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## A Simplified Approach for Water Hammer Analysis

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### Abstract

The objective of this paper is to provide a practical and simplified approach for the analysis of water hammer phenomenon, develop the pressure transient envelopes produced due to water hammer, assess the need for protection, and determine the size of protection device. A typical water supply system consisting of a pump and long transmission pipeline delivering to a terminal reservoir is proposed. About 500 runs are simulated on Bentley Hammer software to cover wide variation of physical and hydraulic parameters. The results of simulation are used to develop a model for the pressure envelopes along the pipeline profile and another model for sizing of the protection device needed to reduce the impact of water hammer.

**Keywords:** Transient Pressures, Water Hammer, Surge Protection Devices, Simplified Approach.

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### Introduction

Water hammer prediction used to carry out graphically (Allievi, 1925) (1). The graphical method is very complex and not accurate. Angus and Parmakian, (1963) (2) and Wood & Jones, (1973) (3), refined the graphical calculation method. Numerical methods implemented in computer codes addressed this problem. The development of computer technologies made the numerical method of water hammer simulation in complex pipe networks become easier. In recent years, numerical methods are widely used in water hammer phenomenon study and almost replaced the graphical method. The main numerical methods to Joukowsky developed an equation in 1898 to calculate pressure drop or rise due to sudden pump

simulate water hammer events include method of characteristic (Wylie and Streeter, 1993) (4), the finite volume Method (Zhao and Ghidaoui, 2004) (5), the finite element method (Kochupillail et al., 2005) (6), Wavelet-Galerkin (Sattar et al., 2009) (7), the fluid structure interaction, and so on. Among those methods, the method of characteristic (MOC) is the most popular one. Afshar and Rohani, (2008) (8), developed a different MOC procedure. Some research indicates that MOC fits experimental data well. Ghidaoui et al., (2005) (9) investigated eleven available water hammer commercial software packages, and found that in eight of them MOC was applied.

power failure. Joukowsky's Equation is shown in equation (1):

$$\Delta H_1 = \pm \frac{a}{g} \Delta V \tag{1}$$

Where,  $\Delta H_1$ ; is the change of surge pressure,  $\Delta V$ ; is the change of water velocity in the pipeline,  $a$ ; is the wave speed, and  $g$ ; is the gravitational acceleration line with instantaneous failure. Joukowski's equation is based on some assumptions such as the occurrence of hammering is instantaneous, the pipeline properties are uniform, and the pipe is rigid. During transient, pressure and velocity in pipes change with distance and time where they follow the laws for conservation of mass and conservation of momentum given in Equation (2, 3) respectively. (10)

$$\frac{\partial P}{\partial t} + v \left( \frac{\partial P}{\partial x} \right) + \rho a^2 \left( \frac{\partial v}{\partial x} \right) = 0 \tag{2}$$

$$\frac{\partial v}{\partial t} + v \left( \frac{\partial v}{\partial x} \right) + \frac{1}{\rho} \left( \frac{\partial P}{\partial x} \right) + g \sin \theta + \frac{fv|v|}{2D} = 0 \tag{3}$$

Where  $\frac{\partial P}{\partial t}$ ; is the change of surge pressure with time during transient,  $\frac{\partial v}{\partial t}$ ; is the change of flow velocity with time during transient,  $\frac{\partial P}{\partial x}$ ; is the change of surge pressure with the distance in the pipeline,  $\frac{\partial v}{\partial x}$ ; is the change of flow velocity with the distance in the pipeline,  $v$ ; is the fluid flow velocity,  $\rho$ ; is the mass density of the fluid,  $a$ ; is the wave speed,  $g$ ; is the gravitational acceleration line,  $D$ ; is the conduit diameter of pipeline,  $\theta$ ; angle the conduit makes with the horizontal, and  $f$ ; is the friction factor. The main concept behind of MOC is the transformation of partial differential equations (2, 3) into ordinary differential equations and these equations are shown concisely in equation (4,5). (10)

$$Q_p = C_p - C_a H_p \tag{4}$$

$$Q_p = C_n - C_a H_p C^+ \tag{5}$$

Where,  $Q_p$ ; and  $H_p$ ; are the discharge and head at point P respectively, ( $C_p$ ,  $C_n$ ,  $C_a$ ) are constants dependent upon pipe properties, initial condition and time interval. Thorley and Lastowiecki, (1985) (11) presented the first computer based iterative procedure for sizing air vessels for pipeline systems. Stephenson, (2002) (12) showed the effect of using air vessels in protecting the distribution system against negative pressures during water hammer, and reported that air vessels can maintain a positive pressure in the line at all stages following pump trip. Di Santo et al., (2002) (13) developed design charts for air vessel sizing for pump trip scenario

