# INVESTIGATION ?'HE OPTIMUM CONDITIONS OF GRAIN MILLING 

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ABSTRACT
The objective of this work is to study the optimum conditions of grain milling during the milling process, and find out the best values for the design parameters (disc diameter, crossing angle of furrows, disc weight and rotational speed).

## INTRODUCTION

A metallic-disc mill [1] was choosen for this study. It is composed of two horizontal, parallel and coaxial discs. The discs are made from grey cast iron having $160 \mathrm{H} . \mathrm{B}$, and the distance between them may be adjusted in order to meet the requirements of the grains to be milled. The upper disc is rotary and has an open hole in the centre through which the grains may be passed, while the lower disc is stationary. The grains which fall through the open hole of the upper disc are pulled and moved outward by centrifugal forces.

## STRESSES IN THE ROTARY DISC

The particles of a rotary disc are under the action of centrifugal forces which try to tear off the particles from the disc. Thus internal stresses are created in the disc.
Consider an element of the rotary disc. The various stresses acting on it are indicated in the Fig. (1). Solution for these stresses are given as below :
Radial stress $\sigma_{r}$ at the radius $r$ of a hollow disc of internal radius $r_{i}$

$$
\begin{align*}
& \text { and external radius } r_{0} \text { is given by equation } \\
& \qquad \sigma_{r}=\left(\frac{3+\nu}{8}\right) \frac{\rho \omega^{2}}{g}\left(r_{i}^{2}+r_{0}^{2}-r^{2}-\frac{r_{i}^{2} r_{0}^{2}}{r^{2}}\right) \tag{1}
\end{align*}
$$

and the hoop stress $\theta$ is given by :

$$
\begin{equation*}
\sigma_{\theta}=\left(\frac{3+\nu}{8}, \frac{\rho \omega^{2}}{g}\left[r_{i}^{2}+r_{o}^{2}-\frac{1+3}{3+} r^{2}+\frac{r_{o}^{2} r_{i}^{2}}{r^{2}}\right]\right. \tag{2}
\end{equation*}
$$

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| :---: | :---: |

The maximum radial stress occurs at $r=\sqrt{r_{0} r_{i}}$
Thus $\left(\sigma_{r}^{\prime}\right) \max =\frac{\rho \omega^{2}}{g} r_{0}^{2}\left(\frac{3+\nu}{8}\right)\left(1-\frac{r_{i}}{r_{0}}\right)^{2}$
and
The maximum hoop stress occurs at $r=r_{i}$
Thus $\left(\sigma_{\theta}\right) \max =\frac{\rho \omega^{2}}{g} r_{0}^{2} \frac{(3+\nu)}{4}\left(1+\frac{1-\nu}{3+\nu} \frac{r_{i}^{2}}{x_{0}^{2}}\right)$
The allowable speed can be calculated based on the distortion energy theory [2] as follows:

$$
\begin{equation*}
\text { (al) max }=\left[\frac{8 g \partial a}{\rho(3+\nu) r_{0}^{2}}\left\{\frac{1}{2+\left(\frac{r_{1}}{r_{0}}\right)^{2}\left(1-\frac{(1+3 \nu)}{3+\nu}\right)}\right\}\right]^{\frac{1}{2}} \tag{5}
\end{equation*}
$$

ACTING FORCES ON THE GRAIN
The acting forces on the grain during the milling process may be divided into the following items :-

$$
\begin{align*}
& \quad \text { Frictional Forces Due to the Rotary Disc } \\
& F_{f l}=\mu_{l}^{\mu_{1}} \frac{W_{d}}{n_{g}}  \tag{6}\\
& F_{f 2}=\mu_{2} \frac{W_{d}}{V_{g}} \\
& F_{V}=\frac{W_{d}}{n_{g}} \tag{7}
\end{align*}
$$

where

$$
\begin{align*}
n_{g}= & \frac{A_{d}}{A_{g}} \cdot K_{0} \\
& \text { Centrifugal Force of Grain } \\
F_{c}= & M_{g} w_{g}^{2} \quad q=\frac{M_{g} w^{2} q^{3}}{s_{0}^{2}} \tag{9}
\end{align*}
$$

