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## PERFORMANCE ANALYSIS OF 49-QPRS THROUGH NONLINEAR SATELLITE CHANNELS IN THE PRESENCE OF GAUSSIAN NOISE AND COCHANNEL INTERFERENCE

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**ABSTRACT** : This paper is concerned with the analytical performance analysis and evaluation of 49-ary Quadrature Partial Response Signaling when transmitted through nonlinear satellite channel in the presence of Additive White Gaussian Noise and Co-channel Interference ; in both uplink and downlink channels . The main source of the nonlinearities is the Traveling Wave Tube Amplifier on-board of the satellite. The transponder nonlinearities considered in this paper are due to : input amplitude -to-output amplitude conversion and input amplitude-to-output phase conversion . The cochannel interference results from interferers in the passband of the coherent receiver . The results in terms of the dependence of the average symbol error probability upon the uplink and downlink ; signal-to-noise ratio's and " signal -to - cochannel interference signal ratio's at different values of Back-Off from saturation operation of the Traveling Wave Tube Amplifier on-board of the satellite are illustrated . The results showed that the Back-Off value is the dominant factor in determining the system performance .The appropriate values of the threshold levels ; d's and compensation phases ;  $\theta$ 's at the receiver are highly correlated and can only be arrived at by minimizing the average symbol error probability .

### Key Words :

Quadrature Partial Response Signaling ; QPRS - Additive White Gaussian Noise ; AWGN Co-channel Interference ; CCI - Traveling Wave Tube Amplifier ; TWTA - Input amplitude -to-output amplitude conversion ; AM/AM -Input amplitude-to-output phase conversion ; AM/PM -The average symbol error probability;  $P_e$  - Signal-to-noise ratio's ;  $\rho_{nu}$  and  $\rho_{nd}$  - Signal -to - cochannel interference signal ratio's ;  $\rho_{cu}$  and  $\rho_{cd}$  - Back-Off from saturation operation of the TWTA ; BO - Threshold levels ; d's -compensation phases ;  $\theta$ 's at the receiver and Average symbol error probability;  $P_e$

### I-INTRODUCTION

The duobinary " correlative coded technique" signal introduces a controlled amount of Intersymbol Interference ( ISI ) in order to simplify the filter design ; particularly the phase-equalization problem ; and to enable the transmission at ; or slightly higher ; the Nyquist rate [ 1 ] .

The 49-ary QPRS consists of two seven-level duobinary ; partial response baseband signals (PRS) which are modulating two orthogonal carriers. One of the main advantages of QPRS as compared to equivalent schemes is that they are speed tolerant, i.e., it is possible to transmit at rate which is higher than Nyquist rate without suffering significant degradation [1] and [2] . The 49-ary QPRS is expected to find increased applications in the future communication by satellite or microwave radio link due to its spectrum efficiency ;  $\geq 4$  bits / sec. / Hz of the IF-bandwidth , its relative simplicity of implementation and good error performance through linear Gaussian channels [3] - [6] . Performance of another schemes such as 16-ary QAM , 16-ary QAM/MSK , 16-ary CPSK and 9-ary QPRS through nonlinear satellite channel in the presence of AWGN are illustrated in [7] - [10] respectively .

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The purpose of this paper is to present an analytical performance evaluation of 49-ary QPRS in the presence of TWTA nonlinearities ; AWGN and CCI preceding and following the nonlinearities . In Section -II the average symbol error probability ; Pe analysis is presented . In section-III ; computation aspects , results and comments are presented . Section IV is concerned with the conclusion about the results .

## II-AVERAGE SYMBOL ERROR PROBABILITY ANALYSIS

Assuming the system model shown in Fig.(1) ; the modulated QPRS ;  $S_1(t)$  during any symbol duration ;  $T_s$  may be written as:

$$S_1(t) = \mu_1(t) \cos \omega_c t - \lambda_1(t) \sin \omega_c t \quad (1)$$

Where.  $\omega_c = 2 \pi f_c$  ,  $f_c$  is the carrier frequency ,  $P(t)$  is the pulse shape defined by :

$$\begin{aligned} P(t) &= A & 0 \leq t \leq T_s ; \text{ and} \\ &= 0 & \text{elsewhere} \end{aligned}$$

$$\mu_1(t) = a P(t) \quad \text{and} \quad \lambda_1(t) = b P(t) ; \quad (2)$$

$T_s$  is the symbol duration , a and b are two independent random variables and are  $\in \{-6,-4,-2,0,2,4,6\}$  with probabilities  $\in \{1/16,2/16,3/16,4/16,3/16,2/16,1/16\}$  respectively . It is assumed that  $a_i$  and  $a_j$  or  $b_i$  and  $b_j$  are independent for all values of  $i \neq j$  .