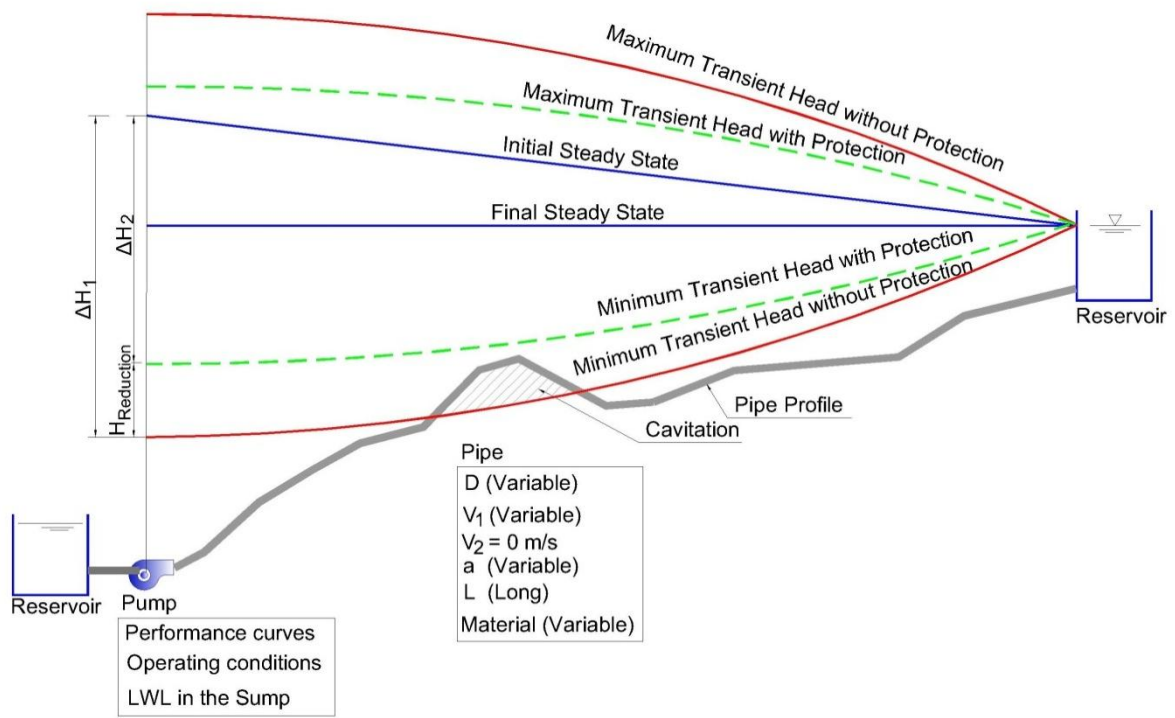
that can be applied only at preliminary design stage due to their simplifying assumptions (e.g. neglecting frictional losses), selection and range of parameters, limited accuracy of solutions and lack of completeness. Martino et al., (2004) (14) reported that Evangelisti in 1938 developed graphs that aid in the sizing of air vessels, using incompressible flow theory neglecting pipe friction and assuming adiabatic expansion of air ( $n=1.41$ ).

Evangelisti's Equations allow for analytical solution if pipe friction is neglected and introduced a dimensionless constant (ratio of steady state head loss to absolute steady state pressure) for use in numerical integration procedures for solution when pipe friction was considered. These graphs demonstrated the favorable role of pipe friction loss in attenuating over pressure oscillations El-Bahrawy, (2004) (15) presented a simplified description of water hammer, its effects, control devices and equations. He also presented a spread sheet for teaching transient flow in pipes. Fleming and Gullick, (2005) (16) developed surge models for five distribution networks and used it to identify the locations within the distribution systems where low or negative pressures were most likely to occur. Durand et al., (2006) (17) developed a simplified analysis of water hammer. The analysis calculates four main parameters of water hammer; velocity of the pressure wave celerity, critical time, maximum head developed in the maximum pressure time and minimum head developed in the critical time. Gao et al., (2012) (18) investigated cases studies of three kinds of hammer protecting devices which are two-phase control valve, one-way surge tank and hydropneumatic tank. According to the simulation results, the effective protecting scheme of water hammer is through hydropneumatic tank to reduce the surge damage combined with the application of the air valve. Himr, (2013) (19) simulated unsteady flow during water hammer using Matlab-Simulink-SimHydraulics and HYDRA. Simulation results proved in very good agreement with experimental measurements. Oulhaj et al., (2013) (20) presented the influence of using the protection devices to control the adverse effects due to excessive and low pressure occurs in the transient. Pato and Navarro, (2014) (21) presented a reformulation of the mathematical model developed by Preissmann, 1964 for the estimation of pressure values in

