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FUZZY LOGIC – BASED CONTROLLER with PI COMPENSATOR in SERVO POSITIONING CONTROL SYSTEM

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ABSTRACT

Many types of drives used in positioning systems need high performance controllers to achieve good dynamic performance in the presence of system uncertainty and complex environment. Traditional control schemes like PID can not meet these requirements. On the other hand, a conventional fuzzy logic controller can usually control a nonlinear system more efficiently, and provide better performance than PID controllers in terms of shorter rise time and smaller over shot. Unfortunately, the traditional fuzzy logic controller cannot improve the steady state performance for time varying systems. To overcome this drawback, the integral of the error of the system is taken in consideration. This paper presents a hybrid of the conventional PI compensator with fuzzy logic controller to improve steady-state and dynamic accuracy of the servo position control system. The results obtained indicate that the proposed controller has an excellent position tracking performance compared with both traditional PID controller and fuzzy PD controller.

KEY WORDS

PID controllers - Fuzzy logic controller- PI compensator- Fuzzy PD controller.

INTRODUCTION

Positioning servo system control is a very challenging area in the field of control system engineering, in which different control techniques in linear and nonlinear systems have been developed. The difficulty of position servo systems is caused by its dynamical nonlinearity and complex in environment [1].

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Most types of drives used in the position servo systems require high performance controllers to guarantee good dynamic performance and position accuracy. Different control techniques have been formulated such as conventional controllers, intelligent controllers, and mixture of both with the hybridization of conventional PI control method and fuzzy logic [2,3,4]. In this paper a design methodology of fuzzy logic-based controller with the incorporation of PI compensator has been developed. The block diagram of the positioning servo system equipped with the proposed controller is illustrated in Fig.1. The servo system is composed of a Permanent-magnet brushless dc motor (three phase permanent-magnet synchronous machine) with sinusoidal back electromotive force (EMF) fed from pulse width modulated Voltage Source Inverter (VSI).

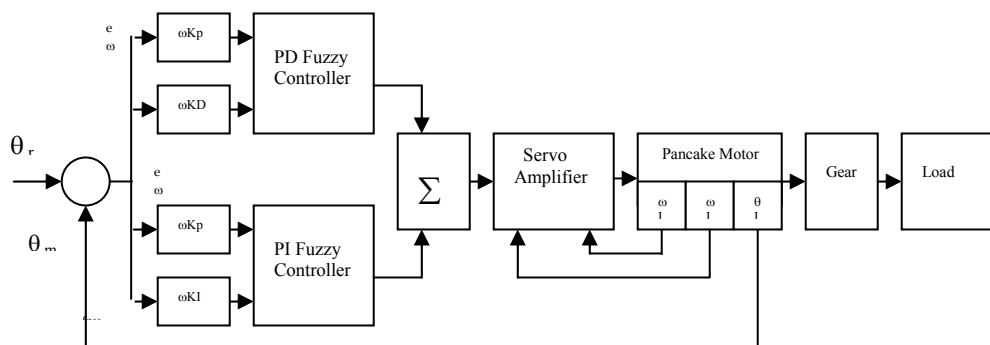


Fig.1 The block diagram of the positioning servo system equipped with PI-Fuzzy controller

The conventional proportional-integral (PI) controllers have great effect in the control of steady state error of a control system, in other words bringing down the steady-state error to zero. However, the disadvantage of this controller is its inability to improve the transient response of the system. With this controller it is very difficult to the system's percentage overshoot and the settling time, which on the other hand, can be controlled by a fuzzy PD controller. This is why many researches use the hybridization of both fuzzy controller and PI compensator [2,5,6].

