_p}{P_{SA}} \quad (5)$$

$$\frac{\sum_{p \in NSA} C_p}{P_{NSA}}$$

As a rule this rating variable changes over the focuses on a surface, and depends upon the acquaintance of that surface with the sun.

3.2 Genuine shadow insurance

In the shadow insurance step, a binary shadow cover is generated to ensure the individuals pixels in a genuine shadow from any rating. Those rate variable is facilitated those shade of the non-covering zones for pixels in those genuine shadow. In that purpose when those yield of the shadow recognition step is utilized with complete those shadow cover; every point in those genuine shadow is successfully hindered from moreover rendering: those subsequent unreal shadow will be predictable, similarly as indicated for Fig 1(b).

In view of the shadow form, binary mask is developed. This mask will be used to indicate which concentrates in the genuine show are in shadow alternately not. In a manner of speaking, it could a chance to be viewed as Likewise as a surface maps in order that overlay the surfaces of the sight. That yield of the shadow identifier will be an edge picture, holding data for this shadow shape, at some stage in pixel level. Since the detector recognizes edges concerning one pixel thickness then expels an enormous share disaster inward these picture, the shadow location can be resolved for the most part straightforward: the shadow cover structure takes the edge outline data and utilizes a region growing algorithm to become full the shadow zone in the shadow shape.

Those beginning stage over the area Creating might a chance to be at whatever purpose in those shadow district, which might be gotten from the shadow evaluate. Gray-level mask will be shaped with values setting off from 0 on 1 rather than a binary one. The individual's pixels inner those shadow are totally secured (light), the pixels out the shadow are no longer ensured (lightless), then the pixels during those shadow edge would incompletely secured (grade gray level). The grade between the refined districts will be quadratic to mirror those visionless deviations take into consideration according to a place sun. The aids of the quadratic gradient increment the amount of delicate quality. This does stand evaluated if the separation on the light source then its locality is round known.

For an outside scene, of a shining day it is acknowledged so the sun consolidated perspective concerning 0.5 degrees. The direction about the daytime an approximation on the amount of delicate can be computed. In alter cases, certain be able utilizes the performance over the pixel intensities round those perceived shadow edge. AT every pixel a grey degree could a chance to be created in shadow masks so demonstrates what amount of light it gets, without reorganize the shadow rendering step.

3.3 Virtual shadow rendering

In the shadow rendering step, a steady shadow procedure VSM is utilized to create the unreal shadows. The power of the shadow identifies with the best possible rate variable handled in advance; cover among genuine and unreal shadows is avoided by utilizing mask created in past stage. The individuals' bits of the unreal shadow that allocate in genuine shadow would neglect. Those drives of the pixels in the virtual shadow in the non-covering areas would determine by rating those surface shading with the variable rate. The effect of the decision of the rating variable may be demonstrated in Fig 1(b). Amid those rendering, an alternate rating variable should be utilized for various items.

When the genuine shadow areas would distinguish, such is conceivable to mimic those shadows as a result of displaying the unreal items. These shadows might make handled for various calculations.

In the present utilization, shadow maps What's more shadow volumes are utilized, be that whatever available ongoing shadow rendering procedure, which include softness shadows, is suitability. Those shadows are figured utilizing those

estimated position of the sun and think as of the participation amongst unreal also real items.

Shadows from digital items are thrown on authentic what's more digital items; also real items could throw shadows on unreal items. Shadows as a result of authentic items onto other authentic items are by now incorporated. The power of the shadows would be assessed utilizing those rating variable likewise registered in area B. This rating variable varies for every item looking into which those shadow may be thrown. It ought to reflect both those item properties and the light obtained within each and every area.

Shadow maps are regularly utilized as a part of real-time rendering, yet they can't be separated directly like standard color, bringing about extreme aliasing. VSMs settle this issue by representing the depth dissemination utilizing moments, which can be straightly separated. VSMs offered a respond in due order regarding this issue by speaking to a probability distribution about depths at every shadow map. For attain consistent space usage, the distributions need aid approximated utilizing their first couple moments. Those visibility function over a free filter area might be evaluated utilizing chebyshev's Inequality, that produces a top bound concerning the quantity of light arriving at the part continuously shaded. On account of an absolute planar occluder furthermore a solitary planar recipient those remaking will be accurate, inspiring its immediate requisition to shading.