transitory situations between both shallow and pressurized flows by adapting it to abrupt transient situations. The objective of this paper is to provide a practical and simplified approach for the analysis of water hammer phenomenon, develop the pressure transient envelopes produced due to water hammer, assess the need for protection and determine the size of the gas volume in the air vessel. Bentley Hammer V8I software, which adapts the MOC is used for transient analysis.

**Materials and Methods**

Atypical water supply system consisting of a pump and long transmission pipeline delivering to terminal reservoir is used for the analysis. Figure (1) shows the water supply system, pipe profile, initial and final steady state hydraulic grade, maximum and minimum transient head with and without protection.



**Figure (1): Typical Pressure Envelops With and Without Protection**

To conduct the aforementioned objectives of research, about 500 simulation runs are applied on Bentley Hammer to the water supply system covering a wide range of physical and hydraulic parameters as presented in Table (1).

**Table (1): Variation of the Physical and Hydraulic Parameters**

Parameters	Range
Diameter (D) (mm)	300 to 1200
Velocity (V) (m/s)	0.5 to 2.5
Wave Speed(a) (m/s)	300 to 1500
Demand and Pump Head (H)	Depend on the velocity and diameter
Pipe length (L) (m)	Long pipeline (30 km)

The analysis is undertaken in three steps:

**Step 1** - Evaluate the impact of water hammer pressure, presented by calculating the pressure drop ( $\Delta H_1$ ) as a result of water hammer.

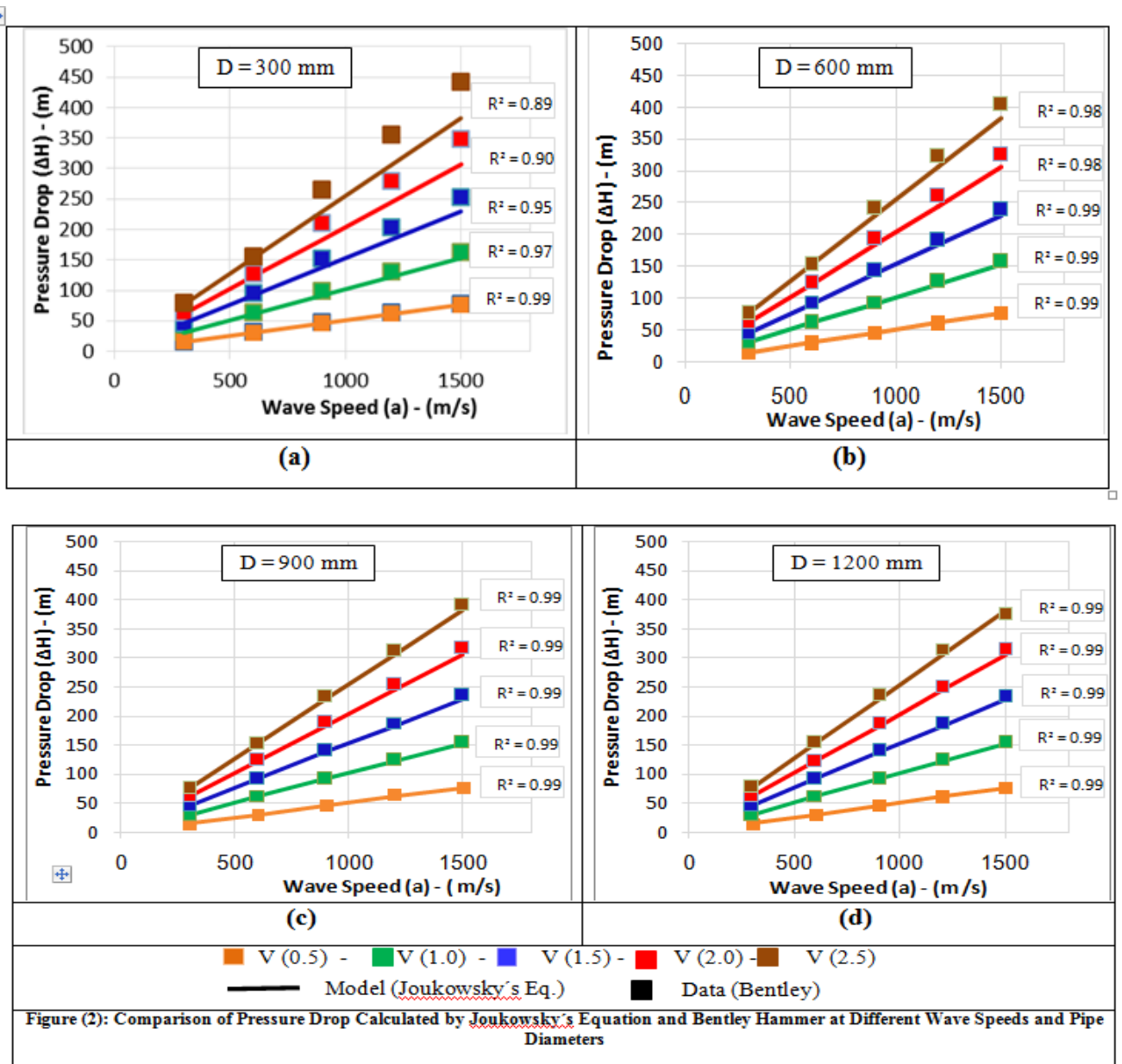
**Step 2** - Develop a relation for the pressure envelops which upon plotting against pipe profile, the need for water hammer protection can be assessment.