MODELING OF BRUSHLESS DC SERVO MOTOR

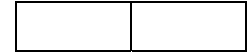
The brushless dc servo motor under consideration is a three phase permanent-magnet synchronous machine with sinusoidal back electromotive force (EMF). The voltage equations for the stator windings can be expressed as [7]:

$$\begin{bmatrix} v_{as} \\ v_{bs} \\ v_{cs} \end{bmatrix} = \begin{bmatrix} R_s & 0 & 0 \\ 0 & R_s & 0 \\ 0 & 0 & R_s \end{bmatrix} \begin{bmatrix} i_{as} \\ i_{bs} \\ i_{cs} \end{bmatrix} - \begin{bmatrix} L_s & 0 & 0 \\ 0 & L_s & 0 \\ 0 & 0 & L_s \end{bmatrix} \frac{d}{dt} \begin{bmatrix} i_{as} \\ i_{bs} \\ i_{cs} \end{bmatrix} - \omega_r k_e \begin{bmatrix} \sin(\theta_r) \\ \sin(\theta_r - 2\pi/3) \\ \sin(\theta_r + 2\pi/3) \end{bmatrix} \quad (1)$$

where

- v_{as}, v_{bs}, v_{cs} the applied stator voltages;
- i_{as}, i_{bs}, i_{cs} the applied stator currents;
- R_s the resistance of each stator winding;
- L_s the inductance of stator winding;
- ω_r the electrical rotor angular velocity;
- θ_r the electrical rotor angular displacement;
- k_e the emf constant.

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The electromagnetic torque can expressed as:

$$T_e = k_t [i_{as} \sin(\theta_r) + i_{bs} \sin(\theta_r - 2\pi/3) + i_{cs} \sin(\theta_r + 2\pi/3)] \tag{2a}$$

While the torque, speed, and position may be related by:

$$T_e = J_m (2/P) d\omega_r/dt + B_m(2/P)\omega_r + T_L \tag{2b}$$

$$\theta_r = \int \omega_r dt \tag{2c}$$

$$\omega_m = \omega_r (2/P) \tag{2d}$$

where

- k_t the current constant;
- P the number of poles;
- J_m the inertia of rotor;
- B_m the damping coefficient;
- T_L the load disturbance;
- ω_m the mechanical angular velocity of the rotor.

FUZZY-PI CONTROLLER

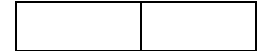
The combination of intelligent control technique and conventional control strategy bring up a new approach in designing an intelligent robust control system. Fuzzy control as one branch of intelligent control, is easy to understand, easy to operate, it has a quick response and it doesn't need system model [4]. The input of fuzzy controller is the system error and the changing of errors, thus it can be taken as PD controller. Its dynamic characteristics are good and can get stable state smoothly. But its anti-noise is not good and cannot improve the steady state performance. To overcome the disadvantages of both control strategies and to enhance the dynamic system performance fuzzy control and PI compensator have been used at the same time. The two inputs of fuzzy PD controller are the error signal $e(t)$ and the derivative of error $ce(t)$. In the proposed positioning servo system the fuzzy input vector comprises the following variables:

$$e(k) = \theta_r(k) - \theta_m(k) \tag{3}$$

$$ce(k) = e(k) - e(k-1) \tag{4}$$

where

$e(k)$ is the error at k^{th} sampling interval



$ce(k)$ is the change of error at k^{th} sampling interval

$\theta_r(k)$ is the reference position at k^{th} sampling interval

$\theta_m(k)$ is the motor shaft position at k^{th} sampling interval

The output of the fuzzy controller is the control voltage and is defined as:

$$U_c(k) = G_u * \Delta U_c(k) \tag{5}$$

Where:

$\Delta U_c(k)$ is the output signal of fuzzy controller at k^{th} sampling interval

G_e, G_{ce}, G_u are the gain factors of the fuzzy controller of fig .1.