The uplink signal  $S_1(t)$  is corrupted with the uplink narrow-band Gaussian noise  $n_u(t)$  . The resultant signal at the input of TWTA on-board the satellite's transponder may be written as :

$$S_i(t) = R(t) \cos [\omega_c t + \phi_i(t)] \quad (3)$$

Where.  $R^2(t) = [X_1^2(t) + Y_1^2(t)] \quad (4)$

$$\begin{aligned} X_1(t) &= \mu_1(t) + n_{uc}(t) + C_{uc}(t) , \text{ and} \\ Y_1(t) &= \lambda_1(t) + n_{us}(t) + C_{us}(t) \end{aligned} \quad (5)$$

$$\phi_i(t) = \tan^{-1} [ Y_1(t) / X_1(t) ] \quad (6)$$

$n_{uc}(t)$  and  $n_{us}(t)$  are the uplink ; inphase and quadrature components of the uplink AWGN , each are independent with zero mean and variance  $\sigma_{nu}^2$  ; and  $C_{uc}(t)$  and  $C_{us}(t)$  are the uplink ; inphase and quadrature components of the interfering signal and are assumed to be originated independently of each other and of the transmitted signal or noise sources . They are represented in [ 9 ] as follows :

$$\begin{aligned} C_c(t) &= \sum_i B_i \cos [ (\omega_i + \omega_c) t + \gamma_i(t) + \epsilon_i ] , \text{ and} \\ C_s(t) &= \sum_i B_i \sin [ (\omega_i + \omega_c) t + \gamma_i(t) + \epsilon_i ] \end{aligned} \quad (7)$$

Where.  $i = 1,2,3,\dots,N_c$  represent the number of interferers ( in this work  $i = 1$  ) ;

- $B_i$  represents the amplitude of ith interferer ;
- $\gamma_i(t)$  represents the digital modulated phase ; and
- $\epsilon_i$  represents the digital unmodulated phase which uniformly distributed  $(0, 2\pi)$

The signal  $S_i(t)$  is degraded by the TWTA , the output signal  $S_o(t)$  may be given as :

$$S_o(t) = F [ R(t) ] \cos \{ \omega_c t + \phi_i(t) - \psi [ R(t) ] + \theta \} \quad (8)$$

Where .  $F [R]$  denotes the AM/AM conversion function ;

.  $\psi [R]$  denotes the AM/PM conversion function ; and

.  $\theta$  represents the compensation phase in radians at receiver to account for the average AM / PM conversion .

The signal  $S_o (t)$  is corrupted with the downlink Gaussian noise  $n_d (t)$  and cochannel interference  $C_d (t)$  to give the signal  $S_2 (t)$  at the input to the coherent receiver as:

$$S_2(t) = X_2 (t) \cos (\omega_c t) - Y_2 \sin (\omega_c t) \quad (9)$$

Where .  $X_2(t) = \mu_2(t) + n_{dc}(t) + C_{dc}(t)$  ;

.  $Y_2(t) = \lambda_2(t) + n_{ds}(t) + C_{ds}(t)$  ;

.  $\phi_o(t) = \phi_i(t) - \psi [R(t)] + \theta$  ;

.  $\mu_2(t) = F [R(t)] \cos [\phi_o(t)]$  ; and

.  $\lambda_2(t) = F [R(t)] \sin [\phi_o(t)]$  (10)

.  $n_{dc}(t)$  and  $n_{ds}(t)$  are the downlink ; inphase and quadrature components of the downlink AWGN, each of which with zero mean and variance  $\sigma_{nd}^2$  ; and

.  $C_{dc}(t)$  and  $C_{ds}(t)$  are the downlink ; inphase and quadrature components of the cochannel interference

The receiver coherently demodulate the input signal  $S_2 (t)$  to give the inphase and quadrature components of the baseband signal  $X_2(t)$  and  $Y_2(t)$  . The later are sampled at  $t = t_0 + k T_s$  ,  $0 \leq k \leq T_s$  . A decision is made to estimate the receiving symbol corresponding to the transmitted symbol . The diagram of Fig.(2) illustrates all possible components of the baseband received samples in the absence of any degradation and the regions for correct decision ;  $R_i$  corresponding to the transmitted elements  $A_i$  ,  $i = 1,2,3,4, 5,6, \dots, 49$ .