**Step 3** - Develop a relation for the size of water hammer protection device.

**Results and Discussion**

*Step 1- Pressure Drop at the pump station*

Comparison between the calculated pressure drop ( $\Delta H_1$ ) due to pump power failure by Joukowsky’s Equation and the resulting pressure drop by Bentley HAMMER software is presented in Figures 2 (a to d) for diameters 300, 600, 900 and 1200 mm respectively. The velocity ranged from 0.5 to 2.5 m/s and wave speed from 300 to 1500 m/s. The values of wave speed were used to represent a rigid pipe and an elastic pipe. The coefficient of determination ( $R^2$ ) is used for model assessment.



Joukowsky's Equation is validated by comparing the results of calculated pressure drop ( $\Delta H_1$ ) and those resulting from Bentley Hammer software, it is noted that Joukowsky's Equation can be expressed the pressure drop with high agreement. the pressure drop values are in close proximity with ( $R^2 > 0.95$ ) at flow velocity of less than 2.0 m/s, while the results for the velocity higher than 2 m/s is slightly close with ( $R^2 > 0.89$ ).

Where,  $\Delta H$ ; Pressure drop along the pipe line (m),  $\Delta H_1$ ; Pressure drop at the pump (m) (calculated by Joukowsky's Equation),  $X$ ; Distance interval (m), and  $L$ ; Length of the

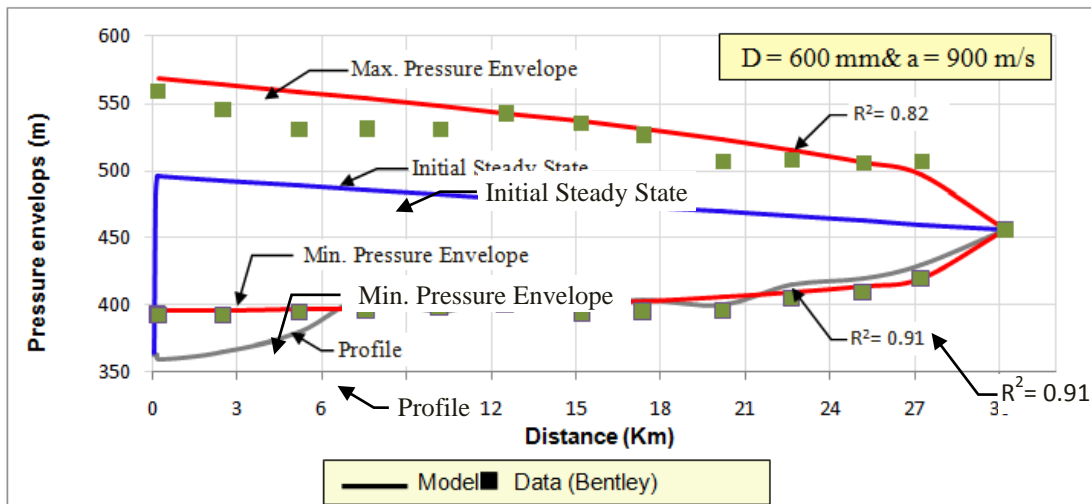
Finally Joukowsky's Equation can be expressed the transient behavior for simple system.