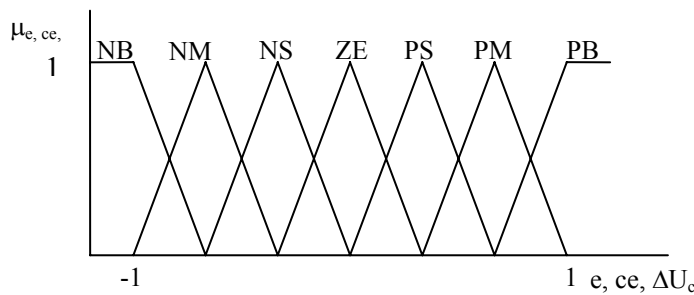


Fig.2 Membership function for $e, ce, \Delta U_c$

The membership classes for the input variables $e(k)$ and $ce(k)$, and the output variable $\Delta U_c(k)$ are shown in Fig.2. The universe of discourse (UOD) for both inputs and outputs is divided into seven fuzzy subsets: NB (Negative Big), NM (Negative Medium), NS (Negative Small), ZE (Zero), PS (Positive Small), PM (Positive Medium), PB (Positive Big). The UOD covers a wide range of positive and negative change of the variables $e(k)$, $ce(k)$ and $U_c(k)$. The values of $e(k)$, $ce(k)$, and $U_c(k)$ are normalized. Table (1) depicts the output decoding-rule which represents the output control signal $\Delta U_c(k)$ for all combinations of input variables.

Table(1) Rule base for the position controller

| $ce \backslash e$ | NB | NM | NS | ZE | PS | PM | PB |
|-------------------|----|----|----|----|----|----|----|
| NB | NB | NB | NB | NB | NM | NS | ZE |
| NM | NB | NB | NB | NM | NS | ZE | PS |
| NS | NB | NB | NM | NS | ZE | PS | PM |
| ZE | NB | NM | NS | ZE | PS | PM | PB |
| PS | NM | NS | ZE | PS | PM | PB | PB |
| PM | NS | ZE | PS | PM | PB | PB | PB |
| PB | ZE | PS | PM | PB | PB | PB | PB |

The rule assignment table is designed using human expertise to generate the output rule when knowing the input rule.



SIMULATION RESULTS

With the proposed controller, the motor's angular position should follow arbitrary predetermined reference tracks without overshoot. For verifying the effectiveness of the proposed controller, PID controller and conventional fuzzy PD controller are compared with Fuzzy-PI controller. Also to demonstrate the robustness of the proposed controller the position tracking errors were investigated when the load is disturbed during trajectory control. The PID parameters were adjusted (or "tuned") for meeting the performance criteria Fig.3 shows the performance of the system for step input under exceeding the load by 30%. Fig.4 illustrates the position errors of PID controller, conventional fuzzy PD, and Fuzzy-PI controller. final position errors of the controllers have been presented in table (2), Fig.5, and Fig.6, and Fig.7 present the response of the system when it is disturbed by an impulse at .05 sec. It is clear that Fuzzy-PI controller has much better response than PID and conventional fuzzy PD controller even when the system is disturbed, because the response time is short, no overshoot, and it has no steady- state error.

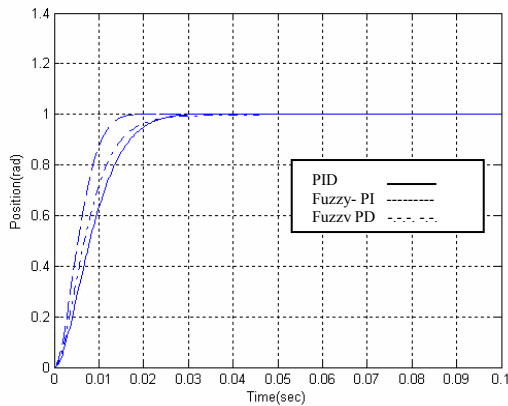


Fig.3 The response of the system Without variation in system parameters

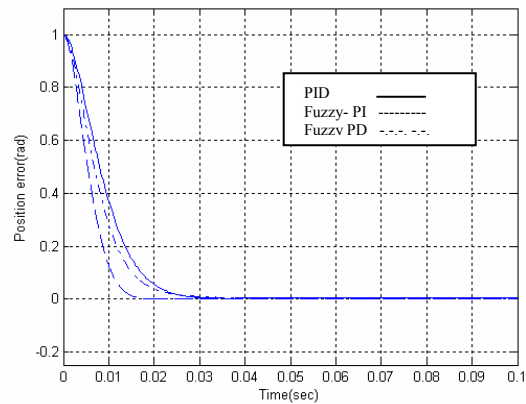


Fig.4 The position errors of controllers

Table (2) the final Position errors

| Steady-state error (rad) after disturbance | | |
|--|----------|----------|
| PID | Fuzzy PD | Fuzzy-PI |
| 0.003853 | 0.002047 | 0.000154 |