Since each element  $A_i$  in the transmitted set has its specific probability of existence ,  $p(A_i)$  and conditional error probability ;  $p_{e, A_i}$  it follows that the average symbol error probability  $P_e$  for 49-ary QPRS may be given as :

$$P_e = \sum_i p(A_i) \cdot p_{e, A_i} \quad (11)$$

Where .  $p(A_1) = p(A_7) = p(A_{13}) = p(A_{19}) = 1/256$  ;  
 $p(A_8) = p(A_{14}) = p(A_{20}) = p(A_{26}) = 2/256$  ;  
 $p(A_{15}) = p(A_{21}) = p(A_{27}) = p(A_{33}) = 3/256$  ;  
 $p(A_{16}) = p(A_{22}) = p(A_{28}) = p(A_{34}) = 4/256$  ;  
 $p(A_2) = p(A_6) = p(A_{12}) = p(A_{18}) = 2/256$  ;  
 $p(A_3) = p(A_5) = p(A_{11}) = p(A_{17}) = 3/256$  ;  
 $p(A_{10}) = p(A_{16}) = p(A_{22}) = p(A_{28}) = 6/256$  ;  
 $p(A_{17}) = p(A_{19}) = p(A_{31}) = p(A_{33}) = 9/256$  ;  
 $p(A_4) = p(A_{12}) = p(A_{20}) = p(A_{28}) = 4/256$  ;  
 $p(A_{11}) = p(A_{23}) = p(A_{27}) = p(A_{39}) = 8/256$  ;  
 $p(A_{18}) = p(A_{24}) = p(A_{26}) = p(A_{32}) = 12/256$  ;  
 $p(A_{25}) = 16/256$

The conditional error probabilities  $p_{e, A_i}$ 's are also equal ; as given in (12); for example :

$$p_{e, A_1} = p_{e, A_7} = p_{e, A_{43}} = p_{e, A_{49}} \quad ; \quad \text{and so on for the other equalities} \quad (13)$$

Substituting from (12) and (13) into (11) yields :

$$p_e = (1/64) [ 4 p_{e, A_{25}} + 12 p_{e, A_{32}} + 8 p_{e, A_{39}} + 4 p_{e, A_{48}} + 9 p_{e, A_{33}} + 6 p_{e, A_{40}} + 3 p_{e, A_{47}} \\ + 2 p_{e, A_{48}} + 4 p_{e, A_{41}} + 6 p_{e, A_{34}} + 3 p_{e, A_{35}} + 2 p_{e, A_{42}} + p_{e, A_{25}} ] \quad (14)$$

It is evident that the error probability assuming  $A_i$  is transmitted may be written as :

$$p_{e, A_i} = 1 - \iint_{R_i} p_{A_i}(X_2, Y_2) dX_2 dY_2 \quad (15)$$

Where  $p_{A_i}(X_2, Y_2)$  denotes the joint probability density function ; pdf of  $X_2, Y_2$  assuming that element  $A_i$  is transmitted .

Using Bayes rules for conditional probability ; (15) may be written as :

$$p_{e, A_i} = 1 - \iint_{R_i} [ \iint_{-\infty}^{\infty} p(X_2, Y_2 / X_1, Y_1) p_{A_i}(X_1, Y_1) dX_1 dY_1 ] dX_2 dY_2 \quad (16)$$

Using the fact that : integration process are linear transformation or mapping , ( 16 ) may be written as :

$$p_{e, A_i} = 1 - \iint_{-\infty}^{\infty} [ \iint_{R_i} p(X_2, Y_2 / X_1, Y_1) p_{A_i}(X_1, Y_1) dX_2 dY_2 ] dX_1 dY_1 \quad (17)$$

Where  $p(X_2, Y_2 / X_1, Y_1)$  denotes the joint pdf of  $X_2$  and  $Y_2$  conditioned upon  $X_1$  and  $Y_1$  assuming that the signal element  $A_i$  is transmitted .

.  $R_i$  defines the region for correct decision when  $A_i$  is transmitted .

.  $p_{A_i}(X_1, Y_1)$  is the joint pdf of  $X_1$  and  $Y_1$  assuming  $A_i$  is transmitted .