Step 2 - Pressure envelopes

To assess the need for a protection strategy, it is important to calculate the pressure envelopes and plot it over the pipe profile. A new empirical formula is developed for determining the pressure envelopes along the pipeline as shown in Equation (6).

$$\Delta H = \Delta H_1 \left[ 1 + \left( \frac{X}{L} \right)^{0.35} \right] \quad (6)$$

pipe (m). Figure (3) shows pressure envelopes without protection for diameter of 600 mm and wave speed (a) of 900 m/s.



**Figure 3: Pressure Envelopes without Protection**

The developed formula in Equation (6) is validated by comparing the results of the pressure with those calculated by Bentley Hammer, it is noted that the developed Equation can be expressed the pressure envelopes with high agreement. The maximum and minimum pressure values are in close proximity with  $R^2$  (0.82 and 0.91) respectively. Therefore, the developed empirical formula Equation (6) proved to be a good approximation for calculating the maximum and minimum pressure envelopes and

$$V = 0.4D^5 H^{1.75} \quad (7)$$

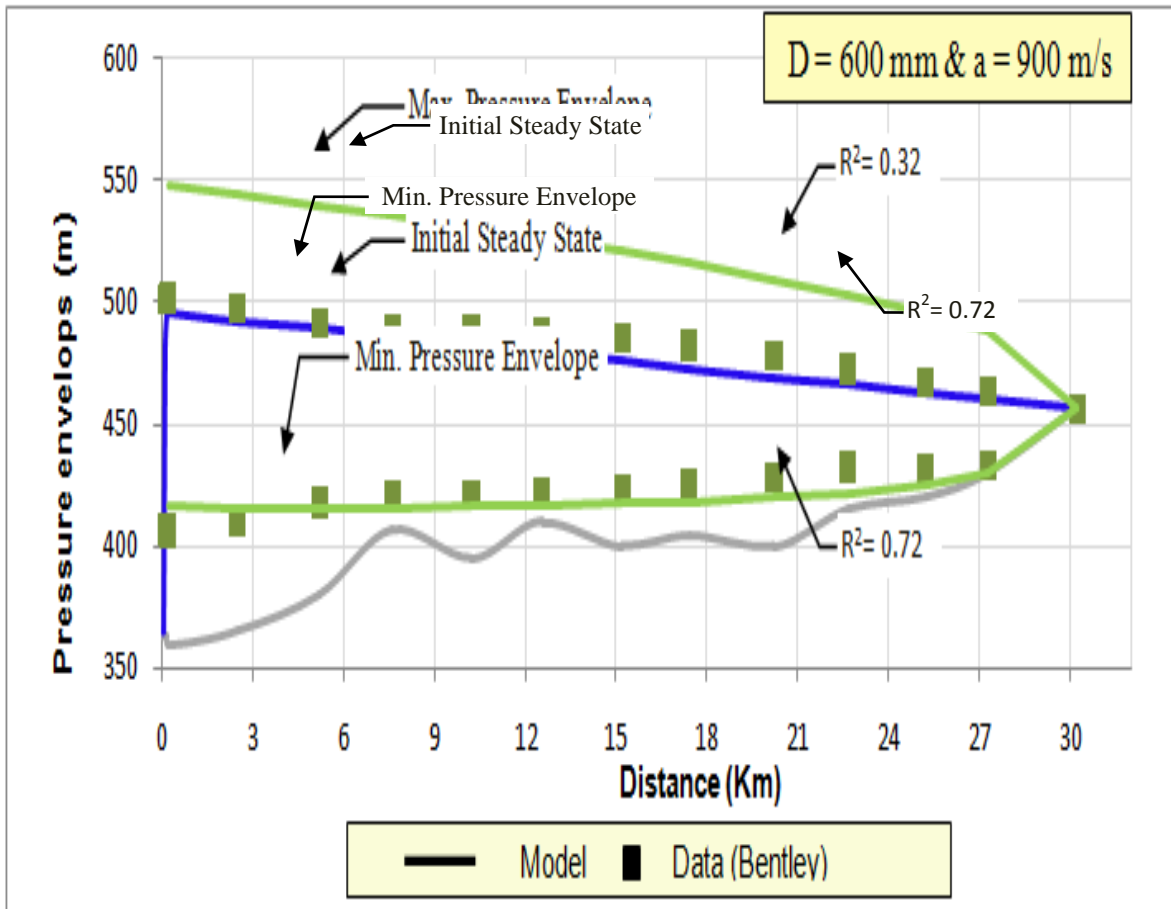
Where,  $V$ ; Gas volume in the hydropneumatic tank ( $m^3$ ),  $D$ ; Pipe diameter (m),  $H$ ; Required reduction of the pressure drop to eliminate water hammer effect (m).