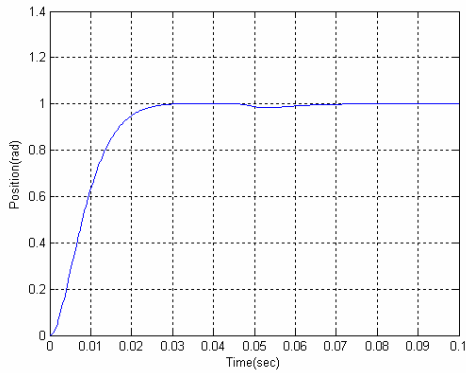


Fig.5 The response of the system with PID controller under disturbance

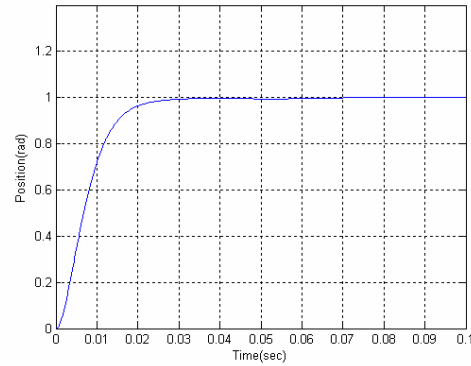


Fig.6 The response of the system with fuzzy PD controller under disturbance

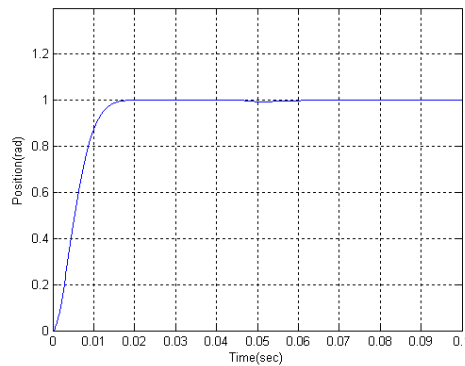


Fig.7 The response of the system with Fuzzy-PI controller under disturbance

Fig.8 indicates the input sinusoidal trajectory, while the investigation of comparing the position tracking errors of controllers when the load is step increased by 30% is illustrated in Fig.9. It is obvious that Fuzzy-PI controller offers the best position tracking error tracking when the load is disturbed

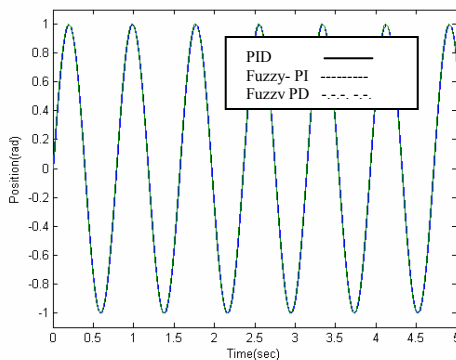


Fig.8 The response of the system with fuzzy PD controller under disturbance

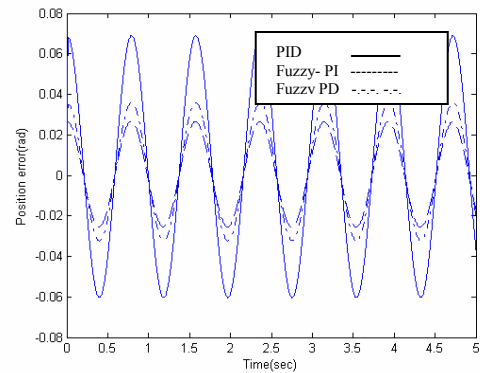
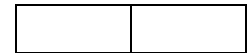


Fig.9 The position tracking error after the load is increased by 30%



CONCLUSION

The paper developed a combination of fuzzy logic and a proportional – integral controller for enhancing the dynamic performance and controlling the steady-state error of the positioning control system. The simulation results showed that the method of combination of fuzzy logic and proportional-integral controller is not only robust, but also can improve the dynamic performance of the positioning control system it also enhances its anti-error under the variation of system parameters or the load conditions.

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