Assuming sampling of the random processes defined by (5) ; both  $n_{uc}(t)$  and  $n_{us}(t)$  are Gaussian random processes , at specific time ( $t_0$ ) , may be regarded as independent Gaussian random variables  $n_{uc}$  and  $n_{us}$  respectively ; each with zero mean and standard deviation  $\sigma_{nu}$  whilst  $C_{uc}$  and  $C_{us}$  are the inphase and quadrature components random variables associated with the uplink cochannel interference . The joint pdf of  $X_1$  and  $Y_1$  conditioned upon  $C_{uc}$  and  $C_{us}$  is given as follows :

$$p_{A_i}(X_1, Y_1 / C_{uc}, C_{us}) = (1/2 \pi \sigma_{nu}^2) \exp - [ (X_1 - \mu_1 - C_{uc}) / (\sqrt{2} \sigma_{nu}) ]^2 \\ \exp - [ (Y_1 - \lambda_1 - C_{us}) / (\sqrt{2} \sigma_{nu}) ]^2 \quad (18)$$

Assuming sampling of the random processes defined by (9) , both  $n_{dc}(t)$  and  $n_{ds}(t)$  are Gaussian random processes , at specific time ( $t_0$ ) , may be regarded as Gaussian random variables  $n_{dc}$  and  $n_{ds}$  respectively ; each with zero mean and standard deviation  $\sigma_d$  . Thus the conditional pdf may be given as :

$$p(X_2, Y_2 / X_1, Y_1 \text{ and } C_{uc}, C_{ds}) = (1/2 \pi \sigma_{nd}^2) \exp -[(X_2 - \mu_2 - C_{dc}) / (\sqrt{2} \sigma_{nd})]^2 \cdot \exp -[(Y_2 - \lambda_2 - C_{ds}) / (\sqrt{2} \sigma_{nd})]^2 \quad (19)$$

Using Taylor series expansion about  $[(X_1 - \mu_1) / (\sqrt{2} \sigma_{nu})]$  and  $[(Y_1 - \lambda_1) / (\sqrt{2} \sigma_{nu})]$  for (18) and ;  $an(X_2 - \mu_2) / (\sqrt{2} \sigma_{nd})$  and  $(Y_2 - \lambda_2) / (\sqrt{2} \sigma_{nd})$  for (19) . The conditional pdf in (18) and (19) transform to the following forms :

$$p_{Ai}(X_1, Y_1) = (1/2\pi\sigma_{nu}^2) \cdot \sum_{m=0}^{\infty} \sum_{n=0}^{\infty} (-1)^{m+n} \cdot \{1/(\sqrt{2}\sigma_{nu})\}^{2m+2n} \cdot b_{2m,2n} \cdot \exp -[(X_1 - \mu_1) / (\sqrt{2}\sigma_{nu})]^2 \cdot \exp -[(Y_1 - \lambda_1) / (\sqrt{2} \sigma_{nu})]^2 \cdot H_{2m} [(X_1 - \mu_1) / (\sqrt{2}\sigma_{nu})] \cdot H_{2n} [(Y_1 - \lambda_1) / (\sqrt{2} \sigma_{nu})] \quad (20)$$

$$p(X_2, Y_2 / X_1, Y_1) = (1/2\pi\sigma_{nd}^2) \cdot \sum_{k=0}^{\infty} \sum_{l=0}^{\infty} (-1)^{k+l} \cdot \{1/(\sqrt{2}\sigma_{nd})\}^{2k+2l} \cdot a_{2k,2l} \cdot \exp -[(X_2 - \mu_2) / (\sqrt{2}\sigma_{nd})]^2 \cdot \exp -[(Y_2 - \lambda_2) / (\sqrt{2} \sigma_{nd})]^2 \cdot H_{2k} [(X_2 - \mu_2) / (\sqrt{2}\sigma_{nd})] \cdot H_{2l} [(Y_2 - \lambda_2) / (\sqrt{2} \sigma_{nd})] \quad (21)$$

Where .  $b_{2m,2n}$  and  $a_{2k,2l}$  are the coefficients of infinite double power series expansion of the joint characteristic functions of the uplink random variables  $C_{uc}$  and  $C_{us}$  ; and downlink random variables  $C_{dc}$  and  $C_{ds}$  respectively for one interferer [9] and [10] .