assessment of the need for a protection device by plotting the pipe profile against the pressure envelopes.

Step 3 - Sizing the Protection Device

In piping system, various control procedures are used to reduce or eliminate undesirable transients, such as excessive pressure rise or drop. In this study, the air vessel is suitable for controlling transients generated by power failure of the pumps. A new formula is developed for determining the size of gas volume as presented in Equation (7).

Applying Equation (7) on the proposed water system, the gas volume in the air vessel for the system is  $7 m^3$  approximately to reduce the pressure drop 21 m approximately.



**Figure (4): Pressure Envelopes with Protection**

As shown in figure 4, it is noted that the calculated gas volume calculated by Equation (7) eliminates the pressure transient impact. The developed formula in Equation (7) is validated by comparing the results of the pressure with those calculated by Bentley Hammer, it is noted that the developed Equation can be expressed the pressure envelopes with protection with high agreement in calculating the downsurge pressure while upsurge pressure is underestimation. The maximum and minimum pressure values are in close proximity with  $R^2$  (0.72 and 0.32) respectively. Therefore, the developed empirical formula Equation (7) proved

to be a good approximation for sizing the gas volume.

To assess the impact of pipe diameters on the gas volume, About 80 simulation runs are applied on Bentley Hammer software to the water supply system covering the impact of various pipe diameters of 300, 600, 900 and 1200 mm respectively on the gas volume. Figure 5 (a to d) compare the values of pressure drop calculated using Bentley water Hammer and those calculated from Equation (7) for pipe diameters of 300, 600, 900 and 1200 mm; respectively.