In light of the fact that just two moments are stored, complex visibility functions can't be remade superbly. This prompt areas that ought to stay on shadow existence lit, a relic acknowledged as "light bleeding". Storing extra moments may want to do away with the problem; however computing visibility feature becomes entirely computationally hard any more moments are utilized. Besides higher request moments are numerically unsteady, make to them hard in imitation of utilizes within practice, Fig 3 demonstrates a case of light bleeding practically speaking.

An easy scenario which bleeding happens, the tree casts an appropriate shadow onto seat. The ground have to be totally occluded through seat, however a percentage of the penumbra from tree's shadow "bleeds" through wrongly. Note up to expectation the ratio on Δx (tree to seat) in accordance with Δy (seat to ground) may be high, prompting knowing artifacts. With a specific end goal to keep whatever overlap between those produced shadows and the genuine shadows those shadow mask registered Previously, segment 3 is utilized to show the locales that could make drawn in the color buffer. Districts with zero qualities (lightless) may lie overdraw also areas with one quality (light) are completely secured. Areas with gray level qualities are incompletely secured.



Fig 3: Light bleeding: That penumbra from the tree shadow will be inappropriately bleeding via the seat.

In summary, the proposed strategy sums up VSM that gives a versatile best approach to decrease alternately remove the light bleeding. Another competency is to that the proposed technique wills a wider range of graphics fittings over standard VSMs. It is indicated that the proposed technique prepare great nature shadows same time looking after secondary execution. They would truly suitableness for utilize in games also different ongoing graphics requisitions that require prominent shadow.

4. RESULTS

From the view of constant rendering, the proposed strategy is sufficiently precise. The effects presented in this area view those techniques through which those targets and therefore the point of the research are attained. Those shadows and the impacts about overlap with respect to unreal items in the AR framework are handled gradually.

Since it is primarily in view of shadow maps, throwing the unreal shadows into other items may be the principle capability from this class of shadow generating systems. Table1 shows a performance comparison of proposed algorithm and several methods in different resolution. The computation time between the proposed system and some very much revealed techniques in the literature is given in Table2. The proposed method is performed on LabelMeFacade image dataset, in addition to consumer-grade images which randomly selected from flicker [33].

Table1. Speed of Rendering measured by FPS in different resolutions.

Rendering Technique	512 * 512	1024 * 1024	2048 * 2048
VSM [26]	109	75	63
LVSM [32]	112	82	76
HSM [27]	123	89	82
The proposed method	132	98	91

From Table1, the proposed framework outperforms the methods of VSM, layered variance shadow map (LVSM) and HSM in both low and high resolution. Results of assigning different resolution achieve amazing results, which gets the highest shadow rendering rate for all resolution. The proposed framework outperforms VSM, LVSM and HSM because of faster computation time, and is more precise and easily implemented.

Table2. Time computation (milliseconds) of shadow rendering methods.

Rendering Technique	512 * 512	1024 * 1024	2048 * 2048
VSM [26]	0.0091	0.0133	0.0158
LVSM [32]	0.0089	0.0121	0.0131
HSM [27]	0.0081	0.0112	0.0121
The proposed method	0.0075	0.0102	0.0109

Vertical shadow angle (VSA) and horizontal shadow angle (HSA) in a similar place been measured and the outcome is as per the following. Fig 4 reveals that proposed calculation (HSA) changes easily like separated of normal distribution. Fig 5 uncovers that VSA diminishes in the vicinity at time 6 and 11 forcefully and around 11 increments pointedly and again declines to -0.5 at 18. It implies that to concentrate on measure of shadow in rearrangement, the time in the vicinity of 11 and 16 is generally imperative. This implies in spite of the fact that measure of shadow ought not to be stressed over, it is vital to have less daylight in warm places and more daylight in icy spots.