.  $H_{2m}(\cdot)$  and  $H_{2n}(\cdot)$  ; and  $H_{2k}(\cdot)$  and  $H_{2l}(\cdot)$  are calculated from the recurrence relationship for the Hermit Polynomial defined by :

$$H_{m+1}(X) = [2X \cdot H_m(X) - 2m \cdot H_{m-1}(X)] \quad , \text{ given that } H_0(X) = 1 \text{ and } H_1(X) = 2X \text{ constitute the starting points for evaluating } H_m(X) \text{ for all values of } m$$

Substitute (20) and (21) into (17) ; for element  $A_i$  ,  $i = 25$  as an example , we get:

$$p_{e, A_{25}} = 1 - \iint_{-\infty}^{\infty} F(X_1, Y_1) p_{Ai}(X_1, Y_1) dX_1 dY_1 \quad (22)$$

Where .  $p_{Ai}(X_1, Y_1)$  given in (20) ; and

$$F(X_1, Y_1) = \iint_{R_{25}} P(X_2, Y_2 / X_1, Y_1) dX_2 dY_2 = (1/4) \cdot [\text{erf}(d - \mu_2) / (\sqrt{2}\sigma_{nd}) + \text{erf}(d + \mu_2) / (\sqrt{2}\sigma_{nd})] \cdot [\text{erf}(d - \lambda_2) / (\sqrt{2}\sigma_{nd})$$

$$+ \text{erf}(d + \lambda_2) / (\sqrt{2}\sigma_{nd})] - (1/4\pi) [\text{erf}(d - \lambda_2) / (\sqrt{2}\sigma_{nd}) + \text{erf}(d + \lambda_2) / (\sqrt{2}\sigma_{nd})] \cdot$$

$$\sum_{k=0}^{\infty} (-1)^k \cdot \{1/(\sqrt{2}\sigma_{nd})\}^{2k} \cdot a_{2k,0} \cdot \{ \exp -[(d - \mu_2) / (\sqrt{2}\sigma_{nd})]^2 \} \cdot (\text{cont.})$$

$$\begin{aligned}
 & H_{2k-1} \left[ \frac{(d-\mu_2)}{\sqrt{2}\sigma_{nd}} \right] + \exp \left[ -\left( \frac{d+\mu_2}{\sqrt{2}\sigma_{nd}} \right)^2 \right] \cdot H_{2k-1} \left[ \frac{(d+\mu_2)}{\sqrt{2}\sigma_{nd}} \right] \\
 & - \left( \frac{1}{2\sqrt{\pi}} \right) \cdot \left[ \operatorname{erf} \left( \frac{d-\mu_2}{\sqrt{2}\sigma_{nd}} \right) + \operatorname{erf} \left( \frac{d+\mu_2}{\sqrt{2}\sigma_{nd}} \right) \right] \cdot \sum_{L=1}^{\infty} (-1)^L \cdot \left\{ \frac{1}{(\sqrt{2}\sigma_{nd})} \right\}^{2L} \\
 & \cdot a_{0,2l} \cdot \left\{ \exp \left[ -\left( \frac{d-\lambda_2}{\sqrt{2}\sigma_{nd}} \right)^2 \right] \cdot H_{2l-1} \left[ \frac{(d-\lambda_2)}{\sqrt{2}\sigma_{nd}} \right] + \exp \left[ -\left( \frac{d+\lambda_2}{\sqrt{2}\sigma_{nd}} \right)^2 \right] \cdot H_{2l-1} \left[ \frac{(d+\lambda_2)}{\sqrt{2}\sigma_{nd}} \right] \right\} \\
 & + \left( \frac{1}{\pi} \right) \cdot \sum_{K,L=1}^{\infty} (-1)^{K+L} \cdot a_{2k,2l} \cdot \left\{ \frac{1}{(\sqrt{2}\sigma_{nd})} \right\}^{2K+2L} \\
 & \cdot \left\{ \exp \left[ -\left( \frac{d-\mu_2}{\sqrt{2}\sigma_{nd}} \right)^2 \right] \cdot H_{2k-1} \left[ \frac{(d-\mu_2)}{\sqrt{2}\sigma_{nd}} \right] + \exp \left[ -\left( \frac{d+\mu_2}{\sqrt{2}\sigma_{nd}} \right)^2 \right] \cdot H_{2k-1} \left[ \frac{(d+\mu_2)}{\sqrt{2}\sigma_{nd}} \right] \right\} \\
 & \cdot \left\{ \exp \left[ -\left( \frac{d-\lambda_2}{\sqrt{2}\sigma_{nd}} \right)^2 \right] \cdot H_{2l-1} \left[ \frac{(d-\lambda_2)}{\sqrt{2}\sigma_{nd}} \right] + \exp \left[ -\left( \frac{d+\lambda_2}{\sqrt{2}\sigma_{nd}} \right)^2 \right] \cdot H_{2l-1} \left[ \frac{(d+\lambda_2)}{\sqrt{2}\sigma_{nd}} \right] \right\} \quad (23)
 \end{aligned}$$

Substituting (20) and (23) into (22) we get the error probability for one element  $p_{e, A25}$ . The  $p_{e, Ai}$ ,  $i \neq 25$  are calculated in the same way, substitute into (14) to get the average error probability;  $p_e$  for 49-QPRS at specific conditions of back-off; uplink and downlink signal-to-noise ratio and signal-to-interference ratio.