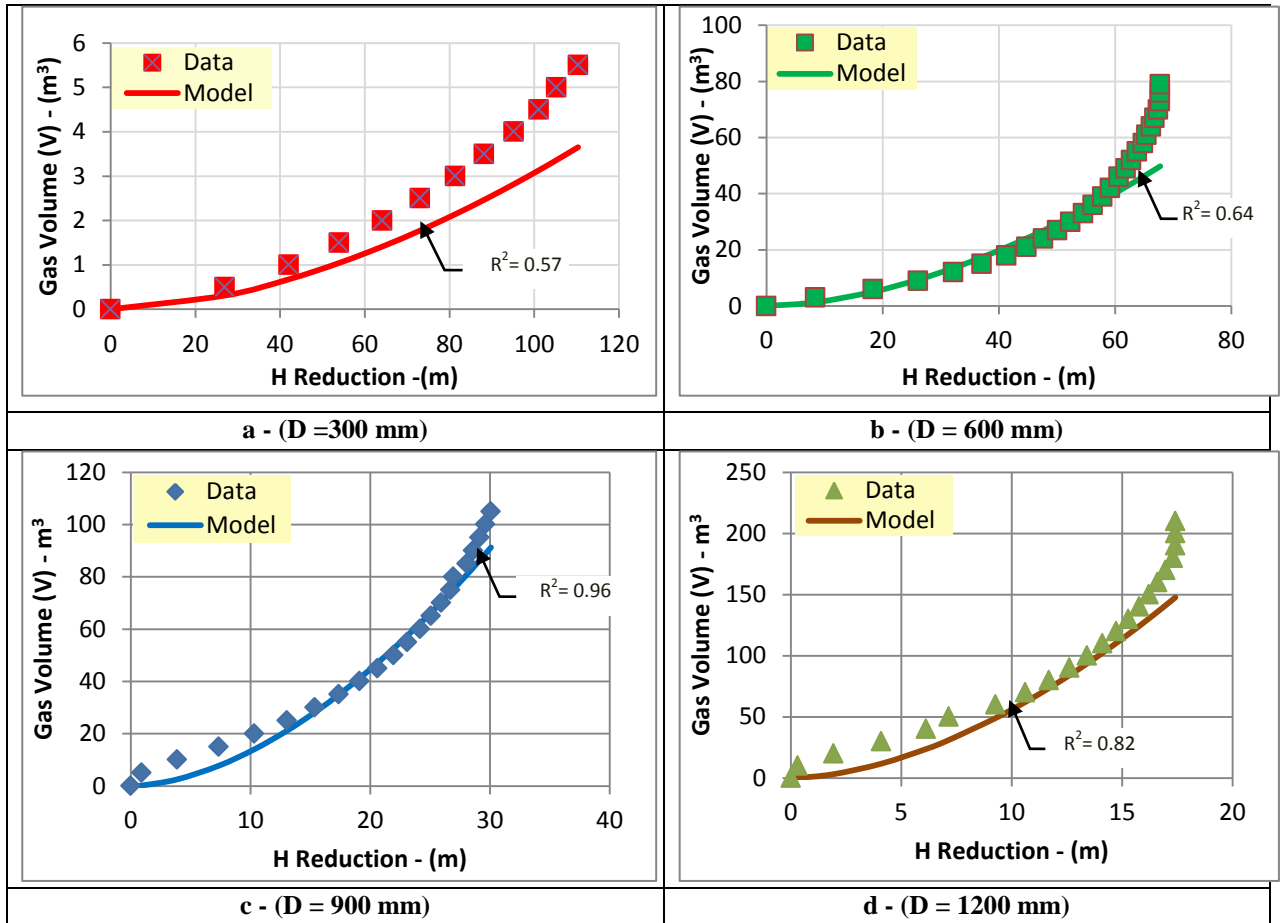


Figure (5): Gas Volume Required to Achieve Pressure Drop Reduction by Bentley Hammer and the Developed Equation

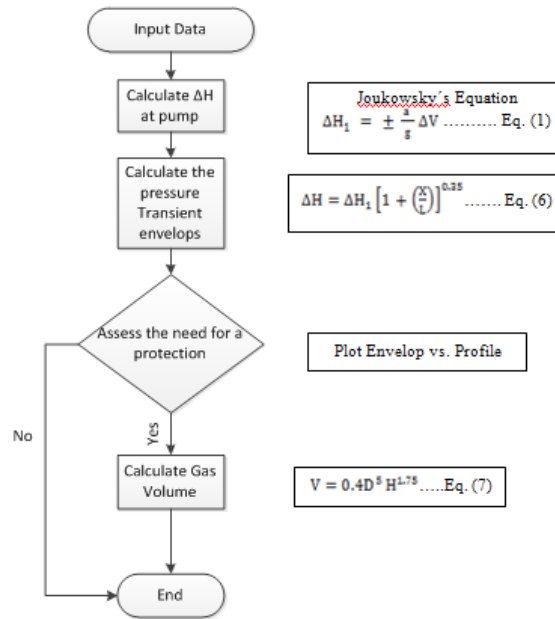
By comparing the results of the pressure drop reduction (H) with those calculated by Bentley Hammer, it is noted that the developed Equation (7) can be expressed with high agreement with ( $R^2$ ) ranges from 0.96 to 0.57 for the diameters ranges of 300 to 1200 mm respectively, and also noted that the developed formula can be expressed with high agreement for calculating the gas volume.

**Conclusion**

A simplified approach for the analysis of water hammer phenomenon has been developed the pressure transient envelops, asses the need for protection, and determine the size of the gas volume in the air vessel. After analyzing the

water hammer system, the approach can be drawn as follows:

- The direct relationship which known with Joukowsky’s equation is valid to approximately estimate the pressure drop at the pump.
- A new empirical formula is developed to calculate the maximum and minimum pressure envelops along the pipeline and to assess the needing of protection.
- A new empirical model is developed to size the gas volume in the air vessel. As such the developed simplified approach for calculating water hammer can be summarized in Figure (6).



**Figure 6: Flow Chart of the Simplified Approach for Calculating Water Hammer**

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