where ,

$$
w_{g}=\frac{w_{g}}{s_{0}}
$$

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## Shearing Force

$$
\begin{equation*}
F_{s h}=\sigma_{s h} A_{s h} \tag{10}
\end{equation*}
$$

The grain movement may be described as a multiturn spiral w.r.t the stationary disc, and the absolute velocity may be obtained from the equation of multiturn spiral. The spiral equation can be written as follows:

$$
\begin{equation*}
q=k \theta[3] \tag{11}
\end{equation*}
$$

where

$$
\mathrm{K}=\mathrm{a} / 2 \pi
$$

The above equation is plotted in Fig. (2). The acting resultant force on the grain $\mathrm{F}_{\mathrm{g}}$ during the milling process can be obtained as follows:

$$
\begin{equation*}
F_{g}=\sqrt{\left(F_{\operatorname{sh}} \sin \alpha-F_{q}\right)^{2}+\left(F_{\Theta}+F_{V}+F_{\operatorname{sh}} \cos \alpha\right)^{2}} \tag{12}
\end{equation*}
$$

where,
$F_{q}=M_{g}\left(\frac{\omega}{S_{o}}\right)^{2} q^{3}$, $F_{\theta}=2 M_{g}\left(\frac{\omega}{S_{o}}\right)^{2} q^{3} K$ and $F_{v}=\frac{w_{d}}{n_{g}}$

Substituting the values of $F_{q}, F_{\theta}$ and $F_{V}$ in eq. (12), yields ;
$F_{g}=\sqrt{\left(F_{\operatorname{sh}} \sin \alpha-M_{g}\left(\frac{\omega}{S_{0}}\right)^{2}+\left(2 M_{g}\left(\frac{\omega}{S_{0}}\right)^{2} q^{2} k+\frac{W_{d}}{n_{g}}+F_{s h} \cos \alpha\right)^{2}\right.}$
From eq. (13), it is clear that the acting resultant force on the grain during the milling process depends on the crossing angle ( $\propto$ ), rotational speed ( $w$ ) of the rotary disc, variable radial vector ( $q$ ) and the the weight of the rotary disc $\left(W_{d}\right)$.
The value of the optimum rotational speed of the rotary disc must not exceed $22 \mathrm{rad} / \mathrm{sec}$ [4] to avoid the increase in flour temperature which in turn leads to unfavorite change its coleur.

$$
\begin{aligned}
\text { Let, } & =20 \mathrm{rad} / \mathrm{sec}, \mathrm{~K}=0.016 \mathrm{~m}, W_{g}=0.05 \times 10^{-3} \mathrm{~kg}, A_{\mathrm{g}}=0.12 \times 10^{-4} \mathrm{~m}^{2}, \\
G_{S h} & =2.1[4] \mathrm{kg} / \mathrm{mm}^{2}, K_{O}=0.06, a=0.1 \mathrm{~m}, A_{\mathrm{Sh}}=0.011 \times 10^{-4} \mathrm{~m}^{2}, \\
S_{O} & =2 \times 10^{-3} \mathrm{~m} .
\end{aligned}
$$

Substituting from equations (8-11) into equation (13) and using the above values yields ;

$$
\begin{equation*}
F_{g}=\sqrt{\left(2.373 \sin \alpha-505 q^{3}\right)^{2}+\left(16.31 q^{2}+8.98 \times 10^{-7} \mathrm{w}_{\mathrm{d}}\right)^{2}} \tag{14}
\end{equation*}
$$

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## RESULTS AND DISCUSSION

Figure (3) shows the effect of the crossing angle (o) on the resultant force. It can be seen that the force ( $F_{q}$ ), that acts on the grain, decreases very slightly with an increase in the crossing angle.
Small crossing angles cause high reduction rate of the semi-product which consequently consumes high power. This will lead to choose the crossing angle in the range from 30 to 50 degrees.
Figure (4) represents the relation between the weight of the rotary disc and the resultant force acting on the grain. It can be noticed that the relation is almost a horizontal straight line which means that the resultant force can be considered to be constant with the weight of the disc. The effect of the variable radial vector $(q)$ on the resultant force is shown in Fig. (5). It is clear that the resultant force increases with an increase in the variable radial vector, which is thought to be logical. The best value of (q) lies in the range from 0.45 to 0.5 m . Above this range, the increase in (q) will cause more power consumption.