### III-COMPUTATION, RESULTS AND COMMENTS

Each infinite-double integration defining conditional error probability is numerically evaluated using the Cartesian products of Gauss-Hermit quadrature formulas [11]. The amplitude-phase model of the TWTA nonlinearities represented in [7]-[9] by:

$$\begin{aligned}
 & F(R) = 10 \cdot \left( \alpha \left\{ \cos \left[ \log \left( \frac{R}{\hat{R}} \right) / \beta \right] - 1 \right\} \right) \quad R > \tilde{R} \\
 & = R \quad R \leq \tilde{R} \quad , \text{ and} \\
 & \psi(R) = K_1 \left[ 1 - \exp \left( -K_2 R^2 \right) \right] + K_3 R^2 \quad (24)
 \end{aligned}$$

Where  $\alpha$ ,  $\beta$ ,  $\hat{R}$ ,  $\tilde{R}$ ,  $K_1$ ,  $K_2$  and  $K_3$  are constants chosen to fit the measured amplitude and phase characteristics of the TWTA of type: A-TRW-DSCS-II with constant parameters above given to be 0.394, 0.475, 2.317, 0.355, 0.605, 0.66 and 1/102.4 respectively.

The TWTA average transmitted power is given by:

$$\begin{aligned}
 & \left[ \bar{P}_t \right]_{\max} = \hat{R}^2 / 2 \quad \text{at full saturation mode, and} \\
 & \bar{P}_t = \left( \hat{R}^2 / 2 \right) \cdot 10^{(-BO/10)} \quad \text{at any other operation mode} \quad (25)
 \end{aligned}$$

Where BO denotes the degree of input back-off in dB.

The average power transmitted for 49-ary QPRS is given as:

$$\bar{P}_t = \sum_i \sum_j [(a_i^2 + b_j^2)^{1/2} A]^2 p(a_i) \cdot p(b_j) = 10 A^2 \quad (26)$$

From (25) and (26) we can get an expression for the amplification factor ; A given as :

$$A = (\hat{R} / \sqrt{20}) \cdot 10^{(-BO / 20)} \quad (27)$$

The uplink  $\sigma_{nu}$  and  $\sigma_{cu}$  and the downlink  $\sigma_{nd}$  and  $\sigma_{cd}$  expressed in terms of uplink and downlink  $\rho_{nu}$  and  $\rho_{nd}$  and  $\rho_{cu}$  and  $\rho_{cd}$  respectively as follows :

$$\begin{aligned} \sigma_{nu}^2 &= \bar{P}_t / \rho_{nu} & \text{and} & & \sigma_{nd}^2 &= \bar{P}_r / \rho_{nd} & ; \text{and} \\ \sigma_{cu}^2 &= \bar{P}_t / \rho_{cu} & \text{and} & & \sigma_{cd}^2 &= \bar{P}_r / \rho_{cd} \end{aligned} \quad (28)$$

Where  $\bar{P}_r$  is the average power at the TWTA output , assuming noise and interference signal powers are neglected compared with the uplink signal power  $P_t$  , is given by :

$$\bar{P}_r = \sum_i \sum_j [ F\{(a_i^2 + b_j^2)^{1/2} A \}]^2 p(a_i) p(b_j) \quad (29)$$

It is found from the results that the later depend upon back-off , signal-to-noise ratio and signal-to-interference ratio but the back-off is dominated factor ; a sample of the computed results are shown in Fig. (3) and Fig. (4) . The appropriate values of threshold level ; d and compensation  $\theta$  can only be arrived at by minimizing the average symbol error probabilities;  $P_e$  . Fig. (5) shows the minimum average error probability ;  $P_e$  detection for different values of threshold levels d and different compensation phases  $\theta$  .

#### IV-CONCLUSION

In this paper we presented a complete analysis for the performance of 49-ary QPRS through two link nonlinear satellite channels in the presence of AWGN and CCI preceding and following the TWTA nonlinearities . An expression of the average symbol error probability has been derived and evaluated using Gauss-Hermite quadrature techniques for infinite-double integration and Hermit Polynomial for double summation . It is found from the results that  $P_e$  ; as a measure for the system performance ; depends upon back-off , signal-to-noise ratio and signal-to-interference ratio but back-off is the dominated factor . The values of threshold levels and compensation phase are found to be highly correlated and can only be arrived at optimum by minimizing the average symbol error probability  $P_e$  . The results are useful for : satellite ; data and information Networks and radio-relay communications . QPRS ; for more spectral efficient ; is candidatd to replace the other modulation techniques in the near future .