The proposed solution is ensured to have lower aliasing and more soft edges. The improvements of shadow quality by the proposed method can see in fig 6 that show close-up of object shadow rendered using proposed method (right) and VSM (left). A close-up appears some artifacts and aliasing for the left image.



Fig 6: close-up of shadow using VSM (left) and the proposed method (right).

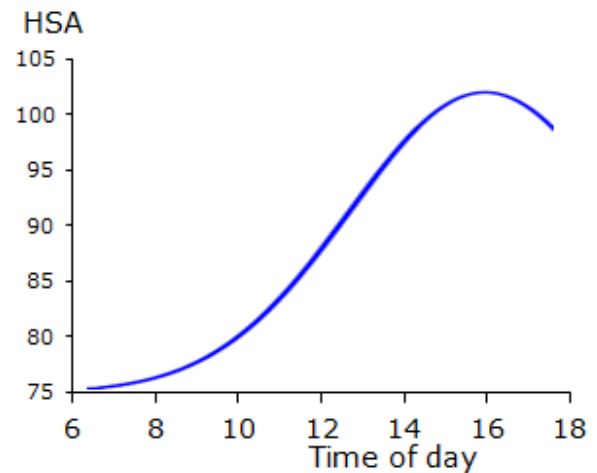


Fig 4: HSA in various time of day.

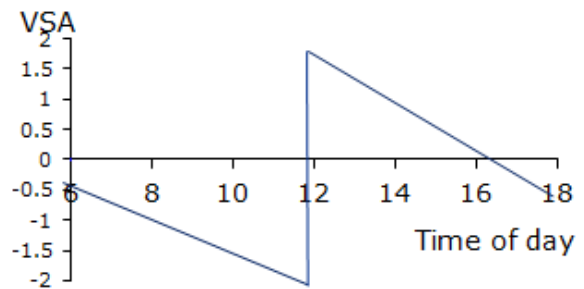


Fig 5: VSA in various time of day.

The cooperation of the virtual items is registered continuously. Fig 1 (b) as of now demonstrated the aftereffect of the exhibited strategy on an outside scene. An alternate illustration on a greater complicated view is provided here.

Fig 7 demonstrates an indistinguishable scene from in Fig3, aside from now rendered with proposed technique. Note that the light draining has been totally disposed.



Fig 7: Light bleeding doesn't exist into a picture render with the proposed algorithm.

The software utilizes " AR Toolkit" in conformity with perform real-time monitoring about the camera.

Same time the digicam captures that scene, a digital avatar strolls crosswise over those genuine shadow outskirts. Those digital shadows of the avatar are added reliably inside the actual scene, utilizing those rating variable and the shadow mask computed after those ongoing shadow recognition. In a similar way, the symbol gets shadows from the genuine object. The camera alignment is refreshed each frame and accordingly the shadow mask additionally should be refreshed each frame, as opposed to ascertaining it once and fusing it into the scene. No further activity has been embraced to make more valuable condition impacts and subsequently the shadows are not hard shadows. Fig8 show Consequences of the calculation for an energized virtual symbol strolling around real tree in street. Shadows are consequently identified and created utilizing suggested real-time calculation. Execution information truly exhibit that recommended strategy will be great suiting to utilization into real-time application.

5. CONCLUSION

This paper introduced a steady shadow reproduction for AR applications without requiring any earlier data and semi-soft shadows are applied. The proposed technique is comprised of a three-stage structure: shadow location, shadow insurance, and shadow rendering. This three-stage calculation created reliable shadows amongst actual and unreal objects continuously. This permits the utilization of the displayed technique in expanded reality applications. Approaches will be scanned for making this calculation more strong for all kinds of delicate shadows. This study have considered just outdoor environment in daylight and the general lighting conditions are overlooked. More work must be performed to simulate the impacts of actual items on unreal ones and vice versa. In the future work would present an algorithm which will match overall lighting effects.



(a)

(b)

(c)

Fig 8: An example of a large scene with overlapping shadows rendering virtual object using proposed method. (a) The case of non-overlapping so rendering the complete shadow of object. (b) The partial overlapping then rendering shadow of the only shining part. (c) The completely overlapping so no rendering shadow.

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