## CONCLUSIONS

The following conclusions may be drawn from this study :
1- The best value of crossing angle of furrows lies between $\left(30-50^{\circ}\right)$.
2- The best value of the disc diameter lies between ( $0.9-1.2$ ) meter, and the ratio between the inner and outer radius of the rotary disc must be not less than 0.3 .
3- The weight of the rotary disc has a very small effect on the acting resultant force on the grain.
4- The frictional forces between the grain and the disc surfaces have a significant effect on the milling quality.
5- The best value of the rotational speed is $22 \mathrm{rad} / \mathrm{sec}$ to avoid an increase of flour temperature and bad colour of Elour.

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## REFERENCES

1- Nasser, A.A. , Serag, S. Eineen, M. and Ahmed, S., "Design Consideration and Theoretical Analysis of Grain Milling Between Two Metallic Disc", 2nd International Conference, PEDAC, Alexandria Univ, Dec, 1983.
2- Pujara,k.K. , and Juneja, B.t., "Machine Design", lst Edit., Pub: by J.C.Kapur for Dhanpat \& Rai \& Sons, Delhi-Jullundur (1976).

3- VYGODSKY, M. "Mathematical Hand Book Higher Mathematics", Mir Publisher, pp. 781-785, Moscow (1971).
4- El-Kady, A. and El-Shazli。A. "Engineering and Milling Technology", Vol. I, lst Edit., Pub. by General Egyptian Organization for Mills, Silos and Bakers, Egypt (1971).

## NOMENCLATURE

$\propto$ : Crossing angle of furrows in degrees
$\nu$ : Poisson ratio dimensionless
N: Coefficient of friction between the grain and the disc surface

| $\rho$ | : Density of the material of the disc | $\mathrm{kg} / \mathrm{cm}^{3}$ |
| :---: | :---: | :---: |
| $\theta$ | : Grain rotating angle from the initial position | degrees |
| $\omega$ | : Angular velocity of the rotary disc | rad/sec |
| $\omega_{g}$ | : Grain angular velocity | rad/seç |
| Oa | : The allowable or design stress | $\mathrm{kg} / \mathrm{cm}_{2}^{2}$ |
| ${ }_{\text {O }}{ }_{\text {a }}$ | : Grain shear stress | $\mathrm{kg} / \mathrm{mm}^{2}$ |
|  | - The lead of the spiral | $\mathrm{m}_{2}$ |
| ${ }^{A}{ }^{\text {a }}$ g | : Grain Cross-Section area | $\mathrm{m}_{2}$ |
| ${ }^{\text {A }}$ sh | : Shearing area of the grain | $\mathrm{m}^{2}$ |
| $\mathrm{D}_{\mathrm{d}}$ | : Disc diameter | m |
| $\mathrm{F}^{\text {d }}$ | : Centrifugal force | kg |
| $\mathrm{F}_{\mathrm{g}}$ | : Resultant force | kg |
| $\mathrm{F}_{\mathrm{q}}$ | : Radial force component | kg |
| $F_{\theta}^{q}$ | : Normal force component | kg |
|  | : Shearing force | kg |
| $\mathrm{K}^{\text {Sh }}$ | : The Parameter of the spiral | m |
| K | : Contact factor between the grain and the disc surface |  |
| $\mathrm{M}_{\mathrm{g}}$ | : Mass of grain | kg |
| $\mathrm{n}^{9}$ | : 'The number of grains that are milled in the same time | grain |
| $\mathrm{F}_{\mathrm{V}}$ | - Vertical load | kg |
| q | : Variable radial vector | m |
| $\mathrm{r}_{1}$ | : Internal radius of the disc | m |
| $r_{0}^{1}$ | - External radius | m |
| $\mathrm{S}_{0}$ | - Grain thickness | m.m |
| W | : Disc weight | kg |



Pig. 8: Plofied the equation a $\mathfrak{K}$.







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