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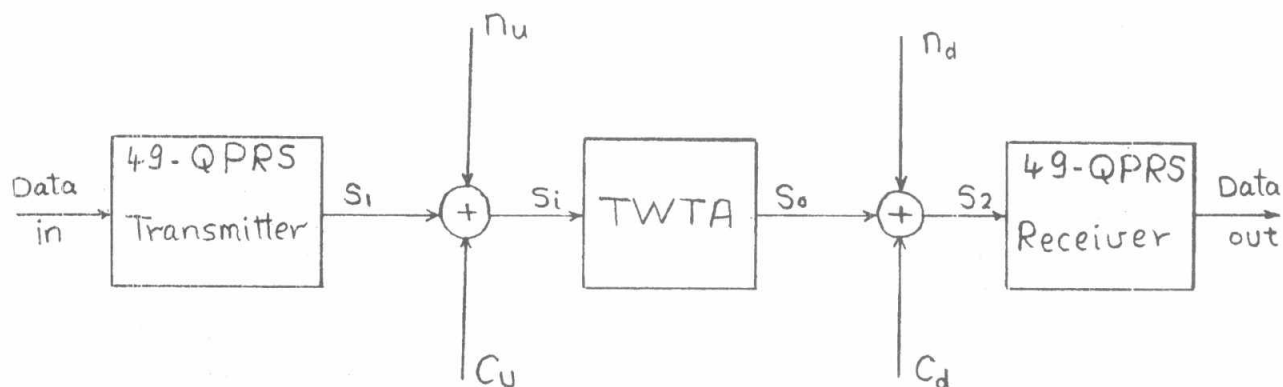


Fig. (1) System Model



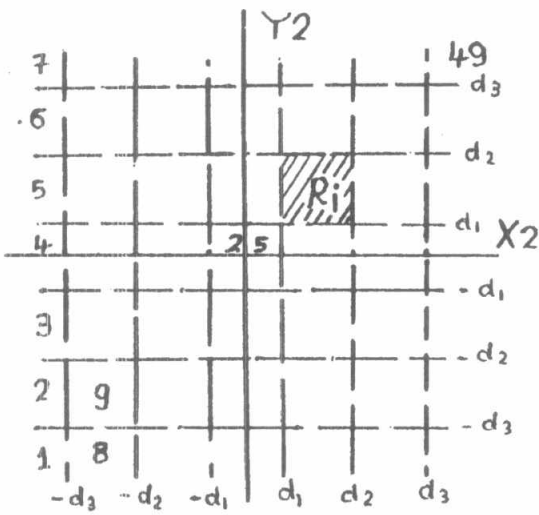
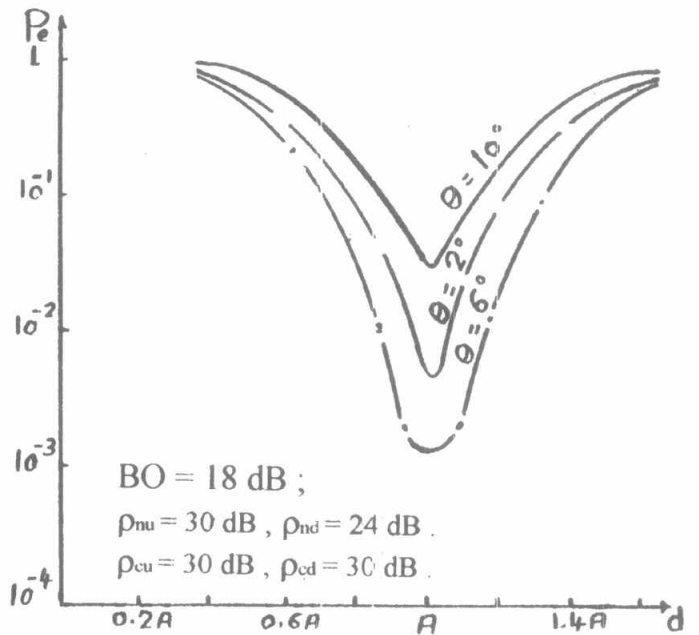


Fig. (2) Region for correct decision ; Ri.



BO = 18 dB ;  
 $\rho_{nu} = 30$  dB ,  $\rho_{nd} = 24$  dB .  
 $\rho_{cu} = 30$  dB ,  $\rho_{cd} = 30$  dB .

Fig. (5) Minimum Pe detection .

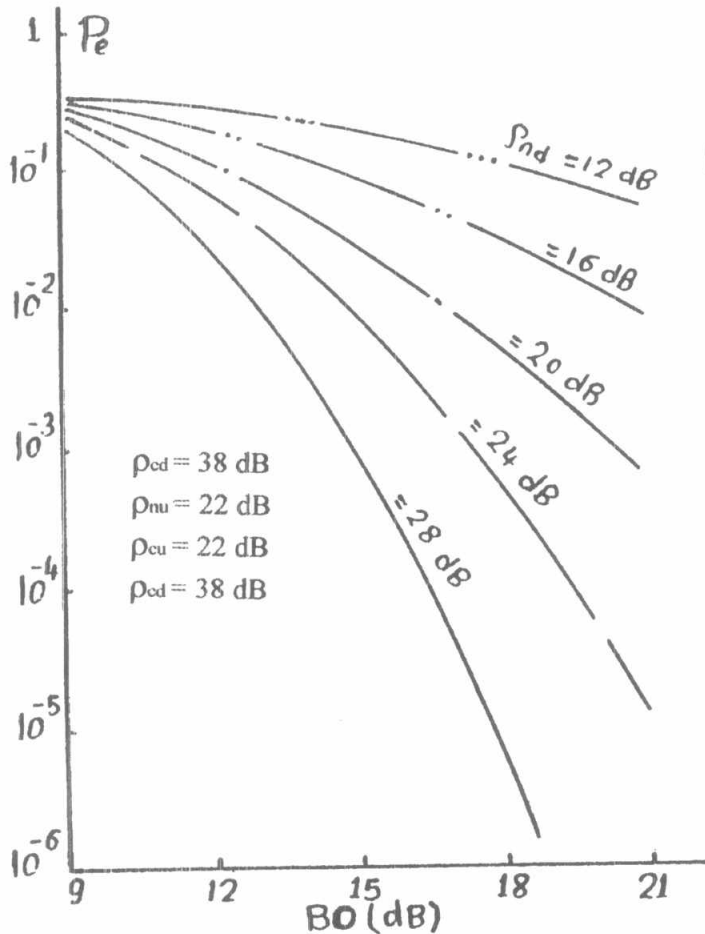


Fig. (3) Pe as function of BO.

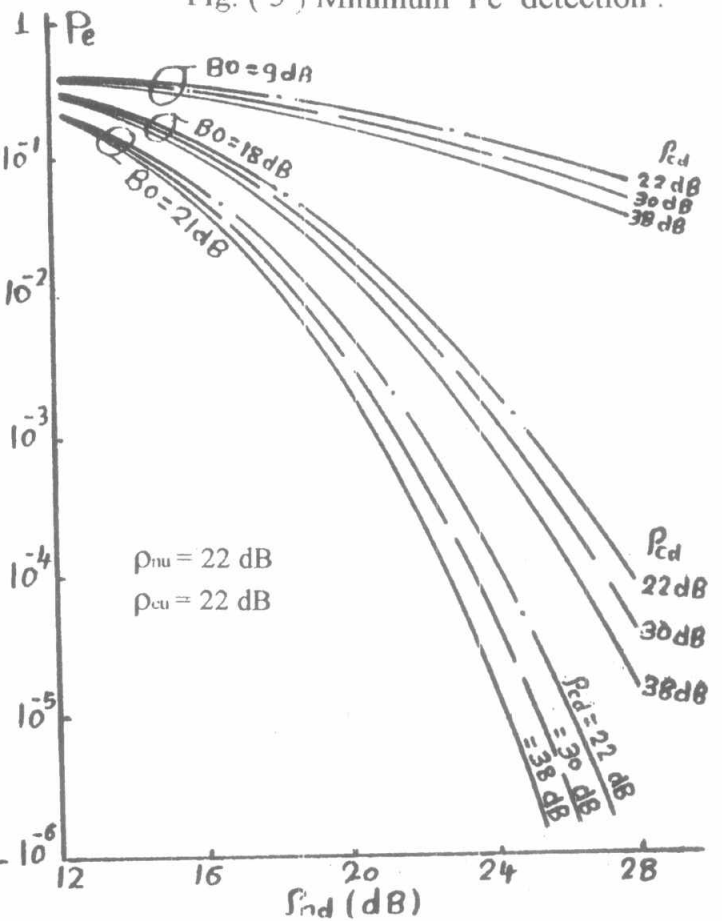


Fig. (4) Pe as function of  $\rho_{nd}$  .

